



## Regular article

# Development, identification and validation of a mathematical model of anaerobic digestion of sewage sludge focusing on H<sub>2</sub>S formation and transfer



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## ABSTRACT

Nowadays, there are plenty of models of the anaerobic digestion process, however the impact of this odor emission on these models has received very little attention. Hydrogen sulfide (H<sub>2</sub>S) has been used as odor trace marker for odor dispersion studies which is formed by microbial action of sulfate reducing bacteria under anaerobic conditions. A mathematical model with focus on the H<sub>2</sub>S generation with a reduce number of parameters of five stages was developed. The model and parameters were calibrated and validated with experimental data from two pilot scale anaerobic reactors treating sewage sludge. The developed model is able to describe properly the dynamic behavior of this system, particularly, its gas phase composition with an accuracy of 90%, for hydrogen sulfide and carbon dioxide, and 60% for methane, within 99% of confidence.

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## 1. Introduction

In bioprocesses, the application of mathematical models allows representing and predicting the system's dynamic behavior and therefore, the establishment of control strategies and operational management measures. Unfortunately and despite the significant progress of the modeling practice in anaerobic digestion (AD), a proper application of mathematical modeling for control strategies remains a complex and an unsolved issue, which is caused, among other things by the lack of reliable, informative and affordable on-line measurement of the state variables [1]. The anaerobic digestion model n1 (ADM1) is a widely used model in AD, which provides a good tool to illustrate the complex system behavior of the AD [2]. However, in order to represent this complexity entails a high number of state variables as well as the physicochemical

and biochemical processes, consequently a high number of parameters that need to be properly identified [3]. It is therefore that, simpler, although still mechanistic, models have been developed. That is the case of the AM2 model developed by Bernard et al. [1] and several modifications [3,4], which simplifies the whole anaerobic process in two stages, acidogenesis and methanogenesis. When the hydrolysis is the limiting step of the whole reaction, for instance when particulate substrate are treated, it is necessary to include the hydrolysis stage, previous to the acidogenesis [5].

The main odor emissions released to the atmosphere from the operation of WWTP come from several organic gases, but they can be characterized in terms of odor nuisance produced by sulfur reduced compounds, with H<sub>2</sub>S as the main compound [6–9]. The H<sub>2</sub>S generation is mainly based on the action of sulfate reducing bacteria (SRB) that can compete with methanogenic archaea for the intermediate carbon source [10,11]. However, the H<sub>2</sub>S generation has been barely considered when using simplified models [12,13] despite, as previously mentioned, the importance of this compound on the global performance of the sludge management and treatment system as well as odor generation in WWTP [9].

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## Nomenclature

$X_0$	particulate organic matter (gCOD L <sup>-1</sup> )
$S_1$	soluble organic matter (gCOD L <sup>-1</sup> )
$S_2$	acetic acid equivalent (gCOD L <sup>-1</sup> )
$S_3$	sulfate (mg L <sup>-1</sup> )
$K_{s1}$	affinity constant of fermentative bacteria (gCOD L <sup>-1</sup> )
$K_{s2}$	affinity constant of methanogens (gCOD L <sup>-1</sup> )
$K_{s3}$	affinity constant of SRB (gCOD L <sup>-1</sup> )
$K_{a1}$	equilibrium constant H <sub>2</sub> S (mol L <sup>-1</sup> )
$K_j$	stoichiometric coefficient
$X_1$	fermentative bacteria (gCOD L <sup>-1</sup> )
$X_3$	sulfate reducing bacteria (SRB) (gCOD L <sup>-1</sup> )
$\mu_{m1}$	maximum specific rate acidogenic bacteria (d <sup>-1</sup> )
$\mu_{m2}$	maximum specific rate methanogenic archaea (d <sup>-1</sup> )
$\rho_{a1}$	acid–base equilibrium rate (mmol L <sup>-1</sup> d <sup>-1</sup> )
$D$	dilution rate (d <sup>-1</sup> )
$\xi_{in,i}$	state variable value in the inlet
$\xi_i$	state variable
$q_c$	molar flow CO <sub>2</sub> (mmol L <sup>-1</sup> d <sup>-1</sup> )
$\rho$	liquid–gas desorption rate (mmol L <sup>-1</sup> d <sup>-1</sup> )
$B$	bicarbonate (mmol L <sup>-1</sup> )
$IC$	inorganic carbon (mmol L <sup>-1</sup> )
$Z$	cations (mmol L <sup>-1</sup> )
$r_{ij}$	reaction rate for state variable $i$
$X_2$	methanogens bacteria (gCOD L <sup>-1</sup> )
$k_h$	hydrolysis coefficient (d <sup>-1</sup> )
$\mu_{m3}$	maximum specific rate SRB (d <sup>-1</sup> )
$K_{Hcc}$	dimensionless Henry constant

The aim of this study is to develop a simplified mathematical model for the anaerobic digestion process that takes into account the hydrolysis and sulfate reducing action for hydrogen sulfide formation such that this model can afterward be used to assess the odor impact of the anaerobic digestion emissions.

