



A new approach to non-fragile state estimation for continuous neural networks with time-delays [☆]



Fan Yang ^a, Hongli Dong ^{a,*}, Zidong Wang ^{b,c}, Weijian Ren ^a, Fuad E. Alsaadi ^c

^a College of Electrical and Information Engineering, Northeast Petroleum University, Daqing 163318, China

^b Department of Computer Science, Brunel University London, Uxbridge, Middlesex UB8 3PH, United Kingdom

^c Faculty of Engineering, King Abdulaziz University, Jeddah 21589, Saudi Arabia

ARTICLE INFO

Article history:

Received 10 December 2015

Received in revised form

29 January 2016

Accepted 15 February 2016

Available online 16 March 2016

Keywords:

Recurrent neural networks

State estimation

Non-fragility

Time-delays

Lyapunov functional

Matrix inequality

ABSTRACT

In this paper, the non-fragile state estimation problem is investigated for a class of continuous neural networks with time-delays and nonlinear perturbations. The estimator to be designed is of a simple linear structure without requiring the exact information of the activation functions or the time-delays, and is therefore easy to be implemented. Furthermore, the designed estimator gains are allowed to undergo multiplicative parameter variations within a given range and the non-fragility is guaranteed against possible implementation errors. The main purpose of the addressed problem is to design a non-fragile state estimator for the recurrent delayed neural networks such that the dynamics of the estimation error converges to the equilibrium asymptotically irrespective of the admissible parameter variations with the estimator gains. By employing a combination of the Lyapunov functionals and the matrix analysis techniques, sufficient conditions are established to ensure the existence of the desired estimators and the explicit characterization of such estimators are then given via solving a linear matrix inequality. Finally, a simulation example is used to illustrate the effectiveness of the proposed design method.

© 2016 Elsevier B.V. All rights reserved.

1. Introduction

For several decades, recurrent neural networks (RNNs) have been a focus of research mainly because of their capability of learning and approximating nonlinear functions in an adaptive way. So far, a variety of RNN architectures as well as RNN learning schemes have been used for pattern recognition, classification, regression and optimization problems with practical applications in many areas such as system identification and control, trajectory prediction, decision making and medical diagnosis [9,13]. On the other hand, due to finite switching speed of amplifiers in electronic neural networks and finite signal propagation time in biological networks, the time-delays in signal transmission are often unavoidable. If not properly taken into account, the time-delays would cause the undesirable oscillation and even the instability. In the past 10 years or so, the time-delay phenomenon has received considerable research attention in the dynamic analysis problems for various neural networks [6,8,12,17,33]. For example, in [35], a kind

of observer-based adaptive neural network controller has been designed for a class of single-input single-output strict-feedback nonlinear stochastic systems with unknown time-delays. In [26], the problem of global exponential stability of static neural networks with time delay and impulses has been investigated by using the Lyapunov functional and the Razumikhin-type techniques.

For the successful application of neural networks, it is often a prerequisite to know the actual information about the neuron states which can then be used for optimization or control purposes. However, due to resource and physical limits, it is quite common that only partial information about the neuron states is available through the network outputs especially in relatively large-scale neural networks. As such, an imperative task is to estimate the neural states as precisely as possible via the available network outputs [25], and the resulting state estimation problem for neural networks has attracted an ever-increasing research interest in the past decade and a rich body of literature has been published, see e.g. [3,5,7,20] and the references therein. In particular, a state estimator has been designed in [27] for discrete-time neural networks with Markovian jumping parameters and time-varying delays. The problem of observer-based state estimation has been studied in [15] for fuzzy neural networks (FNNs) with time-varying structured uncertainties and time-varying delays.

In the course of controller/estimator implementation, it is often the case that the actually implemented parameters are slightly different from the expected ones owing to various reasons such as numerical roundoff errors, limited word length of the computer and

[☆]This work was supported in part by the National Natural Science Foundation of China under Grants 61422301 and 61374127, the Outstanding Youth Science Foundation of Heilongjiang Province under Grant JC2015016, the Technology Foundation for Selected Overseas Chinese Scholar from the Ministry of Personnel of China, and the Alexander von Humboldt Foundation of Germany.

