



## Letter

## Enhancing heat transfer at the micro-scale using elastic turbulence

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## ABSTRACT

Small concentrations of a high-molecular-weight polymer have been used to create so-called “elastic turbulence” in a micro-scale serpentine channel geometry. It is known that the interaction of large elastic stresses created by the shearing motion within the fluid flow with streamline curvature of the serpentine geometry leads initially to a purely-elastic instability and then the generation of elastic turbulence. We show that this elastic turbulence enhances the heat transfer at the micro-scale in this geometry by up to 300% under creeping flow conditions in comparison to that achieved by the equivalent Newtonian fluid flow.

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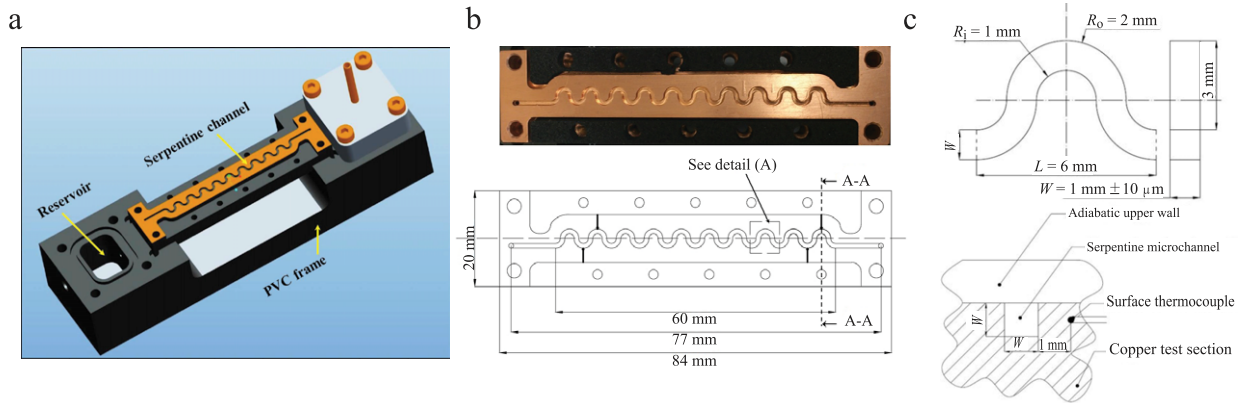
In so-called “creeping flow”, i.e., flows for which the Reynolds number ( $Re$ ) remains small ( $Re < 1$ ), Newtonian fluids remain laminar and steady. Consequently efficient mixing and heat transfer to the fluid are problematic for very viscous systems or liquid flows at small scales (e.g., microfluidics) as they are essentially diffusion/conduction dominated. One method to circumnavigate these problems is to make the fluid non-linear by the addition of small amounts of high molecular-weight polymer. The resulting viscoelastic solution enables fluid flows at arbitrarily small values of  $Re$  to exhibit “turbulent-like” characteristics such as randomly fluctuating fluid motion excited across a broad range of temporal and spatial scales [1–6]. Steinberg and co-workers [1–4] showed that highly-elastic viscoelastic fluids can undergo a series of flow transitions from viscometric laminar flow, to periodic flow, to apparently chaotic flow, and then to fully developed elastic turbulence (ET) in conditions of negligible inertia ( $Re < 1$ ) and this has been shown in a range of flows: swirling flow between parallel disks [1,4,5], in serpentine or wavy channels [2–4,6] and in concentric cylinder devices [4,7]. The instabilities and resulting non-linear interactions are “purely-elastic” in nature – driven by the elastic (normal) stresses developed in flow – and occur at Reynolds numbers far removed from the usual turbulence observed for Newtonian fluids which is inertial in nature (critical  $Re$  on the order

