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Fabrício Benevides, Victor Campos, Mitre C. Dourado, Rudini M. Sampaio, Ana Silva

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### ACCEPTED MANUSCRIPT

# The maximum infection time in the geodesic and monophonic convexities $\stackrel{\diamond}{\Rightarrow}$

Fabrício Benevides<sup>a,1,\*</sup>, Victor Campos<sup>a,1</sup>, Mitre C. Dourado<sup>b,1</sup>, Rudini M. Sampaio<sup>a,1</sup>, Ana Silva<sup>a,1</sup>

<sup>a</sup> Universidade Federal do Ceará, Fortaleza, Brazil <sup>b</sup> Universidade Federal do Rio de Janeiro, Rio de Janeiro, Brazil

#### Abstract

Recent papers investigated the maximum infection time  $t_{P3}(G)$  of the  $P_3$ convexity (also called maximum time of 2-neighbour bootstrap percolation) and the maximum infection time  $t_{mo}(G)$  of the monophonic convexity. In 2014, it was proved that, for bipartite graphs, deciding whether  $t_{P3}(G) \ge k$ is polynomial time solvable for  $k \le 4$ , but is NP-complete for  $k \ge 5$  [23]. In 2015, it was proved that deciding whether  $t_{mo}(G) \ge 2$  is NP-Complete even for bipartite graphs [12]. In this paper, we investigate the maximum infection time  $t_{gd}(G)$  of the geodesic convexity. We prove that deciding whether  $t_{gd}(G) \ge k$  is polynomial time solvable for k = 1, but is NP-complete for  $k \ge 2$  even for bipartite graphs. We also present an  $O(n^3m)$ -time algorithm to determine  $t_{gd}(G)$  and  $t_{mo}(G)$  in distance-hereditary graphs. For this, we characterize all minimal hull sets of a general graph in the monophonic convexity. Moreover, we improve the complexity of the fastest known algorithm for finding a minimum hull set of a general graph in the monophonic convexity.

*Keywords:* Geodesic convexity, maximum infection time, monophonic hull number, monophonic convexity

\*Corresponding author

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*Email addresses:* fabricio@mat.ufc.br (Fabrício Benevides), campos@lia.ufc.br (Victor Campos), mitre@dcc.ufrj.br (Mitre C. Dourado), rudini@lia.ufc.br (Rudini M. Sampaio), anasilva@mat.ufc.br (Ana Silva)

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