



Multilevel survival modelling of recurrent urinary tract infections

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ABSTRACT

A multilevel survival frailty model is presented for analyzing clustered and recurrent urinary tract infections among elderly women residing in aged-care institutions. At the subject level, serial dependence is expected between recurrent events recorded on the same individual. At the cluster level, correlations of observations within the same institution are present due to the inherent residential environment and hierarchical setting. Two random components are therefore incorporated explicitly within the survival frailty model to account for the simultaneous heterogeneity and autoregressive structure. A Splus computer program is developed for the estimation of fixed effect and variance component parameters.

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1. Introduction

Survival frailty models are commonly used to analyse survival data in different health and biomedical settings, by assuming gamma and log-normal distributions for the random effects [1–3]. Alternatively, random effects Cox models can be defined by specifying the first and second moments of the frailty distribution [4]. The advantage of applying log-normal frailty model is its flexibility on the correlation structure for the failure time data, while keeping the interpretation of regression coefficients meaningful. For example, in order to handle time dependent correlated frailties, Yau and McGilchrist [5] proposed a log-normal frailty model incorporating an autoregressive correlation structure for the frailty term.

Multilevel models [6] are also available for handling nested survival data. A multilevel frailty model with two nested random effects has been developed, in which the random effects

follow a gamma distribution [7]. For log-normal frailty, similar multilevel models [8] were considered following the generalised linear mixed modelling approach [2]. Zhang and Steele [9] proposed a semi-parametric multilevel survival model, with a non-linear effect for the continuous covariate and a linear effect for categorical covariate in the log-hazard function. Recently, Ha and Lee [10] used multilevel mixed linear models to analyse censored survival data. An application of multilevel frailty modelling of clustered grouped survival data can be found in [11] where the MCMC method is used for parameter estimation.

Our modelling of multilevel survival data is motivated by a longitudinal study of recurrent urinary tract infections sustained by a group of elderly women residing in aged-care institutions. At the facility/cluster level, all subjects from the same institution share a common random institution effect. At the subject level, repeated measurements (recurrent times)

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from the same individual are expected to be correlated. An autoregressive covariance structure is thus specified as part of the variance component for the recurrent times.

2. Recurrent urinary tract infections

Urinary tract infection (UTI) is one of the most common bacterial infections in women, and one in four of these women will develop a recurrence. Between 10% and 20% of women aged 60 years and over are affected by asymptomatic infection or bacteriuria [12]. Various risk factors predispose women of different age groups to recurrence [13]. The prevalence of recurrent UTI also increases for women living in nursing homes [14].

A retrospective cohort study was conducted in 2003 to determine the risk factors associated with recurrent UTI among elderly women in residential aged-care facilities [15]. Eligibility criteria for the subjects were defined to be female residents aged 60 years or above with an institutionalisation period of at least 6 months. A total of 201 subjects satisfying the selection criteria were recruited from six randomly selected aged-care institutions in Perth, Western Australia. Women residing in the same institution were likely to be correlated in terms of contracting UTI because of their exposure to the same environment [15].

It was found that 93 of the 201 women experienced at least one UTI episode during the 2 years follow-up period. For this subgroup of women, the outcome variable was taken to be the duration between successive UTI episodes. In addition to age (in years), available covariates were binary variables indicating the presence or absence of diabetes mellitus, stroke history, history of prior UTI, urinary incontinence, hysterectomy, faecal incontinence, immuno-compromised, and anatomical abnormalities of the urinary tract. Information on these variables was retrieved from records or medication charts held at each institution. The variables were chosen because they are either established or postulated risk factors for recurrent UTI [13].