of 1000 for internal flows). Although the original work of Groisman and Steinberg [1] has elicited a significant degree of interest (and the passive-scalar mixing effectiveness of the regime has been mentioned repeatedly [1,3–7]) outside of the quantitative studies on passive scalar mixing [8,9], little work has yet been carried out to assess this effectiveness in other typical “mixing” scenarios. An exception to this is the study of Poole et al. [10] where ET was used to create oil in polymer solution emulsions in a swirling flow between parallel disks arrangement (similar to that used in Ref. [1]) where for a Newtonian oil and continuous phase, at identical conditions, no emulsification occurred at all. Flows containing streamline curvature are ideal for encouraging elastic instabilities and elastic turbulence as it is generally accepted that purely-elastic instabilities arise as a consequence of both elastic normal stresses and streamline curvature [11]—although some analytical work [12] and experimental evidence [13] are beginning to show that even parallel shear flows may exhibit ET providing the initial perturbation is sufficiently strong.

The growth of “microfluidic” research, and the major fundamental interest and applications of such flows [14], has revealed previously unobserved instabilities and flow phenomena that occur solely due to viscoelasticity. In fact some of the key publications on ET [4,6,13] have used such micro-geometries to access the required parameter space (low inertia, high elastic stresses). The small scale nature of such flows leads directly to the viscoelastic behavior observed: the small length scale simultaneously makes the Reynolds number ( $Re \equiv \rho UD/\mu$ ) small and the Deborah ( $De \equiv \lambda U/D$ ) or Weissenberg ( $Wi \equiv \lambda U/D$ ) numbers, which characterize the degree of elasticity in the flow, large (where  $\rho$

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**Fig. 1.** (a) Isometric view of the experimental facility, (b) plan views of the serpentine channel, and (c) detailed view and cross section of the serpentine channel.

is density,  $U$  a velocity scale,  $D$  a length scale,  $\mu$  a viscosity, and  $\lambda$  a characteristic or relaxation time for the fluid). The  $De$  number is a ratio of characteristic timescales (fluid to flow) and the  $Wi$  number is the ratio of elastic to viscous forces. Thus at the micro-scale, due to the small flow time scales and the high strain rates attainable, viscoelastic effects will become important even for dilute solutions which appear Newtonian in macro-scale flows. In the current letter we utilize this effect in a microfluidic serpentine channel [3,15–17]. Typical  $Wi$  numbers required to observe elastic turbulence have been reported as: swirling flow between parallel disks  $Wi \sim 3.5$  [1], Taylor–Couette flow  $Wi \sim 4$  [4], serpentine channel flow  $Wi \sim 3.2$  (onset),  $> 6.7$  (developed) [4], 1.4–3.5 (onset), 10 (developed) [3], 7.5–15 (developed) [6]. By the use of high shear rates, viscous solvents, and an extremely high-molecular-weight polymer, we reach  $Wi \sim 100$ .

As far as the effect of ET on heat transfer is concerned, no work has been reported hitherto. For Newtonian fluids at low Reynolds numbers, e.g., in microfluidics applications, both thermal and viscous development are short ( $\sim$ pipe diameter) and the Nusselt number ( $Nu$ ) is an order one constant which is independent of the Reynolds number. The heat transfer is conduction-dominated and long fluid residence times are required to achieve significant temperature increases. In contrast, if (inertial) turbulent conditions can be reached then heat can be transferred much more efficiently. For example in a straight pipe at a Reynolds number of 3000 the Nusselt number is increased by a factor of 10 above the laminar value (for identical Prandtl numbers). It might be anticipated that such large increases in heat transfer coefficients may also occur with ET provided the base flow is free from convection (and therefore heat is treated as a passive scalar). The current paper addresses this question and demonstrates the potential of using ET to enhance heat transfer in microfluidics applications.

The heat transfer measurements were conducted in a serpentine channel as shown in Fig. 1(a). The serpentine channel was micro machined into a piece of copper and consisted of 20 half-loops with inner and outer radii of 1 mm and 2 mm, respectively. The serpentine channel was flanked on either side by straight inlet and outlet channel sections and had a total length of 77 mm (see Fig. 1(b)). The channel had a square cross section with a depth and width of  $1.075 \pm 0.01$  mm (see Fig. 1(c)). The entire channel was mounted on a PVC substrate, which encompassed two separate reservoirs (one at either end of the channel), and the channel was enclosed by an upper wall fabricated from PVC.

