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# Semi-braces and the Yang-Baxter equation 

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#### Abstract

In this paper we obtain new solutions of the Yang-Baxter equation that are left non-degenerate through left semi-braces, a generalization of braces introduced by Rump. In order to provide new solutions we introduce the asymmetric product of left semi-braces, a generalization of the semidirect product of braces, that allows us to produce several examples of left semi-braces.


Keywords: Quantum Yang-Baxter equation, set-theoretical solution, skew brace, semi-brace
2010 MSC: 16T25, 16Y99, 16N20, 81R50

## 1. Introduction

The Yang-Baxter equation is a basic equation of statistical mechanics that arose from a work of Yang's [18] and one of Baxter's [3]. Recall that if $V$ is a vector space, then a function $R: V \otimes V \rightarrow V \otimes V$ is said to be a solution of the Yang-Baxter equation if

$$
R_{12} R_{13} R_{23}=R_{23} R_{13} R_{12}
$$

is satisfied, where $R_{12}=R \otimes \mathrm{id}_{V}, R_{23}=\mathrm{id}_{V} \otimes R, R_{13}=\left(\mathrm{id}_{V} \otimes \tau\right)\left(R \otimes \mathrm{id}_{V}\right)\left(\mathrm{id}_{V} \otimes \tau\right)$, and $\tau$ the twist map on $V \otimes V$.
In 1992 Drinfeld [8] formally proposed to study a simplified case, i.e., the set-theoretical solution of the Yang-Baxter equation. Specifically, fixed a basis $X$ on the vector space $V$ we may find all solutions $R$ induced by a linear extension of a function $\mathcal{R}: X \times X \rightarrow X \times X$, where $X$ is a basis for $V$. In this case, $\mathcal{R}$ is called a set-theoretic solution of the quantum Yang-Baxter equation. It is not difficult to see that if $\tau: X \times X \rightarrow X \times X$ is the twist map then a map $\mathcal{R}: X \times X \rightarrow X \times X$ if and only if the mappung $r=\tau \circ \mathcal{R}$ is a solution of the braid equation

$$
r_{1} r_{2} r_{1}=r_{2} r_{1} r_{2}
$$

where $r_{1}:=r \times \operatorname{id}_{X}$ and $r_{2}:=\operatorname{id}_{X} \times r$. Later, seminal papers of Etingof, Schedler and Soloviev [9] and of Gateva-Ivanova and M. Van den Bergh in [10] laid the groundwork for the study of a particular class of these solutions, the non-degenerate involutive ones, i.e., the solutions $(X, r)$ such that the first and the

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