



# Two-charged non-extremal rotating black holes in seven-dimensional gauged supergravity: The single-rotation case

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## ABSTRACT

We construct the solution for non-extremal charged rotating black holes in seven-dimensional gauged supergravity, in the case with only one rotation parameter and two independent charges. Using the Boyer–Lindquist coordinates, the metric is expressed in a generalized form of the ansatz previously presented in [S.Q. Wu, Phys. Rev. D 83 (2011) 121502(R)], which may be helpful to find the most general non-extremal two-charged rotating black hole with three unequal rotation parameters. The conserved charges for thermodynamics are also computed.

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## 1. Introduction

The discovery of the AdS/CFT correspondence stimulates a great deal of interest in constructing rotating charged black holes in gauged supergravities during the last few years. Of particular interest are those non-extremal black hole solutions in spacetime dimensions  $D = 4, 5, 7$ , which respectively correspond to the maximal  $D = 4$ ,  $\mathcal{N} = 8$ , SO(8);  $D = 5$ ,  $\mathcal{N} = 8$ , SO(6); and  $D = 7$ ,  $\mathcal{N} = 4$ , SO(5) gauged supergravities with respective Cartan subgroups  $U(1)^4$ ,  $U(1)^3$  and  $U(1)^2$ . In recent years, there has been much progress in obtaining new, non-extremal, asymptotically AdS black hole solutions of gauged supergravity theories in four, five, six and seven dimensions. For a comprehensive discussion of these solutions, see for example [1]. However, almost all of these solutions can be classified into three catalogues: either setting all of the angular momenta equal; or setting certain  $U(1)$  charges equal; or restricting to supersymmetric solutions. One main reason is that, for non-extremal solutions of gauged supergravity theories, there is no known solution-generating technique that can charge up a neutral solution, instead one must rely on inspired guesswork and apply these strategies to greatly simplify the problem in finding exact solutions. So far, there is no universal method to derive the above-mentioned solutions, namely those listed in [1].

In a recent paper [2] that extends an interesting work [3] in  $D = 4$  to all dimensions, we have presented in a unified fashion

the general non-extremal rotating, charged Kaluza–Klein AdS black holes with only one electric charge and with arbitrary angular momenta in all higher dimensions. The solutions in  $D = 4, 5, 6, 7$  dimensions can be embedded into corresponding gauged supergravities and the scalar potential in the Lagrangian can be rigorously deduced via the Killing spinor equation [4]. What is more, it has been shown that the general solutions in all dimensions share a common and universal metric structure which can not only naturally reduce to the famous Kerr–Schild ansatz in the uncharged case, but also be generalized to all of already-known black hole solutions with multiple pure electric charges, both in the cases of rotating charged black holes in ungauged supergravity and in the cases of nonrotating AdS black holes in gauged supergravity theories. This means that all previously-known supergravity black hole solutions with multiple different electric charges can be recast into a unified metric ansatz, regardless they belong to ungauged theories or gauged ones. In other words, supergravity black hole solutions in gauged theory inherit the same underlying metric structure as their ungauged counterparts. This significant feature of supergravity black hole solutions had not been exploited in any other previous work. Although that work [2] only dealt with the single-charge case in Kaluza–Klein supergravity, it put forward a universal method to construct the most general rotating charged AdS black hole solutions with multiple pure electric charges in gauged supergravity theory. For example, guided by the generalized form of that ansatz, the most general charged rotating AdS<sub>5</sub> solution with three unequal charges and with two independent rotation parameters has been successfully constructed [5] within five-dimensional  $U(1)^3$  gauged supergravity.

