



Albedo and gain threshold of a diffusive Raman random laser[☆]

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ABSTRACT

The diffuse reflectance (albedo) and transmittance of a Raman random gain medium are derived from a diffusion equation with power dependent gain. The results show good agreement with the experimental data for barium nitrate powder. Both the Raman albedo A_R and Raman transmittance T_R diverge at a critical gain γ_c , interpreted as the threshold for diffusive Raman laser generation. The parametric dependence of the albedo and threshold gain on the scattering characteristics of the random medium is analysed and the feedback effect of Fresnel reflection at the gain boundaries evaluated. The addition of external mirrors, particularly at the pumped surface, significantly reduces the generation threshold.

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1. Introduction

A number of non-linear optical effects have been observed in random laser media via the enhanced interaction arising from multiple scattering and gain, namely second and higher harmonic generation [1–3], anti-Stokes random lasing [4], up-conversion lasing [5], stimulated Raman scattering [6] and surface plasmon enhanced Raman scattering [7] and random lasing [8]. Raman random lasing has been reported in SiC nanorods [9] and the Raman random laser threshold evaluated for a cloud of cold atoms [10], while the feasibility of Raman laser generation in powder media is supported by current developments in CW solid state Raman laser technology [11]. Raman gain has indeed been observed in optically pumped barium nitrate powder via the enhanced reflectance and transmission gain of a Raman probe beam [12]. Unlike conventional random lasers, which function by optical excitation via the absorption bands, Raman random laser media require no intrinsic absorption, but operate by non-linear conversion of the pump light. As such they are ideally lossless, any residual absorption arising from impurities and surface contamination, thereby enabling the pump flux to reach much greater depths than in optically pumped random lasers. Raman gain observed in mono-crystalline barium nitrate powder has been modelled as a radiative transfer process in a scattering medium with non-uniform gain using Monte Carlo methods, the gain profile being determined from the observed variation of pump intensity with optical depth [12]. The pump radiation penetrates to a depth ~ 2 mm, equivalent to ~ 20 scattering lengths in a layer of randomly packed cubic crystals ~ 0.2 – 0.3 mm in size. A linear analysis of the propagation of light in

powdered laser media has previously been made using the Kubelka–Munk two-flux equations with constant coefficients [13] and the dynamics of dye and powder random lasers modelled using time-dependent diffusion equations [14,15]. Diffusion analysis has also been applied to model two-photon absorption in a random medium [16] and the distribution of second harmonic light in porous GaP [2]. Here we apply diffusion theory to analyse Raman gain in a random medium, finding quantitative agreement with the experimental data for the diffuse reflectance and transmittance gain of barium nitrate powder [12]. Having validated the diffusion analysis, we apply it to determine the parametric dependence of the Raman albedo and Raman random laser threshold on the scattering characteristics of a random gain medium, with feedback provided by Fresnel and specular reflection of diffuse light at the gain boundaries [17,18].

2. Diffusion theory

In the original experiment, a laser pump beam and a Raman shifted probe beam were coincident on a sample of mono-crystalline barium nitrate powder, the interaction of the strong pump radiation diffusing into the sample with the diffuse Raman probe radiation providing Raman gain via non-linear conversion of the pump radiation [12]. The process is modelled here via coupled diffusion equations in a 1D planar geometry, with the spatial distribution of the Raman gain determined by the diffuse pump flux distribution.

The diffusion equation for the scalar pump flux φ_p is

$$\partial^2 \varphi_p + S_p(\tau) = \kappa^2 \varphi_p \quad (1)$$

where $\partial^2 \varphi_p = d^2 \varphi_p / d\tau^2$, $d\tau = \kappa_e dz$, κ_e is the extinction coefficient, z is the spatial coordinate, $S_p(\tau)$ the source function (attenuated pump beam) and the diffuse attenuation parameter κ is defined by

