



Hubble parameter data constraints on dark energy

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ABSTRACT

We use Hubble parameter versus redshift data from Stern et al. (2010) [1] and Gaztañaga et al. (2009) [2] to place constraints on model parameters of constant and time-evolving dark energy cosmological models. These constraints are consistent with (through not as restrictive as) those derived from supernova Type Ia magnitude-redshift data. However, they are more restrictive than those derived from galaxy cluster angular diameter distance, and comparable with those from gamma-ray burst and lookback time data. A joint analysis of the Hubble parameter data with more restrictive baryon acoustic oscillation peak length scale and supernova Type Ia apparent magnitude data favors a spatially-flat cosmological model currently dominated by a time-independent cosmological constant but does not exclude time-varying dark energy.

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1. Introduction

It is well established that the Universe is currently undergoing accelerated cosmological expansion. Observational evidence for the accelerated expansion comes from supernova Type Ia (SNIa) apparent magnitude measurements as a function of redshift [3, 4], cosmic microwave background (CMB) anisotropy data [5] combined with low estimates of the cosmological mass density [6], and baryon acoustic oscillation (BAO) peak length scale estimates [2, 7, 8].

The underlying mechanism responsible for this accelerated expansion is not yet well characterized. The “standard” general relativistic model of cosmology has an energy budget that is currently dominated by far by dark energy, a negative-pressure substance that powers the accelerated expansion. (Another possibility is that the above observations are a manifestation of the breakdown of general relativity on large cosmological length scales. In this Letter we assume that general relativity provides an adequate description of gravitation on cosmological length scales.) Dark energy can vary weakly in space and evolve slowly in time, though current data are consistent with it being a cosmological constant. For recent reviews see [9].

There are many dark energy models under discussion (for recent discussions see [10], and references therein). The current

“standard” model is the Λ CDM model [11] where the accelerated cosmological expansion is powered by Einstein’s cosmological constant, Λ , a spatially homogeneous fluid with equation of state parameter $\omega_\Lambda = p_\Lambda/\rho_\Lambda = -1$ (where p_Λ and ρ_Λ are the fluid pressure and energy density). In this model the cosmological energy budget is dominated by far by ρ_Λ , with cold dark matter (CDM) being the second largest contributor. The Λ CDM model provides a reasonable fit to most observational constraints, although the “standard” CDM structure formation model might be in some observational trouble (see, e.g., [12]). In addition, the Λ CDM model raises some puzzling conceptual questions.

If the dark energy density slowly decreased in time (rather than remaining constant like ρ_Λ), the energy densities of dark energy and nonrelativistic matter (CDM and baryons) would remain comparable for a longer period of time, and so alleviate what has become known as the Λ CDM coincidence puzzle. In addition, a slowly decreasing effective dark energy density, based on a more fundamental physics model that is applicable at an energy density scale much larger than an meV, could result in the current observed dark energy density scale of order an meV through gradual decrease over the long lifetime of the Universe, another unexplained feature in the context of the Λ CDM model. Thus a slowly decreasing dark energy density could resolve some of the puzzles of the Λ CDM model [13].

The XCDM parametrization is often used to describe a slowly decreasing dark energy density. In this parametrization the dark energy is modeled as a spatially homogeneous (X) fluid with an equation of state parameter $w_X = p_X/\rho_X$, where $w_X < -1/3$ is an arbitrary constant and p_X and ρ_X are the pressure and energy density of the X-fluid. When $w_X = -1$, the XCDM parametrization

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reduces to the complete and consistent Λ CDM model. For any other value of w_X ($< -1/3$) the XCDM parametrization is incomplete as it cannot describe spatial inhomogeneities (see, e.g., [14]). Here we study the XCDM parametrization only in the spatially-flat cosmological case.

The ϕ CDM model – in which dark energy is modelled as a scalar field ϕ with a gradually decreasing (in ϕ) potential energy density $V(\phi)$ – is the simplest complete and consistent model of a slowly decreasing (in time) dark energy density. Here we focus on an inverse power-law potential energy density $V(\phi) \propto \phi^{-\alpha}$, where α is a nonnegative constant [15,13]. When $\alpha = 0$ the ϕ CDM model reduces to the corresponding Λ CDM case. Here we only consider the spatially-flat ϕ CDM cosmological model.

It has been known for some time that a spatially-flat Λ CDM model with current energy budget dominated by a constant Λ is largely consistent with most observational constraints (see, e.g., [16,17]). SNela, CMB, and BAO measurements mentioned above indicate that we live in a spatially-flat Λ CDM model with non-relativistic matter contributing a little less than 30% of the current cosmological energy budget, with the remaining slightly more than 70% contributed by a cosmological constant. These three sets of data carry by far the most weight when determining constraints on models and cosmological parameters.

Future data from space missions will significantly tighten the constraints (see, e.g., [18]). However, at present, it is important to determine independent constraints that can be derived from other presently available data sets. While these data are not yet as constraining as the SNela, CMB and BAO data, they potentially can reassure us (if they provide constraints consistent with those from the better known data), or if the two sets of constraints are inconsistent this might lead to the discovery of hidden systematic errors or rule out the cosmological model under consideration.

