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On the microscopic theory of the exciton ring fragmentation

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Abstract

The description is presented for the dependence of the indirect exciton condensate density at the ring as a function of the polar angle at zero temperature with the involvement of the processes of formation and recombination of the excitons. In particular, starting from the quasi one-dimensional Gross–Pitaevskii equation with a spatially uniform generating term, we derive an exact analytical solution yielding the fragmentation of an exciton ring which is probably observed in the experiments.

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1. Introduction

In the recent experiments of the Butov's group [1,2] the macroscopically ordered coherent state (MOCS) of the indirect exciton system has been observed in the coupled quantum wells. The state represents a periodic fragmentation of the ring formed in the intersection domain of the surplus densities of electrons in one well and photoexcited holes in another [3–5]. The fragmentation is observed below some critical temperature $(T_c \sim 1 \text{ K})$ and within a certain range of the laser pumping power when the density n of indirect excitons (IEs) at the ring is sufficiently large and the excitons are well defined $(n \sim 10^9 \text{ cm}^{-2})$, an average spacing between IEs at the ring is $\bar{a}_{\text{ex}-\text{ex}} \sim n^{-1/2} \sim 0.1 \,\mu\text{m}$, the IE Bohr radius is $a_{\text{B}} \sim 10^{-2} \,\mu\text{m}$, $\bar{a}_{\rm ex-ex}/a_{\rm B} \sim 10$). The typical parameters of the fragmented ring are as follows [2]: average ring radius is $R \sim 10^2$ µm, the ring width is $\Delta R \sim 10 \ \mu m$, the average radius of a fragment is $r_{\rm fr} \approx \Delta R/2$, and a number of fragments on the ring is $N_{\rm fr} \approx 50$. The evidence for the MOCS coherence results from a clear interference pattern of the IE recombination radiation from one of the ring fragments [6].

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At present, there exist two different phenomenological theories of the MOCS formation. The first theory [7] is based on the assumption that the IE system represents a degenerate twodimensional quasi-ideal Bose gas and the rate of aggregating an electron and a hole to form an indirect exciton is proportional to the factor $(1 + N_0)$, where N_0 is the number of the IEs in the zero momentum state. Under definite conditions this leads to the instability against fluctuations of the IE ring density. However, the theory seems to be intrinsically inconsistent since, on the one hand, the dipole–dipole interaction between the excitons is neglected, what is allowable only in the low density limit, and, on the other hand, the exciton condensate density should be sufficiently large so that the contribution from the stimulated processes would be essential.

The second theory [8] is based on that the total contribution of the repulsive dipole–dipole and attractive van der Waals interactions becomes attractive at the distances smaller than several IE radii. According to this theory, the ring fragmentation is due to formation of the islands of electron–hole liquid and is not associated with the Bose–Einstein condensation of the IEs. (We also mention paper [9] in which the IE energy distribution is suggested to be the Boltzmann one and, along with an attractive pair potential, the repulsive three-body interaction between IEs is considered. At the same time the nature of the latter is not explained.) However, the results of the experiment [10] unambiguously evidence for the repulsive character of the IE interaction. This is consistent with the idea that just this interaction results in a rapid IE thermalization (along with the nonconservation of a transverse momentum) and in the screening of the surface defects in the quantum wells plane. Note that any extension beyond the dipole approximation while considering the interaction between the IEs is equivalent to the deviation from the Bose statistics, which should self-consistently be taken into account.

As is seen from the pictures of the spatial distribution of the IE luminescence (see [1,2]), there exist two different spatial periods on the fragmented ring, namely, the size of a fragment and the size of a dark region separating adjacent fragments. Therefore, it is clear that the density as a function of the polar angle should be expressed via a periodic function with nonsymmetric half-periods, i.e., an elliptic function. So, if $\rho(\phi)$ is an elliptic function, it satisfies equation $(\rho'_{\phi})^2 = P_4(\rho)$, where $P_4(\rho)$ is a quartic polynomial in ρ . To the same form one can reduce the one-dimensional stationary Gross-Pitaevskii equation without an external potential, which, as is well known, describes a condensate of Bose particles. Hence, the idea arises that the ring fragmentation can be explained assuming that under experimental conditions an IE condensate exists on the ring. In addition, the formation and recombination of excitons on the ring can be taken into account by their interaction with some scalar generating, or "source-drain", field independent of coordinates. Formally, this is similar to the contribution from the dipole interaction of atoms with the electromagnetic field. If the number of the IEs on the ring does not vary in time, a concept of energy of the system is meaningful and one can find the stationary states of the condensate as well as the corresponding density spatial distributions.

In this Letter, we suggest the simplest microscopic theory of the MOCS based on the thing that the presence of BEC in the IE system (in spite of the BEC depletion due to repulsive exciton– exciton interaction) as well as the influence of the processes of IE formation and recombination on the ring result in the realization of a stationary excited state of the condensate, which is not spatially uniform. The indirect excitons are treated as genuine Bose particles. In addition, we suppose that the radial profile of the condensate density is governed by the processes which have no direct relation to the ring fragmentation. This allows us to consider a quasi one-dimensional problem.

