



Natural inflation with hidden scale invariance



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ABSTRACT

We propose a new class of natural inflation models based on a hidden scale invariance. In a very generic Wilsonian effective field theory with an arbitrary number of scalar fields, which exhibits scale invariance via the dilaton, the potential necessarily contains a flat direction in the classical limit. This flat direction is lifted by small quantum corrections and inflation is realised without need for an unnatural fine-tuning. In the conformal limit, the effective potential becomes linear in the inflaton field, yielding to specific predictions for the spectral index and the tensor-to-scalar ratio, being respectively: $n_s - 1 \approx -0.025 \left(\frac{N_*}{60}\right)^{-1}$ and $r \approx 0.0667 \left(\frac{N_*}{60}\right)^{-1}$, where $N_* \approx 30\text{--}65$ is a number of efolds during observable inflation. This predictions are in reasonable agreement with cosmological measurements. Further improvement of the accuracy of these measurements may turn out to be critical in falsifying our scenario.

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1. Introduction

Cosmic inflation is an attractive paradigm for the very early universe that resolves some outstanding puzzles of the standard hot Big Bang cosmology, such as the horizon and flatness problems [1–3] (for important precursor works see also [4–6]). In addition, it provides a natural mechanism for generation of nearly scale-invariant inhomogeneities through the quantum fluctuations of the inflaton field, that at later stages result in the observed large scale structure of the universe [7]. Observations on Cosmic Microwave Background (CMB) radiation and the large scale structure provide a strong support for cosmic inflation.

The basic theory of inflation involves a scalar field, the inflaton (ϕ), which slowly rolls down the potential hill. In order to reproduce the CMB anisotropy measurements [8] and satisfy the requirement of sufficient inflation, the scale that defines the height of the inflaton potential must be many orders of magnitude smaller than the scale that defines its width, that is, the potential must be very flat. To maintain the hierarchy between these two different scales under the quantum corrections a precise adjustment of couplings is typically required. This is known as the fine-tuning problem of inflation.

Another potential source that may destabilise the delicate balance between the height and slope of the inflaton potential is higher order operators, which start to contribute significantly for large variations of the inflaton field during inflation. The effective field theory approximation, which favours $|\phi| \ll M_P$, breaks down in such cases and inflationary predictions become unreliable.

A class of natural inflation models has been suggested in [10] as a symmetry-motivated solution to the above fine-tuning problem. The inflaton in this class of models is a pseudo-Goldstone boson of some spontaneously broken anomalous global symmetry. The flatness of the pseudo-Goldstone potential is guaranteed by an approximate shift symmetry, although the underlying global symmetry may be the subject of large explicit breaking by non-renormalisable operators supposedly induced via quantum gravity. It seems, however, that the simplest models of natural inflation are now disfavoured at 95% CL [8].

In some earlier works [11,12] and more recently in [13,14] the scale invariance was advocated as a possible symmetry which is also capable of explaining the hierarchy of different scales without fine-tuning. A variety of specific scale-invariant inflationary models have been presented in recent years [15–25]. In [16] a universality class of models has been identified within the conformal supergravity framework [see also Ref. [18]]. The importance of the underlying scale invariance for natural inflation models has also been stressed in [20].

In this paper we would like to propose a new class of natural inflation models based on a hidden scale invariance, realised through the pseudo-Goldstone boson of a spontaneously broken

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anomalous scaling symmetry, the dilaton. Our key observation is that in a very generic scale-invariant model, with an arbitrary number of scalar fields and non-renormalisable operators in the scalar potential, there always exists a direction in field space which is absolutely flat in the classical limit. This flat direction is lifted upon quantum corrections being taken into account. Inflation proceeds along this direction, while other fields reside in their respective (meta)stable minima. As will be shown below, in the conformal coupling limit within the leading perturbative approximation, the generic model is reduced to a one-field model with a potential linear in the inflaton field, $V(\varphi) \sim \varphi$, with the linear term being radiatively induced. In this regime, the model predicts a characteristic relation between the spectral index n_s and the tensor-to-scalar ratio r :

$$n_s \approx 1 - \frac{3}{8}r \quad (1)$$

This relation is in a reasonable agreement with the currently available data [8,9]. Further improvement on the accuracy of n_s and/or r measurements may confirm or falsify our scenario.

2. Description of the model

Consider a Wilsonian effective field theory that describes the Standard Model, or its extension, coupled to gravity at an ultraviolet scale Λ :

$$S_\Lambda = \int d^4x \sqrt{-g} \left[\left(\frac{M_P^2}{2} + \sum_{i=1}^N \xi_i(\Lambda) \phi_i^2 \right) R - \frac{1}{2} \sum_{i=1}^N \partial_\mu \phi_i \partial^\mu \phi_i - V(\phi_i) + \dots \right], \quad (2)$$

where $M_P \approx 2.4 \cdot 10^{18}$ GeV and we use the mostly positive signature for the metric tensor. Here we have displayed only the scalar sector, which comprises of a set of N scalar fields $\{\phi_i\}$ ($i = 1, 2, \dots, N$) that includes the Standard Model Higgs boson. The scalar potential $V(\phi_i)$ is a generic polynomial of the scalar fields $\{\phi_i\}$ respecting the relevant symmetries of the theory:

$$V(\phi_i) = \sum_{\{i_n\}} \lambda_{i_1, \dots, i_n}(\Lambda) \phi_{i_1} \dots \phi_{i_n}. \quad (3)$$

where $\lambda_{i_1, \dots, i_n}(\Lambda)$ is a coupling of mass dimension $(4-n)$ defined at the Wilsonian cut-off Λ , while $\xi_i(\Lambda)$ is a dimensionless non-minimal coupling of the scalar field ϕ_i to gravity. The scale invariance is explicitly broken in (2) by the ultraviolet cut-off Λ , the Einstein–Hilbert term $\sim M_P^2 R$ and dimensionful couplings σ_{i_1, \dots, i_n} ($n \neq 4$).