* Corresponding author.

E-mail addresses: shiningdhl@vip.126.com (H. Dong),

Zidong.Wang@brunel.ac.uk (Z. Wang).

the imprecision in analog–digital conversion. It is now a well-known fact that small even tiny variations/drifts of the estimator/filter/controller parameters could lead to dramatic changes (e.g. performance degradation or even eventual instability) of the overall system dynamics [2,10], and such kind of phenomenon is referred to as the fragility. In the past few years, the non-fragility has become an increasingly important performance index that aims to guarantee that the desired system behavior is insensitive to the admissible implementation errors for the controllers/estimators. For example, in [37], a non-fragile H_∞ filter has been designed for a class of discrete-time T–S fuzzy systems with both randomly occurring gain variations (ROGVs) and channel fading. In [28], the issue of the non-fragile robust finite-time H_∞ control has been dealt with for a class of uncertain nonlinear stochastic Itô systems via neural network. In [4], a non-fragile procedure has been introduced to study the problem of synchronization of neural networks with time-varying delay.

In the context of non-fragile estimation for neural networks, some initial results have appeared in the literature. For example, in [23], the non-fragile observer design problem has been dealt with for neural networks with mixed time-varying delays and Markovian jumping parameters by developing a reciprocal convex approach. Furthermore, the non-fragile state estimation problem has been investigated in [16] for a class of memristive neural networks with two different types of memductance functions and uncertain time-varying delays by using the Wirtinger-type inequality analysis. It should be pointed out that, in [16,23], the structure of the estimator/observer to be designed has been assumed to be similar to that of the underlying neural network so as to facilitate the subsequent dynamics analysis. Such an assumption, however, implies that the time-varying delays and the activation functions would have to be exactly known in order to make practical sense of the estimator/observer implementation. Unfortunately, utilization of such complex estimators/observers is pretty inconvenient as this would place great demands on the parameter identification as well as the engineering realization. As such, a seemingly natural idea is to develop an easy-to-implement state estimator which is of a simple structure so as to facilitate the practical application with guaranteed estimation performance, and this constitutes the main motivation of this paper.

In this paper, we deal with the non-fragile state estimation problem for a class of continuous neural networks with time-varying delays. By employing a combination of the Lyapunov functionals and the matrix analysis techniques, sufficient conditions are established to ensure the existence of the desired estimators and the explicit characterization of such estimators are then given via solving a linear matrix inequality. A simulation example is used to illustrate the effectiveness of the proposed design method. Comparing to the existing results, the novelty of this paper is mainly twofold: (1) the structure of the non-fragile estimator is of a simple linear form that contains two constant gain matrices, thereby facilitating the practical implementation and (2) the estimator gains are allowed to tolerate multiplicative parameter variations within a given range and such multiplicative form can better reflect the gain-dependent perturbations.

Notation: The notation used in this paper is fairly standard except where otherwise stated. M^T represents the transpose of M . \mathbb{R}^n represents the n dimensional Euclidean space and $\mathbb{R}^{n \times m}$ is the set of all $n \times m$ real matrices. The notation $P > 0$ means that P is a real, symmetric, positive definite matrix. $\|x\|$ stands for the Euclidean norm of a vector x . The notation $\text{diag}\{A_1, A_2, \dots, A_n\}$ stands for a block-diagonal matrix, and $*$ always denotes the symmetric block in a symmetric matrix. The notation $\lambda_{\max}(\cdot)$ shows the maximum eigenvalue.