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$\kappa^2 = 3(1 - \varpi)(1 - \varpi g)$, where $\varpi = \kappa_s/\kappa_e$ is the particle scattering albedo, κ_s is the scattering coefficient, the extinction coefficient $\kappa_e = \kappa_s + \kappa_a$, κ_a is the absorption coefficient and g the scattering asymmetry [19]. The equation for the diffuse Raman radiation flux φ_R in the Raman gain medium is

$$\partial^2 \varphi_R + S_R(\tau) + B_R^2(\tau) \varphi_R = 0 \quad (2)$$

where $S_R(\tau)$ is the source function (attenuated Raman probe beam) and $B_R^2(\tau) \approx 3\gamma(\tau)(1 - \varpi g)$ for $\varpi \approx 1$ [20]; $\gamma(\tau) = \gamma_R(\tau)\lambda_s$ is the dimensionless Raman gain parameter, $\gamma_R(\tau)$ is the spatially varying Raman gain coefficient, the scattering length $\lambda_s = 1/\kappa_s$ and $\gamma_R(\tau) = \Gamma_R \varphi_p(\tau)$, where Γ_R is the intensity dependent Raman gain [12] and $\varphi_p(\tau)$ the pump flux distribution. Eqs. (1) and (2) are coupled diffusion equations describing Raman diffusion in the random gain medium. Setting $S_R(\tau) = 0$ in Eq. (2) yields the diffusive Raman laser threshold equation [21]

$$\partial^2 \varphi_R + B_R^2(\tau) \varphi_R = 0. \quad (3)$$

Eq. (1) can be solved analytically for a planar, normally incident pump beam, equivalent to an exponentially decaying source in the scattering medium [2], to yield the diffuse pump flux distribution

$$\varphi_p(\tau) = \varphi_0 [e^{-\kappa\tau} - \alpha e^{-\kappa(2\Lambda - \tau)} - \beta e^{-\tau}] \quad (4)$$

from which the spatially varying Raman gain profile $\gamma_R(\tau)$ is derived. The second term in Eq. (4) accounts for reflection of the diffuse flux at the rear boundary, where $\Lambda = L/\lambda_s$, L is the physical thickness of the random medium, λ_s is the scattering length and the coefficients α and β are determined from the boundary conditions. When applied to diffusion in the powder layer, the fluxes φ_p and φ_R are extrapolated to zero a distance τ_e (extrapolation distance) beyond the boundary, determined by the refractive index n ($\tau_e = 2.42$ for $n = 1.5$ [16,22]). For anisotropic scattering, τ_e is expressed in terms of the transport length $\lambda_{tr} = \lambda_s/(1 - \varpi g)$ [22]. For a perfectly reflecting boundary τ_e is infinite and the slope zero: $\partial\varphi|_{\tau=0} = 0$. A diffusing layer with one perfectly reflecting boundary is mathematically equivalent to a slab of twice the width, with identical boundaries and a scalar flux distribution $\varphi(\tau)$ symmetric about the mid-plane.

Eq. (2) is used to determine the diffuse Raman reflectance (Raman albedo) A_R and Raman transmittance T_R of the powder layer from the diffuse emission (radiance) at the boundaries: $J_R(0, \Lambda) = -D\partial\varphi_R|_{\tau=0}$, Λ (D is the diffusion coefficient), which can be expressed in terms of the scalar fluxes $\varphi_R(0, \Lambda)$ via the boundary conditions [23]

$$\tau_e \partial\varphi_R|_{\tau=0, \Lambda} = \pm \varphi_R(0, \Lambda) \quad (5)$$

The observed gains in Raman albedo and diffuse Raman transmittance [12] are found from the ratios of the boundary fluxes evaluated with and without the pump source i.e. with and without Raman gain, for a fixed Raman probe intensity, on applying Eq. (5)

$$G(A_R) = J_R(0, \gamma_R) / J_R(0, 0) = \varphi_R(0, \gamma_R) / \varphi_R(0, 0) \quad (6a)$$

and

$$G(T_R) = J_R(\Lambda, \gamma_R) / J_R(\Lambda, 0) = \varphi_R(\Lambda, \gamma_R) / \varphi_R(\Lambda, 0) \quad (6b)$$