We suppose that the underlying theory exhibits a hidden (spontaneously broken) scale invariance, which in the effective low-energy theory is implemented in the (nonlinear) pseudo-Goldstone boson, the dilaton χ . A simple way to incorporate the dilaton field χ is to rescale the dimensionful parameters in (2) by the respective powers of χ/f , f being the dilaton “decay constant”. More specifically:

$$\Lambda \rightarrow \Lambda \frac{\chi}{f} \equiv \lambda \chi, \quad M_P^2 \rightarrow M_P^2 \left(\frac{\chi}{f} \right)^2 \equiv \xi \chi^2, \quad (4)$$

$$\lambda_{i_1, \dots, i_n}(\Lambda) \rightarrow \lambda_{i_1, \dots, i_n}(\Lambda \chi/f) \left(\frac{\chi}{f} \right)^{4-n} \equiv \sigma_{i_1, \dots, i_n}(\lambda \chi) \chi^{4-n} \quad (5)$$

Thus, instead of (2) we consider a new action:

$$S_{\lambda \chi} = \int d^4x \sqrt{-g} \left[\left(\xi \chi^2 + \sum_{i=1}^N \xi_i(\lambda \chi) \phi_i^2 \right) R - \frac{1}{2} \partial_\mu \chi \partial^\mu \chi - \frac{1}{2} \sum_{i=1}^N \partial_\mu \phi_i \partial^\mu \phi_i - V(\phi_i, \chi) + \dots \right],$$

$$V(\phi_i, \chi) = \sum_{\{i_n\}} \sigma_{i_1, \dots, i_n}(\lambda \chi) \chi^{(4-n)} \phi_{i_1} \dots \phi_{i_n}. \quad (6)$$

This action is manifestly scale invariant in the classical limit, the scale invariance being broken at the quantum level through the renormalisation group (RG) running of the couplings, i.e., $\frac{\partial \sigma_{i_1, \dots, i_n}}{\partial \chi} \neq 0$, etc.

It is convenient to use a ‘hyperspherical’ representation for the set of scalar fields $\{\phi_i, \chi\}$:

$$\begin{aligned} \phi_i &= \rho \cos(\theta_i) \prod_{k=1}^{i-1} \sin(\theta_k), \quad (i = 1, 2, \dots, N) \\ \chi &= \rho \prod_{k=1}^N \sin(\theta_k). \end{aligned} \quad (7)$$

Expressing the action (6) through the fields in the above representation, we observe that the modulus field ρ factors out. That is, the first term in the action and the scalar potential presented in Eq. (6) can be written as $\sim \rho^2 \zeta(\theta_i) R$ and $\sim \rho^4 U(\theta_i)$, respectively, in which

$$\zeta(\theta_i) = \xi(\lambda \chi) \prod_{k=1}^N \sin^2(\theta_k) + \sum_{i=1}^N \xi_i(\lambda \chi) \cos^2(\theta_i) \prod_{k=1}^{i-1} \sin^2(\theta_k), \quad (8)$$

$$\begin{aligned} U(\theta_i) &= \prod_{k=1}^N \sin^{4-n}(\theta_k) \sum_{\{i_n\}} \sigma_{i_1, \dots, i_n}(\lambda \chi) \cos(\theta_{i_1}) \\ &\quad \times \prod_{k=1}^{i_1-1} \sin(\theta_k) \dots \cos(\theta_{i_n}) \prod_{k=1}^{i_n-1} \sin(\theta_k). \end{aligned} \quad (9)$$

We further assume that θ_i fields are relaxed in their stable or sufficiently long-lived (with lifetime longer than the duration of the observable inflation) minima $\langle \theta_i \rangle = \theta_i^c$ at very early stages in the evolution of the universe. Hence, their dynamics is of no interest to us in what follows and, instead of the full action (6), we consider the following reduced one:

$$\bar{S}_\rho = \int d^4x \sqrt{-g} \left[\zeta(\rho) \rho^2 R - \frac{1}{2} \partial_\mu \rho \partial^\mu \rho - V(\rho) \right], \quad (10)$$

$$V(\rho) = \sigma(\rho) \rho^4, \quad (11)$$

where $\zeta \equiv \zeta(\theta_i^c)$ and $\sigma \equiv U(\theta_i^c)$. Hence, we arrive at an effective single-field model with a quartic potential and non-minimal coupling [26], but without the standard Einstein–Hilbert term. It resembles also the large field limit of the Higgs inflation model [27].

In order to reproduce the Einstein–Hilbert term in (10) the modulus field ρ has to develop non-zero vacuum expectation value, $\langle \rho \rangle \equiv \rho_0$. If the vacuum configuration $\{\rho_0, \theta_i^c\}$ describes the current vacuum state of the universe, then $\rho_0 = \frac{M_P}{\sqrt{2\zeta(\rho_0)}}$ with $\zeta(\rho_0) \equiv \zeta_0 > 0$. Furthermore, the vacuum energy density, $\frac{\sigma(\rho_0) M_P^4}{4\zeta_0^2}$, in this case must be vanishingly small to satisfy the observations. That is, the scalar potential must be tuned so that $\sigma(\rho_0) \equiv \sigma_0 \sim$

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