## 2. Methodology

### 2.1. Model assumptions and considerations

A general scheme of the bioreaction pathways is shown in Fig. 1. The same stoichiometry and reaction kinetics presented by Donoso-Bravo et al. [14] were used in this study but adding the sulfate reducing stage. It must be kept in mind that any model is a mathematical projection of the actual process. For this reason, some reasonable and affordable assumptions, within the scope and objective of the model application, must be done.

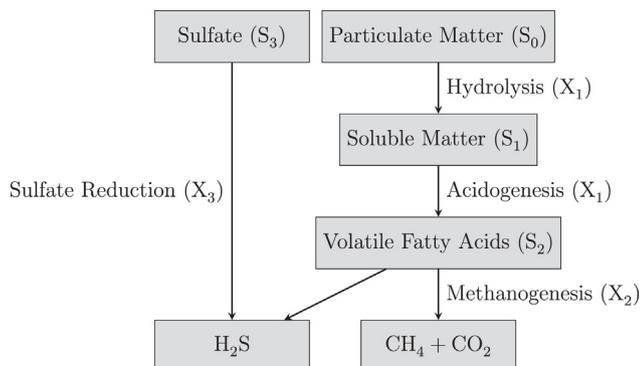
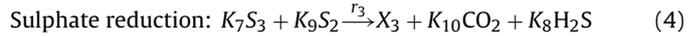
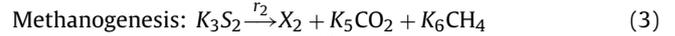
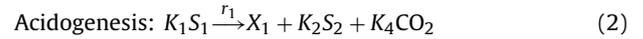


Fig. 1. Scheme of the anaerobic digestion for hydrogen sulfide production.

- There is no biomass death decay.
- The volatile fatty acids (VFA) are represented as acetic equivalents.
- Three microbial populations are involved in the hydrolysis, acidogenesis, methanogenesis and sulphate reduction.
- Hydrogen production/accumulation is negligible. Therefore, SRB use the VFA as electron donor and the sulfate as electron acceptor, instead of hydrogen.
- Only bicarbonate/carbon dioxide, hydrogen sulfide/bisulfide, sulphate and proton contribute to pH according to ion balance.
- There is no metal precipitation, such as FeS.
- Biogas release is carried out by the two-film theory according to the global mass transfer coefficient  $K_LA$  for hydrogen sulfide and carbon dioxide, whereas methane solubilization in water is assumed to be negligible.

### 2.2. Biological model

The first stage corresponds to the solubilization or hydrolysis of the particulate substrate, afterwards the soluble complex substrate is transformed into volatile fatty acids (VFA) which are represented as acetic equivalent, during the acidogenesis reaction, followed by the methanogenic step where the VFA are converted into biogas. Sulfate reduction process is carried out in parallel by the SRB using the VFA as electron donor and the sulfate as electron acceptor. The stoichiometric reactions considered in this model follow:



The hydrolysis was modeled as a Contois function because hydrolysis is considered an enzymatic reaction carried out by hydrolytic/acidogenic bacteria and assumes that a high amount of extra-cell enzyme is a consequence of an increase amount of the biomass, which leads to an increase of the reaction kinetics. Otherwise, it has been shown the Contois function works better than classic first-order kinetics [15]. FB and SRB bacteria are well described their growth function by Monod kinetic, while MB can experiment uncompetitive inhibition for VFA accumulation which is best described by Haldane kinetic [1,11]. Thus, the kinetics for specific growth rate equation for FB, SRB, MB and hydrolysis are described by the following equations,

$$\text{Hydrolysis: } r_0 = k_h \cdot \frac{S_0}{K_{s0} \cdot X_1 + S_0} \cdot X_1 \quad (5)$$

$$\text{Acidogenesis: } r_1 = \mu_{m1} \cdot \frac{S_1}{K_{s1} + S_1} \cdot X_1 \quad (6)$$

$$\text{Methanogenesis: } r_2 = \mu_{m2} \cdot \frac{S_2}{K_{s2} + S_2 + \frac{S_2^2}{K_{j2}}} \cdot X_2 \quad (7)$$

$$\text{Sulphate reduction: } r_3 = \mu_{m3} \cdot \frac{S_2 \cdot S_3}{(K_{s3} + S_2) \cdot (K_{s4} + S_3)} \cdot X_3 \quad (8)$$

The mass balance for a continuous stirred reactor for each state variable is expressed by the following equation,

$$\frac{d\xi_i}{dt} = D \cdot (\xi_{in,i} - \xi_i) + \sum_{j=1}^4 (K_{ij} \cdot r_j) - \rho_i \quad (9)$$

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