3. Multilevel survival frailty model with autocorrelation

For the modelling of clustered recurrent times, let T denotes the duration between successive recurrent events or the time to end of study, with D being the associated indicator of event (1) or censor (0). Suppose T_{ijk} is the observed k th recurrent time of the j th individual nested within the i th institution, with $k = 1, 2, \dots, n_{ij}$, $j = 1, 2, \dots, m_i$, $i = 1, 2, \dots, b$. Here, n_{ij} is the number of repeated observations on subject j ; m_i is the number of subjects within institution i ; and b is the number of randomly selected institutions. There are altogether $\sum_{i=1}^b m_i = M$ subjects, $\sum_{j=1}^{m_i} n_{ij} = n_i$ observations within the i th institution, and $\sum_{i=1}^b n_i = N$ observations in total. In this three-level hierarchical setting, conditional on unobservable institution random effect u_i and subject frailties v_{ijk} , observations (T_{ijk} , D_{ijk}) are assumed to be independent. Following the survival frailty approach [2,5,8], the proportional hazard function may

be written as:

$$h(t; i, j, k) = \lambda(t) \exp(\eta_{ijk}), \quad \eta_{ijk} = x'_{ijk}\beta + u_i + v_{ijk},$$

where $\lambda(t)$ is the underlying baseline hazard, x'_{ijk} is a covariate vector corresponding to t_{ijk} , and β is the associated vector of regression coefficients. Let $u = (u_1, \dots, u_b)'$ and $v = (v_{111}, v_{112}, \dots, v_{211}, v_{212}, \dots, v_{b11}, v_{b12}, \dots)'$. The linear predictor can be expressed as:

$$\eta = X\beta + Z_1u + Z_2v.$$

Without loss of generality, we assume u to be normally distributed, $N(0, \sigma^2 I_b)$, independent of v . To further account for the time dependent correlated frailties, a first-order autoregressive correlation structure is adopted for the subject random effects [5,16], so that v follows a $N(0, \theta A(\phi))$ distribution, where $A = \text{diag}(A_{11}, A_{12}, \dots, A_{b1}, \dots, A_{bm_b})$ is a block diagonal matrix with:

$$A_{ij}(\phi) = \frac{1}{1 - \phi^2} \begin{pmatrix} 1 & \phi & \dots & \phi^{n_{ij}-1} \\ \phi & 1 & \dots & \phi^{n_{ij}-2} \\ \vdots & \vdots & \ddots & \vdots \\ \phi^{n_{ij}-1} & \phi^{n_{ij}-2} & \dots & 1 \end{pmatrix}.$$

The following expressions can be derived as:

$$\begin{aligned} A_{ij}^{-1} &= (1 + \phi^2)I_{ij} - \phi J_{ij} - \phi^2 K_{ij} \quad \text{and} \quad \text{trace} \left(\frac{\partial A_{ij}^{-1}}{\partial \phi} A_{ij} \right) \\ &= -\frac{2\phi}{1 - \phi^2}, \end{aligned}$$

where I_{ij} , J_{ij} and K_{ij} are $n_{ij} \times n_{ij}$ matrices; I_{ij} is the identity matrix; J_{ij} has its sub-diagonal entries ones and zeros elsewhere; K_{ij} takes on the value 1 at the first and last element of its principal diagonal and zeros elsewhere. To simplify notation, I , J and K represent the respective block diagonal matrix with element I_{ij} , J_{ij} and K_{ij} , respectively.

The best linear unbiased prediction (BLUP) log-likelihood is the sum of two components $l = l_1 + l_2$, where l_1 is the logarithm of the partial likelihood of recurrent times conditional on u and v , and l_2 is the logarithm of the probability density function of u and v , namely:

$$\begin{aligned} l_2 &= -\frac{1}{2}(b \log(2\pi\sigma^2) + \sigma^{-2}u'u) - \frac{1}{2}(N \log(2\pi\theta) \\ &\quad + \log |A| + \theta^{-1}v'A^{-1}v). \end{aligned}$$

From now onwards, we use i as the index of observations. By sorting the recurrent event/censoring times T_i in ascending order, we have $\eta_i = x'_i\beta + z'_{1i}u + z'_{2i}v$, where x'_i is the vector of fixed covariates, while $z'_{1i}u$ and $z'_{2i}v$ return the value of u or v for the i th observation. For the above log-normal frailty model with u and v conditionally fixed:

$$l_1 = \sum_{i=1}^N D_i \left[\eta_i - \log \sum_{j=i}^N \exp(\eta_j) \right].$$

When the variance parameters σ^2 , ϕ and θ are held fixed, the estimates of β , u and v are given by the Newton–Raphson

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