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Effects of correlations on honeycomb lattice in ionic-Hubbard model

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1. Introduction

Many mechanisms can open an energy gap in metallic or semimetallic state, such as: Mott-insulator transition or charge and spin density wave on nested Fermi surface [1]. In addition, competition between two interactions can close and suppress the energy gap [2]. For studying the opening and suppression of energy gap in spectrum of a honeycomb lattice, we started with a simple tight binding Hamiltonian, which the substrate can induce a symmetry breaking through an ionic potential of strength Δ and adding onsite repulsive interaction U [3].

The ground state of the honeycomb lattice when $\Delta \neq 0$, U = 0 is a band insulator on the strongly correlated limit [4,5]. This immediately leads to a band gap of magnitude 2Δ , with site occupancies $n_{lower \ band} = 2$, $n_{higher \ band} = 0$. This gap decreases with increasing U, and no-double occupancy constraint imposed by large U [6]. In opposite limit, i.e. $\Delta \ll U$ the system can be described in terms of an effective massive Dirac theory. The intermediate phase can be found between two insulator and massive Dirac fermions, which obeys massless Dirac theory. The first purpose of this paper is to tackle these questions: What would be the result of competition between U and Δ on occupancy of each sub-lattice in honeycomb lattice? Or what would be the effects of U and Δ on the energy gap? Another target of this paper is studying the effects of competition between U and Δ on renormalization of Fermi velocity.

ABSTRACT

In a honeycomb lattice the symmetry has been broken by adding an ionic potential and a singleparticle gap was generated in the spectrum. We have employed the iterative perturbation theory (IPT) in dynamical mean field approximation method to study the effects of competition between U and Δ on energy gap and renormalized Fermi velocity. As we found, the competition between the single-particle gap parameter and the Hubbard potential closed the energy gap and restored the semi-metallic phase, then the gap was opened again in Mott insulator phase. For a fixed Δ by increasing U, the renormalized Fermi velocity \tilde{v}_F is decreased, but change in Δ , for a fixed U, has no effects on \tilde{v}_F . The difference in filling factor is calculated for various numbers of U, Δ . The results of this study can be implicated for gapped graphene e.g. hydrogenated graphene.

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There is a widespread consensus on the large potential of graphene for electronic applications [7,8]. The low electronic density of states near the Fermi energy and zero band-gap at neutrality point in graphene exhibit a small ON/OFF switching ratio, due to this problem the application of graphene for charge based logic devices is inhibited [9]. It has been shown, that pure graphene exhibits weak anti-ferromagnetic properties at near room temperature [10]. The carbon-based systems such as graphene are the most attractive objects for hydrogen storage [11]. The hydrogen adsorption on graphene is an interesting idea for two reasons: first: a band gap is induced [12] and second: the hydrogenated graphene sheet is converted to a hydrogen storage device [13]. The results of this paper could be generalized to hydrogenated graphene.

In semi-metal-insulator transition (SMIT) unlike to metalinsulator transition (MIT), there is no Kondo resonance corresponding to quasi-particle at the Fermi level [14]. Therefore, SMIT can be described by renormalized Fermi velocity \tilde{v}_F instead of spectral weight of such resonant state. The Fermi velocity is an order parameter which is characterized by a Dirac liquid state [25]. We use dynamical mean field theory (DMFT) for probing the effects of U and Δ within paramagnetic phase in ionic-Hubbard model. The DMFT is exact in limit of infinite coordination numbers [15], but for lower dimensions the local self-energy (here it is *k*-independent) becomes only an approximate description [16]. Therefore the critical values of some parameters in DMFT approximation on honeycomb lattice maybe overestimated [17]. But we should note that the overall picture of output numerical results is expected to hold.

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The phase separation in 2D Hubbard model was studied with the dynamical cluster approximation (DCA) [18]. In the DMFT method the interactions in a lattice are mapped to an impurity problem which is embedded self-consistently in a host. Therefore the DMFT neglects spatial correlations, but in DCA we assume that correlations are short range. The original lattice is mapped to a periodic cluster of specific size, which is embedded in a selfconsistent host. Therefore the correlations in same range with the cluster size are considered accurately, while the other interactions with longer length than cluster are described at the mean-field approximation. In limit of $\Delta \rightarrow 0$, the ionic-Hubbard model and Hubbard model are similar, when we use DCA and DMFT in this limit $(\Delta \rightarrow 0)$, we found different results on the same model and same lattice. These differences are in magnitude of critical U_c and border of the phase regions, but the overall descriptions of phase diagram and phase separation are expected to hold. The metal-insulator transition has obtained by cluster DMFT (CDMFT), is different from that of the single-site DMFT. In CDMFT with cluster size larger than 2, the quasi-particle weight is *k*-dependent and nonzero, but in the single-site DMFT, the quasi-particle weight is *k*-independent and vanishes continuously at the MIT region [19]. In Ref. [20], the variational cluster approximation (VCA) is applied to calculate local electron correlations in bipartite square and honeycomb lattices in Hubbard model, they found, in honeycomb lattice electron density displayed smooth metal-insulator transition with continuous evolution. The square lattice experienced metal-insulator transition, but the electron density in square lattice displayed discontinuity with spontaneous transition [20]. The phase transition in the ionic-Hubbard model has been investigated in a two-dimensional square lattice by determinant quantum Monte Carlo (DQMC). The competition between staggered potential and on site potential lead to the phase transition from Mott insulator to metallic and band insulator [21].