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In this Letter, we shall concentrate on constructing new non-extremal rotating charged AdS black hole solutions in the dimension  $D = 7$  which are relevant for the AdS<sub>7</sub>/CFT<sub>6</sub> correspondence in M-theory. The  $D = 7$  case singles it out a unique role since there appears a first-order “odd-dimensional self-duality” for the 4-form field strength, not seen previously in lower-dimensional examples. This feature makes it quite complicated for finding an exact solution. The currently-known charged non-extremal black hole solutions in the seven-dimensional gauged supergravity are as follows. Nonrotating static charged AdS<sub>7</sub> black hole solutions were known [6–8] for a decade because of the AdS/CFT correspondence. The first non-extremal rotating charged AdS black holes with two different electric charges in seven-dimensional gauged supergravity were obtained in [9], in the special case where the three rotation parameters are set equal. Inspired by a special case [9] where both U(1) charges are set equal, Chow [10] found a new rotating charged AdS black hole solution with three independent angular momenta and two equal U(1) charges. The single-charge case within  $D = 7$  Kaluza–Klein supergravity theory was recently found in [2]. However, the most general non-extremal rotating charged AdS black hole solution with all three unequal rotation parameter and two different U(1) charges is still not yet known.

In the present Letter, we shall construct new solution for non-extremal charged rotating black holes in seven-dimensional gauged supergravity, in the case with two independent charges but with only one rotation parameter. This is helped by the metric structure found for the two-charged Cvetič–Youm solution [11] in arbitrary dimensions, which is presented in Appendix A. It should also be pointed out that the recently-found two-charge rotating black holes [12] in four-dimensional gauged supergravity can be cast into the same ansatz. We present the solution in Section 2 and then examine its thermodynamics in Section 3. The conclusion section and the remaining two Appendices B and C summarize our results and present the clue toward constructing the most general solution with two unequal charges and with three unequal rotation parameters in seven-dimensional gauged supergravity.

## 2. Non-extremal rotating charged solution with one angular momentum

The  $\mathcal{N} = 4$  seven-dimensional gauged supergravity theory is a consistent reduction of eleven-dimensional supergravity on  $S^4$ . It is capable of supporting black holes with two independent electric charges, carried by gauge fields in the  $U(1) \times U(1)$  Abelian subgroup of the full  $SO(5)$  gauge group. After a further consistent truncation, in which all except the  $U(1) \times U(1)$  subgroup of gauge fields are set to zero, the fields in the final theory comprise the metric, two dilatons, two U(1) gauge fields and a 4-form field strength that satisfies an odd-dimensional self-duality equation. For the purpose of this Letter, we will consider the bosonic sector of the seven-dimensional gauged supergravity that consist of a graviton, two dilaton scalars, two Abelian gauge potentials and a 3-form potential, whose Lagrangian is given by [9]

$$\begin{aligned} \mathcal{L} = & R \star \mathbb{1} - \star d\varphi_1 \wedge d\varphi_1 - 5 \star d\varphi_2 \wedge d\varphi_2 \\ & - \frac{1}{2} X_1^{-2} \star F_1 \wedge F_1 - \frac{1}{2} X_2^{-2} \star F_2 \wedge F_2 - \frac{1}{2} (X_1 X_2)^2 \star \mathcal{F} \wedge \mathcal{F} \\ & + (F_1 \wedge F_2 - g \mathcal{F}) \wedge C + 2g^2 [8X_1 X_2 \\ & + 4X_1^{-1} X_2^{-2} + 4X_1^{-2} X_2^{-1} - (X_1 X_2)^{-4}] \star \mathbb{1}, \end{aligned} \quad (1)$$

where

$$\begin{aligned} F_1 = dA_1, \quad F_2 = dA_2, \quad \mathcal{F} = dC, \\ X_1 = e^{-\varphi_1 - \varphi_2}, \quad X_2 = e^{\varphi_1 - \varphi_2}, \end{aligned} \quad (2)$$

together with a first-order odd-dimensional self-duality equation

$$(X_1 X_2)^2 \star \mathcal{F} = -2gC - \mathcal{H}, \quad (3)$$

satisfied by the 4-form field strength, which is conveniently stated by introducing an additional 2-form potential  $\mathcal{B}$

