Short communication

Prospecting for water in the transition zone: d ln(Vs)/d ln(Vp)

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ABSTRACT

We report the values of R = d ln(Vs)/d ln(Vp) due to water as a function of pressure for Mg_2SiO_4 olivine, wadsleyite, ringwoodite. The results show that ringwoodite has significantly lower R than olivine and wadsleyite; due to the reason that bulk modulus of ringwoodite is more sensitive to water than shear modulus. R of ringwoodite decreases with pressure while R of olivine and wadsleyite increases with pressure. R reported here was calculated using theoretical method derived equation of states. R due to temperature is also reported as a comparison of R due to water. The local value of R in the upper mantle and transition zone can discriminate between lateral variations of water content and temperature as the origin of lateral seismic variations.

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1. Introduction

The Earth's transition zone has been postulated to be a rich reservoir of water (Bercovici and Karato, 2003, 2004). Wadsleyite and ringwoodite, the high pressure phases of olivine, have a much greater capacity for accommodating H in their crystal structures than does olivine (Smyth, 1994; Smyth et al., 2003). Testing this hypothesis requires defining a metric that is sensitive to water content and insensitive to other variables that are themselves poorly constrained. Seismic velocities provide high resolution observables that reflect on the state of the material. However, radial variations in seismic velocities largely reflect the effects of pressure on the constituent materials, making it difficult to separate out an effect due to water content. Since the sources of water are likely to be spatially variable, concentrated mostly near subduction zones, we would expect that there are large lateral variations in the water content. Here we explore the possibility of detecting lateral variations in water content through lateral variations in seismic velocity. To accomplish this, the effect of water on the seismic velocity must be distinguishable from that of other chemical heterogeneity in chemistry or temperature. We suggest that the correlation of P and S variations potentially provides such a metric.

The correlation of the variations in P and S wave velocities, often expressed by the variable, R = d ln(Vs)/d ln(Vs), can help identify the specific origin of the underlying heterogeneity. Lateral heterogeneity can be associated with numerous factors, such as temperature, density, chemical composition, water content, attenuation associated with grain size, grain boundary behavior, etc. A particularly interesting feature of R is that one can identify individual effects using mineral physics data. For example, we derive $R(H_2O)$ as the ratio between d ln(Vs)/d(H_2O) and d ln(Vp)/d(H_2O) and $R(T)$ as the ratio between d ln(Vs)/dT and d ln(Vp)/dT. By doing so, one can s0eparate and compare the contribution of water and temperature to the lateral heterogeneity.

Studies from S and P tomographic models (Masters et al., 2000; Robertson and Woodhouse, 1996; Romanowicz, 2001, 2003; Vasco and Johnson, 1998; Vasco et al., 1995) have shown that R is a function of depth, with R being $\sim$1.7 in the upper mantle, R >2.5 in the lower mantle and a maximum of R $\sim$3.8 at D''. R is also used as a scaling constant in some seismic tomography models (Dueker and Sheehan, 1998). Large R indicates that shear wave is affected more than P wave by the variable; small R indicates that bulk modulus is more sensitive than shear modulus to the variable. In this paper, we will focus on two factors: water content and temperature on iron-free minerals. We focus on the olivine, wadsleyite and ringwoodite which have large capacity for water in the Earth's upper mantle and transition zone (Williams and Hemley, 2001).

2. R due to water

There have been a number of papers reporting experimentally measured elasticity of dry and wet olivine (Mao et al., 2010; Zha et al., 1997), wadsleyite (Jacobsen et al., 2009; Mao et al., 2008; Zha et al., 1996) and ringwoodite (Li, 2003; Wang et al., 2003,

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Table 1
Effect of water on Mg_2SiO_4 for olivine α, wadsleyite β and ringwoodite γ at 300 K and 0 GPa from experimental data.

Mg_2SiO_4	$d\rho/$ dH_2O	Ks	G	$dK/$ dH_2O	$dG/$ dH_2O	$R(H_2O)$
α (Mao et al., 2010)	0.026	128.8	81.6	3.78	2.22	0.94
β (Mao et al., 2008)	0.046	170.9	111.7	13.8	7.8	1.02
γ (Inoue et al., 1998; Wang et al., 2003)	0.044	184.3	119.5	10.36	5.36	0.76

Fig. 1. $R(H_2O)$ for Mg_2SiO_4 olivine, wadsleyite and ringwoodite. Olivine-cal, wadsleyite-cal, ringwoodite-cal are calculated using data from Li et al. (2009a), Liu et al. (2009), Tsuchiya and Tsuchiya (2009)), respectively. Ringwoodite-cal b is taken from Panero (2010). Olivine-exp, wadsleyite-exp, ringwoodite-exp are calculated used data from (Inoue et al. (1998), Li (2003), Mao et al. (2008, 2010), Wang et al. (2003).

2006). Table 1 reports $R(H_2O)$ calculated from experimental data at ambient conditions by comparing velocity values of wet and dry samples. Often data from different laboratories are used in the comparison and the total water content of the samples is quite small. Thus, small experimental errors can become magnified in the process of calculating R. Theoretical calculations hold a promise to yield more accurate values of R since the techniques of calculating the properties of both the wet and dry samples are very similar allowing one to focus entirely on the effect of the hydrogen on the acoustic velocities. Elasticity data reported from density functional calculations (Li et al., 2009a; Liu et al., 2009; Panero, 2010; Tsuchiya and Tsuchiya, 2009) is used to derive $R(H_2O)$ for these three phases. These four studies reported elasticity of hydrous Mg_2SiO_4 olivine, wadsleyite and ringwoodite as a function of pressure at zero Kelvin. Water is introduced into olivine structure as defects by either substituting Mg cation or Si cation. Water content ranges from zero percent to saturation (3.3 wt.%) where two Mg atoms are substituted by four hydrogen atoms. To calculate $R(H_2O)$ as a function of pressure, what is needed is the water derivative of elasticity at all pressures, as

