



A proposed experiment on ball lightning model

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ABSTRACT

We propose an experiment for strong light amplification at multiple total reflections from active gaseous media.

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1. Introduction

Light reflection from an interface between two media is determined by the wave equation and the boundary conditions, which follow from Maxwell's equations. The wave equations for electric, \mathbf{E} and magnetic, \mathbf{H} , fields in a homogeneous medium with constant μ and ϵ are

$$\Delta \mathbf{E}(\mathbf{r}, t) = \frac{\mu\epsilon}{c^2} \frac{\partial^2 \mathbf{E}(\mathbf{r}, t)}{\partial t^2}, \quad \Delta \mathbf{H}(\mathbf{r}, t) = \frac{\mu\epsilon}{c^2} \frac{\partial^2 \mathbf{H}(\mathbf{r}, t)}{\partial t^2}. \quad (1)$$

Both equations have plane wave solutions

$$\mathbf{E}(\mathbf{r}, t) = \mathbf{E} \exp(i\mathbf{k} \cdot \mathbf{r} - i\omega t), \quad \mathbf{H}(\mathbf{r}, t) = \mathbf{H} \exp(i\mathbf{k} \cdot \mathbf{r} - i\omega t), \quad (2)$$

where $k^2 = \epsilon\mu k_0^2$, $k_0 = \omega/c$ and c is the speed of light in vacuum. The fields \mathbf{E} and \mathbf{H} are not independent. They are related to each other by equations

$$\mathbf{H} = \frac{c}{\mu\omega} [\mathbf{k} \times \mathbf{E}], \quad \mathbf{E} = -\frac{c}{\epsilon\omega} [\mathbf{k} \times \mathbf{H}], \quad (3)$$

and, if $|\mathbf{E}| = 1$, the length of \mathbf{H} is $|\mathbf{H}| = \sqrt{\epsilon/\mu} = 1/Z$, where $Z = \sqrt{\mu/\epsilon}$ is called the medium impedance.

If space consists of two halves with different $\epsilon_{1,2}$ and $\mu_{1,2}$, the wave equations in them (1) are different, and their solutions should be matched at the interface. The matching conditions follow from the Maxwell equations. They require continuity

of the components $\mathbf{E}_{\parallel}(\mathbf{r}, t)$, $\mathbf{H}_{\parallel}(\mathbf{r}, t)$ parallel to the interface, and $\epsilon(\mathbf{n} \cdot \mathbf{E}(\mathbf{r}, t))$, $\mu(\mathbf{n} \cdot \mathbf{H}(\mathbf{r}, t))$, perpendicular to it, where \mathbf{n} is a unit normal vector. The wave function in presence of the interface is

$$\begin{aligned} \psi(\mathbf{r}, t) = & \Theta(z < 0) (e^{i\mathbf{k}_1 \cdot \mathbf{r} - i\omega t} \psi_1 + e^{i\mathbf{k}_r \cdot \mathbf{r} - i\omega t} \psi_r \rho) \\ & + \Theta(z > 0) e^{i\mathbf{k}_2 \cdot \mathbf{r} - i\omega t} \psi_2 \tau, \end{aligned} \quad (4)$$

where the term $\exp(i\mathbf{k}_1 \cdot \mathbf{r} - i\omega t) \psi_1$ with the wave vector \mathbf{k}_1 describes the plane wave incident on the interface from medium 1, factors $\psi_i = \mathbf{E}_i + \mathbf{H}_i$ ($i = 1, r, 2$) denote sum of electric and magnetic polarization vectors, $\mathbf{k}_{r,2}$ are wave vectors of the reflected and transmitted waves, ρ , τ are the reflection and transmission amplitudes respectively, and $\Theta(z)$ is the step function, which is equal to unity when inequality in its argument is satisfied, and to zero otherwise.

The wave vectors $\mathbf{k}_{r,2}$ are completely determined by \mathbf{k}_1 . They are determined uniquely by the constants ϵ_i , μ_i , and by the fact that $k_0 = \omega/c$ and the part \mathbf{k}_{\parallel} of the wave vectors parallel the interface must be identical for all the waves. In the following we assume that the medium 1 is lossless, i.e. $\epsilon_1 \mu_1$ is real, therefore all the components of \mathbf{k}_1 are also real.