2. Polar angle dependence of the condensate density

The Hamiltonian for the exciton system with the source reads

$$\begin{aligned} \hat{H} &= \hat{H}_J + \int d\vec{r} \,\hat{\Psi}^+(\vec{r},t) \frac{\hat{p}^2}{2m} \hat{\Psi}(\vec{r},t) \\ &+ \frac{1}{2} \int d\vec{r} \, d\vec{r}' \,\hat{\Psi}^+(\vec{r},t) \hat{\Psi}^+(\vec{r}',t) U(\vec{r}-\vec{r}') \hat{\Psi}(\vec{r}',t) \hat{\Psi}(\vec{r},t). \end{aligned}$$
(1)

Here $\hat{\Psi}(\vec{r},t)$ is a Bose field operator obeying the commutation relations $[\hat{\Psi}(\vec{r}_1,t),\hat{\Psi}^+(\vec{r}_2,t)] = \delta(\vec{r}_1 - \vec{r}_2), \quad [\hat{\Psi},\hat{\Psi}] = [\hat{\Psi}^+,\hat{\Psi}^+] = 0$. For simplicity, we suggest that the repulsive pair interaction is local, i.e., $U(\vec{r}) = \lambda \delta(\vec{r})$ and $\lambda > 0$. In fact, this means either the Born approximation for the potential U(r)with $\lambda = \int U(r) d\vec{r}$, or the gas approximation $na_{2D}^2 \ll 1$, where *n* is the two-dimensional IE density and $a_{2D} = m\lambda/(4\pi\hbar^2)$ is an exact *s*-scattering length [11]. The contribution of the source is given by

$$\hat{H}_{J} = \int d\vec{r} \left(J(t)\hat{\Psi}^{+}(\vec{r},t) + J^{*}(t)\hat{\Psi}(\vec{r},t) \right),$$
(2)

where $J(t) = |J|e^{i\alpha(t)}$. It is natural to assume that the time dependence of the source is the same as for the wave function of the ground condensate state in the lack of the source, $\alpha(t) = -\mu t$. We suggest that the quantities |J| and μ are time-independent.

Let us consider the equation of motion for $\hat{\Psi}$ -operator, $i\hbar\partial\hat{\Psi}(\vec{r},t)/\partial t = [\hat{\Psi}(\vec{r},t),\hat{H}]$, assuming zero temperature of the system. Here, the most fraction of excitons is in the Bosecondensate state and thus we neglect noncondensate particles. Then $\hat{\Psi}$ -operator becomes the *c*-number and obeys the equation

$$i\hbar\dot{\Psi} = -\frac{\hbar^2}{2m}\nabla^2\Psi + \lambda|\Psi|^2\Psi + J,$$
(3)

which for J = 0 turns into the Gross–Pitaevskii equation. Supposing that the radial profile of the condensate density is unvaried, we consider a quasi 1D problem. Then, the genuine density "in amplitude" refers to the result obtained as $n_{\text{true}}/n \sim \bar{a}_{\text{ex}-\text{ex}}/\Delta R \sim 10^{-2}$. For the polar frame with the origin at the ring center $\nabla^2 \approx R^{-2}\partial^2/\partial\phi^2$, $d\vec{r} \approx 2\pi R\Delta R d\phi = S d\phi$, where ϕ is the polar angle, R is the ring radius, and $R \neq R(n)$. The aim of the work is to find a qualitative behavior $n(\phi)$ at various magnitudes of the parameters.

If one measures energy in units $E_R = \hbar^2/(2mR^2)$, time in $\tau_R = \hbar/E_R$, and density in S^{-1} , the constants in Eq. (3) are dimensionless

$$i\dot{\Psi} = -\Psi_{\phi\phi}^{\prime\prime} + \lambda |\Psi|^2 \Psi + J.$$
(4)

Let us seek for the solution (4) as $\Psi = \rho e^{if}$, where $\rho^2 \approx n$ and *f* are the density and phase of the condensate, respectively. Then, for the real and imaginary parts of Ψ the following equations are valid

$$\rho \dot{f} + \rho (f_{\phi}')^2 - \rho_{\phi\phi}'' + \lambda \rho^3 + |J| \cos(\alpha - f) = 0,$$
 (5)

$$\dot{\rho} + 2\rho'_{\phi}f'_{\phi} + \rho f''_{\phi\phi} - |J|\sin(\alpha - f) = 0.$$
(6)

Multiplying both sides of Eq. (6) by 2ρ and integrating over ϕ , we obtain that the rate of variation of the particle number N equals

$$\dot{N} = \int d\vec{r} \, 2\rho \dot{\rho} = \int d\vec{r} \, 2\rho |J| \sin(\alpha - f). \tag{7}$$

In what follows, we are interested in the stationary currentless states alone: $\dot{N} = 0$, $f'_{\phi} = 0$. Then $f = \alpha + \pi l$, *l* is an integer. So,

$$\rho_{\phi\phi}^{\prime\prime} + \mu\rho - \lambda\rho^3 - |J|(-1)^l = 0, \tag{8}$$

in which $\alpha(t) = -\mu t$ is taken into account. In the case of the homogeneous density $(\rho'_{\phi} \equiv 0, \rho = \rho_0)$ and $|J| = 0, \mu$ has a

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