The ionic-Hubbard (IH) model has been studied in 1-D and 2D [22]. The DMFT approximation has been employed to study of such model [23], this technique is implemented to study the phase transitions and phase diagrams of honeycomb lattice in IH model [6] and a square lattice was studied by determinant quantum Monte Carlo method [24]. The results can be related to physics of graphene and hydrogenated graphene for specific magnitude of Δ and U.

2. Model and method

The ionic-Hubbard model (IHM) on the honeycomb lattice is described by this Hamiltonian,

$$H = -t \sum_{i \in A, j \in B, \sigma} (c_{i\sigma}^{\mathsf{T}} c_{j\sigma} + \text{h.c.}) - \mu \sum_{i} n_{i}$$
$$+ \Delta \sum_{i \in A} n_{i} - \Delta \sum_{i \in B} n_{i} + U \sum_{j} n_{j\downarrow} n_{j\uparrow}, \qquad (1)$$

where *t* is the nearest neighbor hopping, Δ is a staggered onebody potential that alternates sign between site in sub-lattice *A* or *B* and *U* is the Hubbard repulsion. The chemical potential is $\mu = U/2$ at half-filling and so the average occupancy is $\frac{\langle n_A \rangle + \langle n_B \rangle}{2} =$ 1. This model represented a band insulator with energy gap 2Δ at non-interacting limit, U = 0. In opposite limit, $U \gg \Delta$, the system is in Mott insulator state. What's the intermediate phase? The semi-metallic character restored and massive Dirac fermions will become massless, as a result of increasing the Hubbard potential, *U*. It has been demonstrated that by DMFT method can describe and understand band insulator (BI)–semi-metal (SM)–Mott insulator (MI) transition [2]. The first step is introducing interaction Green's function in bipartite lattice,



Fig. 1. (Color online.) The density plot of the energy gap in U, Δ plate. The band insulator and Mott insulator are separated by semi-metal phase.

$$G(\vec{k},\omega^{+}) = \begin{pmatrix} \zeta_A(k,\omega^{+}) & -\epsilon(k) \\ -\epsilon(\vec{k}) & \zeta_B(\vec{k},\omega^{+}) \end{pmatrix}$$
(2)

where \overline{k} is the momentum vector in first Brillouin zone, $\epsilon(\overline{k})$ is the energy dispersion for the honeycomb lattice, and $\zeta_{A(B)} = \omega^+ \mp \Delta + \mu - \Sigma_{A(B)}(\omega^+)$, with $\omega^+ = \omega + i0^+$. The local Green's function corresponding to each sub-lattice can be written as,

$$G_{\alpha}(\omega^{+}) = \sum_{\vec{k}} G_{\alpha \ \alpha}(\vec{k}, \omega^{+})$$
$$= \zeta_{\tilde{\alpha}}(\omega^{+}) \int_{-\infty}^{\infty} d\epsilon \frac{\rho_{0}(\epsilon)}{\zeta_{A}(\omega^{+})\zeta_{B}(\omega^{+}) - \epsilon^{2}}$$
(3)

where $\alpha = A(B)$, $\bar{\alpha} = B(A)$ are corresponding to each sub-lattice, and $\rho_0(\epsilon)$ is the bare DOS of the honeycomb lattice (graphene). The details of calculations are done in previous work [6]. The DOS of an interaction system can be calculated by,

$$\rho_{\alpha}(\omega) = \Sigma_{\vec{k}} \Im \operatorname{Tr} \left[G_{\alpha}(\vec{k}, \omega^{+}) \right] / \pi.$$
(4)

According to particle-hole symmetry at half-filling in honeycomb lattice, we know $\rho_A(\omega) = \rho_B(-\omega)$. The total DOS eventually obtained via $\rho(\omega) = \rho_A(\omega) + \rho_B(\omega)$. The DOS is necessary for obtaining the energy gap for each pair of U, Δ . In computation of energy gap for each pair of U, Δ , the density of state is essential and slope of $\rho(\epsilon)$ near Dirac points determined renormalized Fermi velocity in SM phase [25].

3. Results and discussion

The filling factors of each sub-lattice, n_A , n_B and energy gap have been calculated by DMFT outputs. In Fig. 1, the density plot of the energy gap is plotted vs, U, Δ . In calculation of E_{gap} , the U, Δ have been changed in 0.1t steps, then for better resolution we used interpolation method to obtain continuous density plot. We can observe, the density plot of energy gap is in excellent agreement to Fig. 4 of Ref. [6]. The energy gap vanishes in the semi-metallic phase. In this phase diagram one can find graphene in $U/t \sim 3.0-4.0$ and $\Delta/t \sim 0.04-0.05$, where the system still remains in semi-metallic phase [26]. So the graphene can be SM, despite a symmetry breaking ionic potential of strength $\Delta \sim$ 110–150 meV ($t \sim$ 2.7 eV). The renormalization of the gap magnitude is not the only reason of the Hubbard correlations U. It also influences by other spectral features such as the lifetime of quasi-particles, e.g. in hydrogenated graphene [28]. In this DMFT approximation, results may have overestimated the upper

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