2. Problem formulation

Consider a class of delayed neural network described by:

$$\dot{x}(t) = -Cx(t) + Ag(x(t)) + Bg(x(t-h(t))) \quad (1)$$

where $x(\cdot) = [x_1(\cdot), x_2(\cdot), \dots, x_n(\cdot)]^T \in \mathbb{R}^n$ is the neural state vector, $g(x(\cdot)) = [g_1(x_1(\cdot)), g_2(x_2(\cdot)), \dots, g_n(x_n(\cdot))]^T \in \mathbb{R}^n$ is the nonlinear activation function with the initial condition $g(0) = 0$, $C = \text{diag}\{c_1, c_2, \dots, c_n\}$ is the positive definite diagonal matrix, A and B are the connection weight matrix and the delayed connection weight matrix, respectively. $h(t)$ is the time-varying delay satisfying

$$0 \leq h(t) \leq h \quad (2)$$

$$\dot{h}(t) \leq \mu \quad (3)$$

where h and μ are constants.

The activation function $g(\cdot)$ satisfies the following Lipschitz condition:

$$\|g(x) - g(y)\| \leq G\|x - y\| \quad (4)$$

where $G = \text{diag}\{g_1, g_2, \dots, g_n\}$ is a known diagonal matrix.

The measurements of the neural network are expressed as follows:

$$y(t) = Dx(t) + f(t, x(t)) \quad (5)$$

where $y(t) \in \mathbb{R}^m$ is the measurement output, $D \in \mathbb{R}^{m \times n}$ is a known constant matrix. $f(t, x(t))$ is a neuron-state-dependent nonlinear perturbation at the output of the network with the initial condition $f(0, 0) = 0$. $f(t, x(t))$ satisfies the following Lipschitz condition:

$$\|f(t, x_1) - f(t, x_2)\| \leq F\|x_1 - x_2\| \quad (6)$$

where $F = \text{diag}\{f_1, f_2, \dots, f_n\}$ is a known constant matrix.

The full-order non-fragile state estimator is of the following form:

$$\dot{\hat{x}}(t) = (A_F + \Delta A_F)\hat{x}(t) + (B_F + \Delta B_F)y(t) \quad (7)$$

where $\hat{x}(t)$ is the state estimation of the neural network, A_F and B_F are the gain matrices of the estimator to be designed. ΔA_F and ΔB_F quantify the estimator gain variations satisfying the following norm-bounded multiplicative form [11]:

$$\Delta A_F = A_F H_A F_A(t) E_A \quad (8)$$

$$\Delta B_F = B_F H_B F_B(t) E_B \quad (9)$$

where H_A , H_B , E_A and E_B are known matrices with appropriate dimensions, $F_A(t)$ and $F_B(t)$ are unknown matrices satisfying $F_A^T(t) F_A(t) \leq I$ and $F_B^T(t) F_B(t) \leq I$.

Remark 1. As discussed in the introduction, the non-fragile state estimation problem for time-delayed neural networks has stirred some initial research attention. In the existing literature (e.g. [16,23]), two typical assumptions are that the estimator gain variation is additive and the time-delays are exactly known due to their involvement in the estimator structure. These assumptions are, unfortunately, a bit restrictive in practice. On one hand, a high gain tends to result in a big gain variation during the implementation, which means that the range of the gain variations is largely dependent on the gain itself. As such, the gain variation is usually multiplicative (rather than additive) with respect to the gains. On the other hand, in the case that the exact identification of the time-varying delays is difficult, it is often desirable to have a delay-independent estimator capable of tolerating the delay effects. Therefore, in this paper, a novel delay-independent estimator is introduced in (7)–(9) where the multiplicative gain variations are introduced.

For analysis convenience, we denote

$$\eta(t) = [x^T(t) \hat{x}^T(t)]^T, \quad H_1(\eta(t)) = [g^T(x(t)) \ g^T(\hat{x}(t))]^T,$$

$$H_2(t, \eta(t)) = [f^T(t, x(t)) \ f^T(t, \hat{x}(t))]^T.$$

Download English Version:

<https://daneshyari.com/en/article/411440>

Download Persian Version:

<https://daneshyari.com/article/411440>

[Daneshyari.com](https://daneshyari.com)