The entire facility was housed in a Techne TE-10A water bath continuously-stirred and maintained at a temperature of 30°C (leading to typical fluid temperature increases of 4°C–8°C). The copper bottom and copper side walls guaranteed isothermal boundary conditions and the insulating properties of the PVC ensured an adiabatic boundary condition on the upper wall. The surface temperature of the serpentine channel was monitored by four

$K$ -type thermocouples each embedded 1 mm from the channel side walls. The enhancement of heat transfer generated by the complex fluid flowing through the serpentine channel was quantified by measuring the temperature difference between the two reservoirs (before and after the serpentine channel) with  $K$ -type thermocouples. The  $K$ -type thermocouples had a quoted uncertainty of  $\pm 1^\circ\text{C}$  and were calibrated against a mercury thermometer of certified accuracy ( $\pm 0.1^\circ\text{C}$ ).

The pressure drop along the channel was measured by a Validyne DP15–26 differential pressure transducer. The pressure transducer estimated the streamwise pressure gradient ( $\Delta P$ ), from which the friction factor ( $f = [\Delta P / (0.5\rho U^2)](D_h/L)$ , where  $U$  is the average velocity,  $D_h$  is the hydraulic diameter, and  $L$  is the path-length equal to 111.25 mm in our set-up) could be determined, by measuring the difference in pressure across two pressure taps installed on the upper wall of each reservoir. The pressure transducer used two different diaphragms to capture the full working range: one had a working range of 0.2 bar whilst the other had a range of 2 bar, both are said to be accurate to  $\pm 0.25\%$  full scale, and both diaphragms were periodically calibrated against an MKS Baratron differential pressure transducer (1000 torr fsd).

Fluid was pumped through the serpentine channel by a regulated pressure vessel. The fluid was discharged into a beaker and weighed by a Denver TP-1502 precision balance allowing a measurement of the mass flow rate (uncertainty  $\pm 0.03$  mg). The working fluids were solutions of a high-molecular-weight ( $\sim 18 \times 10^6$  g/mol) polyacrylamide supplied by polysciences, with mass concentrations of 80 ppm and 120 ppm in a Newtonian solvent comprised of 65% sucrose, 1% NaCl, and 34% water (all by mass). At these concentrations the solutions are either dilute or semi-dilute as  $c/c^* \sim 1$ , where  $c$  is the concentration of polymer and  $c^*$  is the critical overlap concentration which is approximately 100 ppm (0.01%) when determined from intrinsic viscosity measurements (assuming  $c^*$  is roughly the inverse of the intrinsic viscosity). All rheological measurements of the fluids were performed with a TA Instruments AR1000N controlled-stress rheometer with a cone-and-plate geometry (60 mm diameter,  $2^\circ$  cone angle).

Those shown in Fig. 2(a) are shear viscosity ( $\eta$ ) measurements versus shear rate ( $\dot{\gamma}$ ) for the Newtonian and complex fluids used in the present study. The Newtonian fluid has a constant shear viscosity of 0.164 Pa·s at 20°C, and the polymer solutions both exhibit slight shear-thinning behavior. The shear viscosity data of the complex fluids have been fit to the Carreau–Yasuda model [18], which allows an estimate of the shear viscosity ( $\eta_{CY}$ ) values at any shear rate:

$$\eta_{CY} = \eta_\infty + \frac{\eta_0 - \eta_\infty}{[1 + (\lambda_{CY}\dot{\gamma})^a]^{n/a}} \quad (1)$$

In Eq. (1),  $\eta_0$  is the zero-shear-rate viscosity,  $\eta_\infty$  is the infinite-shear-rate viscosity,  $\lambda_{CY}$  is a constant which characterizes the

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