$$\mathcal{H} = d\mathcal{B} - (A_1 \wedge F_2 + A_2 \wedge F_1)/2. \quad (4)$$

Now we present the exact solution for non-extremal charged rotating black holes in the above theory, in the case with only one rotation parameter and with two independent charges. In terms of the generalized Boyer–Lindquist coordinates, the metric is written in a generalized form of the ansatz given in a previous work [2], which sheds light on how to find the most general non-extremal two-charged rotating black hole with three unequal rotation parameters. The metric and two U(1) Abelian gauge potentials have the following exquisite form

$$\begin{aligned} ds^2 = & (H_1 H_2)^{1/5} \left[ -\frac{(1 + g^2 r^2) \Delta_\theta}{\chi} dt^2 + \frac{\Sigma}{\Delta_r} dr^2 + \frac{\Sigma}{\Delta_\theta} d\theta^2 \right. \\ & + \frac{(r^2 + a^2) \sin^2 \theta}{\chi} d\phi^2 \\ & + r^2 \cos^2 \theta (d\psi^2 + \cos^2 \psi d\zeta^2 + \sin^2 \psi d\xi^2) \\ & \left. + \frac{2ms_1^2}{r^2 \Sigma H_1 \chi^2 (s_1^2 - s_2^2)} k_1^2 + \frac{2ms_2^2}{r^2 \Sigma H_2 \chi^2 (s_2^2 - s_1^2)} k_2^2 \right], \end{aligned} \quad (5)$$

$$A_i = \frac{2ms_i}{r^2 \Sigma H_i \chi} k_i, \quad (6)$$

in which

$$\begin{aligned} k_1 = & c_1 \sqrt{\Xi_2} \Delta_\theta dt - c_2 \sqrt{\Xi_1} a \sin^2 \theta d\phi, \\ k_2 = & c_2 \sqrt{\Xi_1} \Delta_\theta dt - c_1 \sqrt{\Xi_2} a \sin^2 \theta d\phi, \end{aligned} \quad (7)$$

and

$$\begin{aligned} \Delta_r = & (r^2 + a^2 - 2m/r^2)(1 + g^2 r^2 - 2mg^2 s_1^2 s_2^2 / r^2) + 2mg^2 c_1^2 c_2^2, \\ \Delta_\theta = & 1 - g^2 a^2 \cos^2 \theta, \quad \Sigma = r^2 + a^2 \cos^2 \theta, \\ H_i = & 1 + 2ms_i^2 / (r^2 \Sigma), \quad \Xi_i = c_i^2 - s_i^2 \chi, \quad \chi = 1 - g^2 a^2, \end{aligned}$$

where the short notations  $c_i = \cosh \delta_i$  and  $s_i = \sinh \delta_i$  ( $i = 1, 2$ ) are used.

Two scalars are given by  $X_i = (H_1 H_2)^{2/5} / H_i$ , while the non-vanishing components of the 2-form potential and 3-form potential are

$$\mathcal{B}_{t\phi} = \frac{ms_1 s_2 \Delta_\theta a \sin^2 \theta}{r^2 \Sigma \chi} \left( \frac{1}{H_1} + \frac{1}{H_2} \right), \quad (8)$$

$$\begin{aligned} \mathcal{C}_{t\theta\phi} = & g \frac{2ms_1 s_2 a \sin \theta \cos \theta}{r^2 \chi}, \\ \mathcal{C}_{\psi\zeta\xi} = & \frac{2ms_1 s_2 a \cos^4 \theta}{\Sigma} \sin \psi \cos \psi. \end{aligned} \quad (9)$$

We have found this solution by firstly recasting the metric and two gauge fields into a generalized ansatz in which two vectors  $k_1$  and  $k_2$  can be easily written down. This solution ansatz is inspired from our observation that the general two-charged rotating solutions [11] in all dimensions in ungauged supergravity and a special two-charged rotating AdS<sub>7</sub> gauged supergravity solution [9] with equal rotation parameters can be recast into a similar form, which are respectively rewritten in Appendices A and B. Next, we can decide the radial function  $\Delta_r$  by requiring the metric determinant to be the expected expression. After doing this, we further find the

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