



Dynamical fluctuations in critical regime and across the 1st order phase transition

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Abstract

In this proceeding, we study the dynamical evolution of the sigma field within the framework of Langevin dynamics. We find that, as the system evolves in the critical regime, the magnitudes and signs of the cumulants of sigma field, C_3 and C_4 , can be dramatically different from the equilibrated ones due to the memory effects near T_c . For the dynamical evolution across the 1st order phase transition boundary, the supercooling effect leads the sigma field to be widely distributed in the thermodynamical potential, which largely enhances the cumulants C_3 , C_4 , correspondingly.

Keywords: Dynamical critical phenomena, correlations and fluctuations, critical point, first order phase transition

1. Introduction

The STAR collaboration has measured the higher order cumulants of net protons in Au+Au collisions with collision energy ranging from 7.7 to 200 GeV [1, 2, 3]. The experimental data of $\kappa\sigma^2$ ($\kappa\sigma^2 = C_4/C_2$) shows a large deviation from the poisson baseline, and presents an obvious non-monotonic behavior at lower collision energies, indicating the potential of discovery the QCD critical point in experiment [3].

Within the framework of equilibrium critical fluctuations, we calculated the fluctuations of net protons through coupling the fluctuating sigma field with particles emitted from the freeze-out surface of hydrodynamics [4]. Our calculations can fit the C_4 and $\kappa\sigma^2$ data by tuning the related parameters, as well as qualitatively describing the acceptance dependence of the cumulants of net protons. However, our calculations over-predicted both C_2 and C_3 data due to the positive critical fluctuations, which are in fact intrinsic for the traditional equilibrium critical fluctuations [5, 6, 7].

Recently, Mukherjee and his collaborators have studied the non-equilibrium evolution for the cumulants of sigma field in the critical regime, based on the Fokker-Plank equation [8]. The numerical results showed that, as the system evolves near the critical point, the memory effects keep the signs of the Skewness and Kurtosis at the early time, which are opposite to the equilibrium ones at the freeze-out points below T_c . However, their calculations focus on the zero mode of the sigma field, which has averaged out the spatial information and can not directly couple with particles to compare with the measured experimental data.

To solve this problem, one could directly trace the whole space-time evolution of the sigma field within the framework of Langevin dynamics. In this proceeding, we will present the main results from our recent

numerical simulations of the Langevin equation of the sigma field, using an effective potential of the linear sigma model with constituent quarks. As discovered in early work [8], we also observe clearly memory effects as the system evolves in the critical regime, which largely influence the signs and values of the cumulants C_3 and C_4 . In addition, we find that for the dynamical evolution across the 1st order phase transition boundary, the supercooling effect leads the sigma field to be widely distributed in the thermodynamical potential, which largely enhances the corresponding cumulants $C_2 - C_4$ at the freeze-out points.

2. The formalism and set-ups

In this proceeding we focus on the dynamical evolution of the order parameter field within the framework of the linear sigma model with constituent quarks. According to the classification of the dynamical universality classes [9], our approach belongs to model A, which is not in the same dynamical universality class of the full QCD matter evolution [10], but easy for numerical implementations. The linear sigma model is an effective model to describe the chiral phase transition, which presents a complete phase diagram on the (T, μ) plane with different phase transition scenarios, including a critical point [11, 12]. As the mass of the sigma field vanishes at the critical point, the related thermodynamical quantities become divergent due to the critical long wavelength fluctuations of the sigma field. In the critical regime, the semi-classical evolution of the long wavelength mode of the sigma field can be described by a Langevin equation [13]:

$$\partial^\mu \partial_\mu \sigma(t, x) + \eta \partial_t \sigma(t, x) + \frac{\delta V_{eff}(\sigma)}{\delta \sigma} = \xi(t, x), \quad (1)$$

where η is the damping coefficient and $\xi(t, x)$ is the noise term. Both of these two terms come from the interaction between the sigma field and quarks [13]. Here we take η as a free parameter, and input white noise in the calculation. The effective potential of the sigma field is written as:

$$V_{eff}(\sigma) = U(\sigma) + \Omega_{\bar{q}q}(\sigma) = \frac{\lambda^2}{4} (\sigma^2 - v^2)^2 - h_q \sigma - U_0 + \Omega_{\bar{q}q}(\sigma) \quad (2)$$

where $U(\sigma)$ is the vacuum potential of the chiral field, and the related values of λ , σ , h_q and U_0 are set by the vacuum properties of hadrons. Note that here we have neglected the fluctuations of $\vec{\pi}$, since its mass is finite in the critical regime. $\Omega_{\bar{q}q}$ represents the contributions from thermal quarks, which has the form:

$$\Omega_{\bar{q}q}(\sigma; T, \mu) = -d_q \int \frac{d^3 p}{(2\pi)^3} \{E + T \ln[1 + e^{-(E-\mu)/T}] + T \ln[1 + e^{-(E+\mu)/T}]\} \quad (3)$$

where d_q is the degeneracy factor of quarks, and the energy of the quark is $E = \sqrt{p^2 + M(\sigma)^2}$. Here we introduce an effective mass for the quark, $M(\sigma) = m_0 + g\sigma$ [4, 6]. After the chiral phase transition, quarks obtain effective mass and turn to constituent quarks. Based on the effective potential Eq. (2), one can obtain the corresponding phase diagram in the (T, μ) plane, which is plotted in the left panel of Fig. 1.

For the numerical implementations, we first construct the profiles of the initial sigma field according to the probability function $P[\sigma(\mathbf{x})] \sim \exp(-\mathcal{E}(\sigma)/T)$ (where $\mathcal{E}(\sigma) = \int d^3 x \left[\frac{1}{2} (\nabla \sigma(x))^2 + V_{eff}(\sigma(x)) \right]$), then evolve the sigma field event by event through solving the Langevin equation Eq.(1). With the obtained space-time configurations of the sigma fields, the moments of the sigma field can be calculated as:

$$\mu'_n = \langle \sigma^n \rangle = \frac{\int d\sigma \sigma^n P[\sigma]}{\int d\sigma P[\sigma]}, \quad (4)$$

where $\sigma = \frac{1}{V} \int d^3 x \sigma(\mathbf{x})$. The cumulants of sigma field can be obtained from these above moments.

Note that numerically solving Eq.(1) also needs to input the space-time information of the local temperature and chemical potential, $T(t, x, y, z)$ and $\mu(t, x, y, z)$, for the effective potential, which are in principle provided by the evolution of a back-ground heat bath. For simplicity, we assume that the heat bath evolves

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