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## Column flotation simulation: A dynamic framework

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#### ABSTRACT

Since the introduction of column flotation in mineral processing plants in the early 1980s, modelling of this process has become a prevailing field of investigation. Even if significant progresses have been made with every new attempt, most of the proposed models or simulators have been restricted to the steady-state behaviour. When dynamic mass balance equations were considered, a constant pulp level during the simulation was always assumed. The objective of this paper is to present a framework for the fully dynamic simulation of column flotation. The emphasis is placed on the simulation of water, solids and gas flows and their effect on the pulp level and output flow rates.

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#### 1. Introduction

Since their introduction in mineral processing plants, flotation columns received considerable attention from academics and practitioners. Work related to modelling, especially for the mixing conditions and steady-state performance, led to a better understanding of design and operation issues. Some interesting advances have also been made on column flotation simulation. Although practical outcomes for the mineral processing community have yet not been as tangible, they are progressively emerging, for instance with the work of JKTech (Bouchard et al., 2009).

Pioneering efforts started in the eighties. Luttrell et al. (1987) proposed a static simulator based on a population mass balance (air bubbles, unattached solid particles, and bubble particle aggregates). Mass transport was considered in the model using fluid flows and particle buoyancy, while the bubble particle attachment rate was evaluated using first principles. Some processes, such as the bubble loading and mixing properties, were explained under pre-specified operating conditions, using a semi-fundamental approach requiring the calibration of two empirical coefficients. The simulator attempted to predict the recovery of a specific column flotation operation for design, control, optimisation and scale-up purposes.

During the same period, Sastry and Lofftus (1988) also developed a simulator using a similar approach, but considering the dynamic mass balance equations. The resulting tool opened the door to time-dependent investigations, and process control applications. The assumption of constant air and water holdups, along with the impossibility of analytically solving the general model, represented the greatest limitations of their work.

The addition of air and water mass balance equations to a fivewell-mixed zone reactor instead of the three-zone model of Sastry and Lofftus (1988) led to more flexibility for the simulator proposed by Pate and Herbst (1989). Their approach also replaced the axially dispersed plug flow model with a distributed volume mixers-in-series estimation for increasing computational efficiency. The air mass balance was however taken into account on a static basis following the assumption that air holdup is subject to very fast changes compared with the water volume. Particles could be of any size and were divided into three classes: free valuable mineral, free gangue and locked. Similarly to the above-mentioned simulators, the proposed model exhibited certain empirical features regarding the calibration of rate constants and the description of some phenomena using correlations (water entrainment, water drainage, etc.). Later on, the same team used this dynamic simulator to design a methodology for selecting a control strategy for a column flotation unit (Lee et al., 1991).

Cruz (1997) made a further step and proposed a fully dynamic simulator of column flotation metallurgical performance. Based on fundamental considerations, her work included a comprehensive description of complex phenomena, such as bubble coalescence in the froth and bubble loading, and considered particle and bubble size distributions as well as a particle composition distribution. The design was based on the application of a population

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Nomenclature			
Α	function	$U_{bs}$	terminal rising velocity of a single bubble
$A_c$	columnn cross section area	$U_g$	bubble rising velocity citep
α	air recovery	$U_{gs}$	gas/slurry relative velocity
β	distribution coefficient	$U_l$	liquid interstitial velocity
C	frother concentration	$U_p$	particle interstitial velocity
$C_c$	contamination factor	V	volume
$C_d$	drag coefficient	$v_{pump}$	tailings pump speed
$C_{pb}$	viscous drag coefficient within Plateau borders	$v_g$	vertical component of the froth velocity
d	diameter		
δ	relative volume of the variable pulp cell	Indices and superscripts	
3	holdup	ар	aerated pulp
h	height	at	newly attached particles
Н	froth depth	atm	measured at atmospheric pressure
$H_I$	interface position	b	bubbles or bias
$I^*$	position of the first phantom pulp cell	С	concentrate
J	superficial velocity $(Q/A_c)$	cell	simulation cell with constant volume
$J_b$	water bias	e	entrained stream
$J_{ m gs}$	gas-slurry drift flux citep	ex	external
k	kinetic rate constant	f	feed
$k_1$	function	fpos	position of the slurry feed port
λ	function	fz	froth zone
M	network matrix	g	gas
$\mu$	viscosity	i	simulation cell position
ns	number of mineral classes	I	interface
$N_t$	number of simulation cells	1	liquid
P	pressure	ld	liquid drifted
Q	volumetric flow rate	р	pulp or particles
$Q'_{g^*}$	gas flow rate through the interface cell computed before	pat	particle attachment rate
	applying the correction for the variation of interface po-	pd	particle drifted
	sition	pdet	particle detachment rate
Re	Reynolds number	1	phantom simulation cell
$\rho$	specific gravity	pz	pulp zone
$R_{v}$	average bubble radius in cm	ref	reference
S	s vertical profile in a simulated flotation column:	r	returned stream
	$\mathbf{S} = [s^1, s^2, \dots]^T$	sb	solids attached to bubbles
S	generic variable or Laplace variable	S	solids or slurry
t	time	t	tails
$t_s$	simulation period	w	water or wash water
$U_{ps}$	relative particle settling velocity	wpos	position of the wash water feed port

balance to a vertically distributed volume mixers-in-series framework: a perfectly mixed aeration zone, a perfect-mixers-in-series lower collection zone, a single perfectly mixed feed zone, a perfect-mixers-in-series upper collection zone, the interface, and three plug flow volumes for the froth (stabilised froth, wash water addition zone, and draining froth). Notwithstanding improvements in column flotation simulation, the extent of potential control applications was significantly narrowed down by not allowing carrying out dynamic flow rate variations. In fact, operating conditions were fixed off-line and remained constant throughout the simulation. The process was then driven from an initial to a final state as defined by the simulated operating conditions. Gas holdup and solids flow rate changes were computed, but the dynamic variations of froth depth were not considered. Cruz nevertheless achieved a major breakthrough, even though this work did not attract much attention in the mineral processing community.

On a more specific basis, the froth physics issue was extensively studied by Neethling and Cilliers (2001, 2002a), Neethling et al. (2002), Neethling (2008), and more recently by Brito-Parada et al. (2012), who extended the model of Neethling et al. (2000) to consider unsteady state in up to three dimensions". The proposed computational fluid dynamics (CFD) model studies liquid drainage in foams from a description of the "the balance of the gravity, cap-

illary and viscous forces acting on the liquid in the Plateau borders in a flotation foam".

For process control purposes, simulators may be explicitly used for two different aims:

- 1. nonlinear model-based control (NMC) and
- 2. real-time optimization (RTO).

The simulated process response is used in both cases for computing an objective function to be minimised. It must be emphasised that unlike RTO, NMC requires dynamic models.

According to Henson (1998), the use of commercial dynamic simulators for nonlinear predictive control had not yet been reported in the literature at the end of the nineties. The main reason explaining this is certainly that the complexity of the on-line solution of the nonlinear programming problem increases with that of the model, hence leading to computational and reliability difficulties. The unavailability of the model equations to the control designer is another factor that cannot be denied (Henson, 1998). However, Desbiens and Bouchard (2004) and Bouchard et al. (2005) presented novel predictive control formulations mitigating these obstacles, where the explicit minimisation of the cost function was replaced by a simulation.

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