3. Results

3.1. Raman albedo

Calculations were made for planar pump and Raman probe beams incident on barium nitrate powder sandwiched between glass plates,

for sample thicknesses in the range $L = 10\text{--}100 \lambda_s$, as described in [12]. Raman gains were obtained from the ratios of transmitted and reflected Raman fluxes with and without Raman gain (Eqs. (6a, 6b)). The contribution of the diffuse pump flux reflected at the rear boundary was included in the gain profile (Eq. (4)). For the barium nitrate powder samples used in the experiment, the inferred scattering parameters were $\lambda_s \approx 110 \mu\text{m}$ and $g \approx 0.7$; the Raman gain coefficient ranged from $\gamma_R = 0.5 \text{ cm}^{-1}$ to 2.2 cm^{-1} [12]. A small but positive enhancement of the Raman albedo of the powder at the lowest Raman gain sets a lower limit on the particle scattering albedo viz. $\varpi \geq 1 - \gamma_R \lambda_s \geq 0.995$. For high particle scattering albedoes, both pump and probe beams penetrate further into the diffusive medium, sampling relatively large gain volumes, the diffuse Raman radiation flux reaching its maximum value $\sim 10\text{--}20$ scattering lengths from the pumped surface. Thus quite modest Raman gain can result in significant amplification of the multiply scattered Raman radiation, as shown by the enhanced diffuse reflectance and transmittance observed for barium nitrate powder [12]. Calculations of the Raman albedo gain $G(A_R)$ and diffuse Raman transmission gain $G(T_R)$ vs. L generate profiles with closely similar characteristics to those observed (Fig. 1), except for the quasi-exponential rise observed for thin powder layers ($L \leq 2 \text{ mm}$). However, the value of the gain parameter γ_0 required to fit the data points is lower than the experimental value as a result of the one-dimensional nature of the analysis, which neglects lateral diffusion of scattered light within the finite gain volume [12].

Increasing the Raman gain by further increasing the incident pump intensity causes the diffusely reflected and transmitted fluxes to rise rapidly, the albedo gain $G(A_R)$ and transmittance gain $G(T_R)$ diverging as the Raman gain parameter γ approaches a critical value γ_c , interpreted as the threshold gain parameter γ_{th} for diffusive Raman laser generation. Fig. 2 shows plots of the albedo gain $G(A_R)$ vs. gain parameter γ_0 for several values of scattering asymmetry g . However, the gain ratio $G(T_R)/G(A_R)$ remains finite, reaching a limiting value when $\gamma = \gamma_{th}$.

3.2. Raman laser threshold

The Raman laser threshold condition (Eq. (3)) is satisfied for a specific value of the Raman gain parameter $\gamma_0 = \gamma_{th}$ given by the eigenvalue $B_0^2 \approx 3\gamma_0(1 - \varpi g)$ [21]. The dependence of γ_{th} on the depth of the powder layer and the boundary conditions e.g. reflecting boundaries, is found by numerical solution of Eq. (3), with the gain profile $\gamma(\tau)$ determined by the diffuse pump flux distribution $\varphi_p(\tau)$. For uniform gain $B_R^2 = B_0^2$ constant, $B_0 = \pi/(\Lambda + 2\tau_e)$ and $\gamma_0 \approx \pi^2/3(1 - \varpi g)(\Lambda + 2\tau_e)^2$ [21], where we have included the extrapolation distance τ_e at the boundaries [17,22,23].

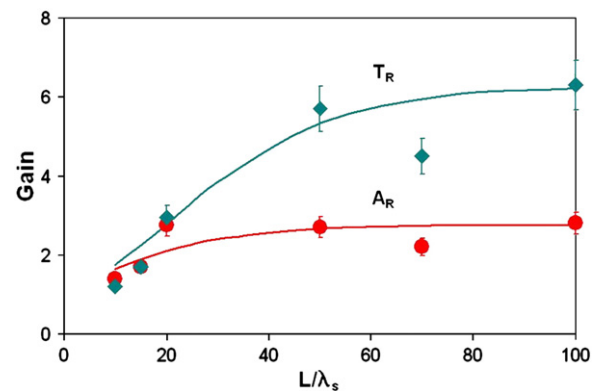


Fig. 1. Raman albedo A_R and Raman transmission gain T_R of barium nitrate powder vs. thickness L of the powder layer for $\varpi = 0.995$, $g = 0.7$. The theoretical curves are matched to the experimental data points $\bullet$, $\blacklozenge$ by adjusting the gain parameter γ_0 . The albedo saturates at smaller depths than the transmission gain, as observed.

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