The normal component $k_{2\perp}$ of the refracted wave is

$$k_{2\perp} = \sqrt{\epsilon_2 \mu_2 k_0^2 - \mathbf{k}_{\parallel}^2} = \sqrt{k_{1\perp}^2 - (\epsilon_1 \mu_1 - \epsilon_2 \mu_2) k_0^2}, \quad (5)$$

or it can be represented as

$$k_{2\perp} = \sqrt{\epsilon k_1^2 - \mathbf{k}_{\parallel}^2} = \sqrt{n^2 k_1^2 - \mathbf{k}_{\parallel}^2}, \quad (6)$$

where $n = \sqrt{\epsilon}$ is the refractive index, and we introduced relative permittivity $\epsilon = \epsilon_2 \mu_2 / \epsilon_1 \mu_1$.

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The amplitudes ρ and τ are well known from textbooks (see [1], for example). They are calculated differently for TE-wave, when the incident electric field is polarized perpendicularly to the plane of incidence, i.e. parallel to the interface (it is usually denoted as E_s), and for TH-field, when the incident electric field is polarized inside the plane of incidence (it is usually denoted as E_p). For both of these cases we have well-known Fresnel formulas

$$\rho_s = \frac{\mu_2 k_{1\perp} - \mu_1 k_{2\perp}}{\mu_2 k_{1\perp} + \mu_1 k_{2\perp}}, \quad \rho_p = \frac{\epsilon_2 k_{1\perp} - \epsilon_1 k_{2\perp}}{\epsilon_2 k_{1\perp} + \epsilon_1 k_{2\perp}}, \quad (7)$$

and $\tau_{s,p} = 1 + \rho_{s,p}$. In the following we for simplicity assume that $\mu_2 = \mu_1 = 1$, so $\mu_{1,2}$ are excluded from all our formulas.

From (6) it follows that for lossless media when $0 < \epsilon < 1$ is real, the incident wave, for which k_{\parallel} is within $nk_1 \leq |k_{\parallel}| \leq k_1$, is totally reflected from the interface. This happens because

$$k_{2\perp} = iK'_{2\perp} \equiv i\sqrt{k_{\parallel}^2 - \epsilon k_1^2}, \quad (8)$$

thus the factor $\exp(ik_{2\perp}z) = \exp(-K'_{2\perp}z)$ of the wave $\exp(i\mathbf{k}_2\mathbf{r})$ exponentially decays, i.e. the refracted wave becomes an evanescent one. Therefore, the energy does not flow inside the medium 2, and due to the energy conservation it must be totally reflected into medium 1.

If the medium 2 is lossy or gainy, the constant ϵ is a complex quantity $\epsilon = \epsilon' \pm i\epsilon''$, with positive ϵ' and ϵ'' . In this case outside the total internal reflection (TIR) region ($|k_{\parallel}|^2 \ll \epsilon'k_1^2$) we have $k_{2\perp} = k'_{2\perp} \pm iK'_{2\perp}$, where for small ϵ'' ($\epsilon''k_1^2 \ll \epsilon'k_1^2 - |k_{\parallel}|^2$)

$$k'_{2\perp} \approx \sqrt{\epsilon'k_1^2 - |k_{\parallel}|^2}, \quad K'_{2\perp} \approx \epsilon'' \frac{k_1^2}{2k'_{2\perp}}. \quad (9)$$

In the TIR regime, $k'_{2\perp}$ in Eq. (9) transforms into $iK'_{2\perp}$, where $K'_{2\perp} \approx \sqrt{|k_{\parallel}|^2 - \epsilon'k_1^2}$, and $K'_{2\perp}$ transforms to

$$K'_{2\perp} \rightarrow -iK'_{2\perp} = \epsilon'' \frac{k_1^2}{2iK'_{2\perp}}. \quad (10)$$

Therefore, at TIR $k_{2\perp} = \pm K'_{2\perp} + iK'_{2\perp}$, where

$$K'_{2\perp} = \epsilon'' \frac{k_1^2}{2K'_{2\perp}}, \quad K'_{2\perp} \approx \sqrt{|k_{\parallel}|^2 - \epsilon'k_1^2}. \quad (11)$$

The '+' sign before imaginary part $iK'_{2\perp}$ determines exponential decay of the refracted wave away from the interface for both lossy and gainy media cases. However the real part, $K'_{2\perp}$ has opposite signs for lossy and gainy cases.