Other data that have been used to constrain cosmological parameters include galaxy cluster gas mass fraction (e.g., [17,19]), gamma-ray burst luminosity distance (e.g., [20,21]), large-scale structure (e.g., [22]), strong gravitational lensing (e.g., [23]), and angular size (e.g., [6,24,25]) data. While the constraints from these data are less restrictive than those derived from the SNela, CMB and BAO data, both types of data result in largely compatible constraints that generally support a currently accelerating cosmological expansion. This gives us confidence that the broad outlines of the “standard” cosmological model are now in place.

Measurements of the Hubble parameter as a function of redshift, $H(z)$, have also been used to constrain cosmological parameters (see [26] for a review). A variant of this test uses lookback time data (see, e.g., [27,28]). Building on the work of [29], Simon et al. [30] used the differential ages of 32 passively evolving galaxies to determine 9 $H(z)$ measurements in the redshift range $0.09 \leq z \leq 1.75$. Cosmological constraints derived using these data are described in [31,32]; more recent references may be traced through [33].

Stern et al. (2010, hereafter S10) [1] extended the Simon et al. [30] sample to 11 measurements of $H(z)$ in the redshift range $0.1 \leq z \leq 1.75$. These data have been used for cosmological tests by Shafieloo and Clarkson [34]. It has become common to augment the S10 data with the Gaztañaga et al. (2009, hereafter G09) [2] estimates of $H(z)$ determined from line-of-sight BAO peak position observations. These data, listed in Table 1, have also been used to constrain cosmological parameters (see, e.g., [35,36] and references therein). There are problems with a number of these analyses. Some of them include both the G09 data points at $z = 0.24$ and $z = 0.43$ (which we use here), as well as the G09 single summary data point at $z = 0.34$ that is based on exactly the same data as the two individual points. In addition, a number of these analyses either ignore the G09 systematic errors or incorrectly account for

Table 1

Hubble parameter versus redshift data from S10 and G09. Where $H(z)$ and σ_H are in $\text{km s}^{-1} \text{Mpc}^{-1}$.

z	$H(z)$	σ_H
0.1	69	12
0.17	83	8
0.24	79.69	2.65
0.27	77	14
0.4	95	17
0.43	86.45	3.68
0.48	97	60
0.88	90	40
0.9	117	23
1.3	168	17
1.43	177	18
1.53	140	14
1.75	202	40

them. We account for the G09 statistical and systematic errors by combining them in quadrature; the G09 data points we list in Table 1 are identical to those used by Ma and Zhang [35] and Zhang et al. [26].

In this Letter we use the 13 S10 and G09 $H(z)$ measurements listed in Table 1 to constrain the Λ CDM and ϕ CDM models and the XCDM parametrization. The resulting constraints are compatible with those derived using other techniques. We also use these $H(z)$ data in combination with BAO and SNela measurements to jointly constrain cosmological parameters in these models. Adding the $H(z)$ data tightens the constraints, somewhat significantly in some parts of parameter space for some of the models we study.

Our Letter is organized as follows. In Section 2 we present the basic equations of the three dark energy models we study. Constraints from the $H(z)$ data are derived in Section 3. In Section 4 we determine joint constraints on the dark energy parameters from a combination of data sets. We summarize our main conclusions in Section 5.

2. Basic equations of the dark energy models

The Friedmann equation of the Λ CDM model with spatial curvature can be written as

$$H^2(z, H_0, \mathbf{p}) = H_0^2 [\Omega_{m0}(1+z)^3 + \Omega_\Lambda + (1 - \Omega_{m0} - \Omega_\Lambda)(1+z)^2], \quad (1)$$

where z is the redshift, $H(z, H_0, \mathbf{p})$ is the Hubble parameter, H_0 is the Hubble constant, and the model-parameter set is $\mathbf{p} = (\Omega_{m0}, \Omega_\Lambda)$ where Ω_{m0} is the nonrelativistic (baryonic and cold dark) matter density parameter and Ω_Λ that of the cosmological constant. Throughout, the subscript 0 denotes the value of a quantity today. In this Letter, the subscripts Λ , X and ϕ represent the corresponding quantities of the dark energy component in the Λ CDM, XCDM and ϕ CDM scenarios.

In this work, for computational simplicity, spatial curvature is set to zero in the XCDM and ϕ CDM cases. Then the Friedmann equation for the XCDM parametrization is

$$H^2(z, H_0, \mathbf{p}) = H_0^2 [\Omega_{m0}(1+z)^3 + (1 - \Omega_{m0})(1+z)^{3(1+w_X)}], \quad (2)$$

where the model-parameter set is $\mathbf{p} = (\Omega_{m0}, w_X)$.

In the ϕ CDM model, the inverse power law potential energy density of the scalar field adopted in this Letter is $V(\phi) = \kappa m_p^2 \phi^{-\alpha}$, where m_p is the Planck mass, and α and κ are non-negative constants [15]. In the spatially-flat case the Friedmann equation of the ϕ CDM model is

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