$$R = \frac{d \ln Vs}{d \ln Vp} = \frac{d \ln \sqrt{\frac{G}{\rho}}}{d \ln \sqrt{\frac{K+4G/3}{\rho}}} = \left(\frac{G'}{G} - \frac{\rho'}{\rho}\right) / \left(\frac{K' + \frac{4G'}{3}}{K + \frac{4G}{3}} - \frac{\rho'}{\rho}\right) \quad (1)$$
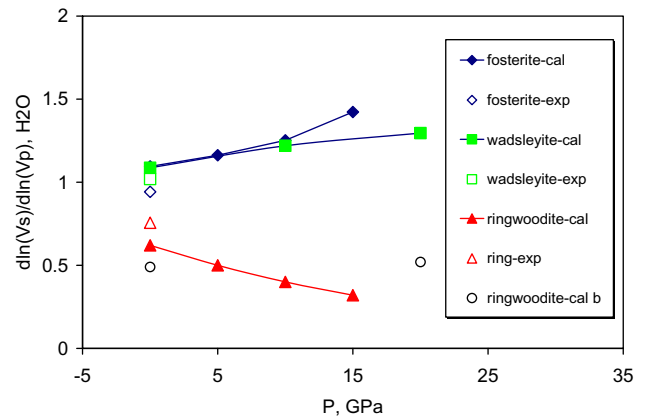
where $\rho' = d\rho/d(H_2O)$, $K' = dK/d(H_2O)$, $G' = dG/d(H_2O)$.

Fig. 1 illustrates $R(H_2O)$ as a function of pressure for Mg_2SiO_4 olivine, wadsleyite and ringwoodite. Both experimental and theoretical elasticity data are included here. $R(H_2O)$ for both olivine and wadsleyite shows positive pressure dependence and values large than 1, while $R(H_2O)$ for ringwoodite decreases with pressure and with a value that is significantly less than 1. The interesting pressure dependence of R is associated with the pressure dependence of elasticity of hydrous phases. As illustrated by (Mao et al., 2010), the cross over of P and S wave velocity occurs at around 3 GPa between dry and wet olivine due to lower modulus but higher pressure derive for wet fosterite. But comparing P and S wave velocities of dry and wet ringwoodite (Li, 2003; Wang et al., 2006), wet ringwoodite has both lower bulk modulus and lower pressure derives of bulk modulus, thus the cross over of P and S waves velocity does not occur. R derived from experimental data at ambient conditions is also plotted. R derived from experimental data is slightly less than 1 and close to the calculated results. In general, the theoretical and experimental values agree to better than 0.2 while the expected uncertainty of the theoretical values is about 0.1 because of the consistency of the method.

3. R due to temperature

To calculate $R(T)$ as a function of pressure, one needs the temperature derivative of elasticity as a function of pressure. In Eq. (1), the variables $\rho' = d\rho/dT$, $K' = dK/dT$, $G' = dG/dT$. Experimental data are not measured at mantle pressure–temperature and are thereby limited in deriving $R(T)$ for the pressure–temperature range of the mantle. Furthermore, we wish to maintain consistency in approach with the calculations of $R(H_2O)$. Thus, we use theoretically calculated thermal EOS to provide this information. In a previous paper (Li et al., 2006a), the thermal EOS of ringwoodite has been reported. It uses the *ab inito* molecular dynamics (AIMD) approach, which simulates the stress–strain relation at elevated pressure and temperature conditions, and has been shown to be an accurate method for calculating elastic properties at high pressure and temperature. It explicitly includes temperature in its simulation and has been used successfully to predict the structural and thermo-elastic properties of mantel silicates (Li et al., 2009b, 2006a,b,c; Oganov et al., 2001a,b). Using the resulting thermal EOS, S and P wave velocities can be derived at any mantle pressure and temperature. In this paper, we report the thermal EOS of olivine and wadsleyite using this method. The thermal EOS parameters have been tested that they can successfully predict the available experimental data for olivine and wadsleyite (shown in Figs. 2 and 3). The AIMD symbols in Figs. 2 and 3 are calculated using thermal EOS (listed in Table 2) and extrapolate to the experimental pressure and temperature conditions to compare with the experimental data. Table 3 summarizes the equations of states for olivine, wadsleyite and ringwoodite referenced to the condition of 2000 K and 0 GPa. The formula of calculating the velocities at pressure and temperature can be found in previous papers (Li et al., 2006a; Oganov et al., 2001a) and thus not reported here.

Fig. 4 shows the $R(T)$ for olivine, wadsleyite and ringwoodite at 300 K and 2000 K, respectively. The first point is that pressure has a positive effect on all three minerals. Secondly, $R(T)$ ranges between

Table 2
Thermo-EOS of olivine from AIMD calculations for Mg_2SiO_4 for the reference state of 2000 K and 0 GPa. The EOS of olivine, α and wadsleyite, β are from this study, the EOS of γ is from (Li et al., 2006a).

Mg_2SiO_4	K_T	V_0	K_T'	G	G'	γ_0	q	α_0	δ	dG/dT	dK/dT
α	110.5	613.4	4.15	58.10	2.51	1.10	1.33	3.07 E−05	4.0	−0.007	−0.002
β	147.4	565.0	4.18	82.06	2.60	1.22	1.01	2.88 E−05	4.0	−0.0085	−0.0015
γ	138.0	560	5.2	90.5	2.07	1.34	1.44	3.85 E−05	5.2	−0.0086	0