The reflection amplitudes (7) at TIR look

$$\rho_s = \frac{k_{1\perp} - iK'_{2\perp} \mp K'_{2\perp}}{k_{1\perp} + iK'_{2\perp} \pm K'_{2\perp}}, \quad (12)$$

$$\rho_p = \frac{\epsilon_2 k_{1\perp} - \epsilon_1 (iK'_{2\perp} \pm K'_{2\perp})}{\epsilon_2 k_{1\perp} + \epsilon_1 (iK'_{2\perp} \mp K'_{2\perp})}. \quad (13)$$

The positive value of $K'_{2\perp}$ for lossy medium means that the reflection coefficient in TIR is less than one, because part of the energy flux proportional to $K'_{2\perp}$ enters the medium 2 and is absorbed there. The negative value of $K'_{2\perp}$ for gainy medium means that the reflection coefficient in TIR is larger than one, because part of the energy flux proportional to $K'_{2\perp}$, exits the medium 2 and adds to the TIR wave.

In [2] it was incorrectly claimed (see, for example, critics in [3]) that in the case of TIR from a gainy medium the wave vector inside the gainy medium has opposite sign: $k_{2\perp} = K'_{2\perp} - iK'_{2\perp}$, and the reflection coefficient at TIR $|\rho_{s,p}|^2$ is less than unity. If it were so, then the wave function inside the gainy medium would increase proportionally to $\exp(K'_{2\perp}z)$ independently of how small is

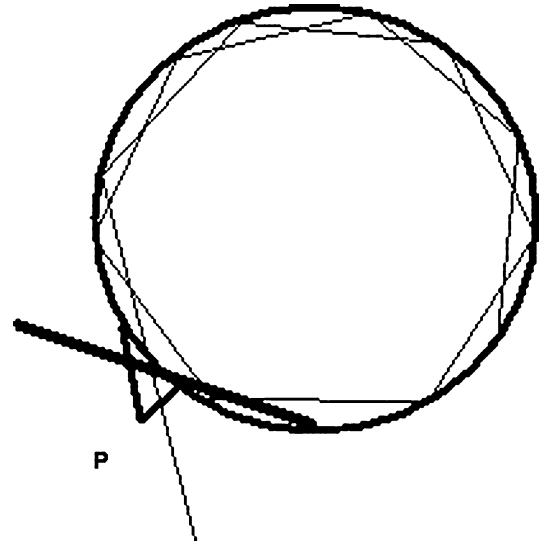


Fig. 1. Schematic of the experiment for multiple TIR off gainy medium.

the gain. Since $K'_{2\perp} \sim 1/\lambda$ (see (11)) then for $\lambda \sim 1000$ nm the intensity of the field inside the gainy medium at a distance 1 mm from the interface would be larger than intensity of the incident wave of light by the factor $e^{2000} \approx 10^{860}$, which surpasses all the astronomical numbers. It proves that the claim in [2] cannot be true.

With the correct sign $k_{2\perp} = -K'_{2\perp} + iK'_{2\perp}$ the reflection coefficient at TIR from a gainy medium is larger than one, and it increases with the gain. The photons induced by the incident wave cannot propagate inside the gainy medium by the same reason as the incident one. They can only go by the tunnelling transmission into the first medium. The increase in the reflected flux is due to the sub-barrier induction of the photon, which tunnels from the gainy medium into medium 1 and coherently adds to the reflected primary photon. The larger is the gain, the larger is the probability of such a process.

2. The proposed experiment for strong enhancement of the light trapped in a glass sphere

The increase of the reflection coefficient at TIR from a gainy medium can be used to develop a curious experiment for storage and amplification of light. Imagine a glass sphere with a coupler P , as shown in Fig. 1. The sphere has thin walls (it is also possible to use a homogeneous glass sphere) and is surrounded by an excited gas (or other active media). The ray of light, shown by the thin line, enters the glass walls through the coupler and then undergoes TIR multiple times. At every reflection the light is amplified according to the analysis in the previous section. It is possible to imagine a geometry in which the ray after entering the glass becomes trapped in it, or after sufficiently many reflections escapes the sphere, as shown by the thick line. The amplification depends on the number of the reflections and on the gain coefficient of the active medium. The number of the reflections is very sensitive to the angle of the incident ray. It is important to note, that the energy accumulates inside the sphere and does not go out of it. The total reflection works like a pump, and the pumped energy density can be much larger than the energy density in the surrounding gainy medium. If the overall amplification is sufficiently high, the glass will melt into a liquid bubble with thin skin filled with the light, similar to the ball lightning described in [4].

We can estimate the magnitude of the light enhancement in such a sphere. Assume that for the active medium $\epsilon_2 \approx 1 - i\alpha$, and

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