

On Intuitionistic Fuzzy Semi - Supra Open Set and Intuitionistic Fuzzy Semi - Supra Continuous Functions

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Abstract

In this paper, we introduce and investigate a new class of sets and functions between topological space called intuitionistic fuzzy semi-supra open set and intuitionistic fuzzy semi-supra open continuous functions respectively..

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1. Introduction and preliminaries.

Intuitionistic fuzzy set is defined by Atanassov [2] as a generalization of the concept of fuzzy set given by Zadesch [9]. Using the notation of intuitionistic fuzzy sets, Coker [3] introduced the notation of intuitionistic fuzzy topological spaces. The supra topological spaces and studied s-continuous functions and s^* -continuous functions were introduced by A. S. Mashhour [5] in 1993. In 1987, M. E. Abd El-Monsef et al. [1] introduced the fuzzy supra topological spaces and studied fuzzy supra continuous functions and obtained some properties and characterizations. In 1996, Keun Min [8] introduced fuzzy s-continuous, fuzzy s-open and fuzzy s-closed maps and established a number of characterizations. In 2008, R. Devi et al [4] introduced the concept of supra α -open set, and in 1983, A. S. Mashhour et al. introduced, the notion of supra- semi open set, supra semi-continuous functions and studied some of the basic properties for this class of functions. In 1999, Necla Turan [6] introduced the concept of intuitionistic fuzzy supra topological space. In this paper, we introduce the notation of intuitionistic fuzzy semi-supra open sets and the basic properties of intuitionistic fuzzy semi-supra open sets and introduce the notation of intuitionistic

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fuzzy semi-supra continuous functions.

Throughout this paper, by (X, τ) or simply by X we will denote the intuitionistic fuzzy supra topological space (briefly, IFTS). For a subset A of a space (X, τ) , $\text{cl}(A)$, $\text{int}(A)$ and $\overline{A}$ denote the closure of A , The interior of A and the complement of A respectively. Each intuitionistic fuzzy supra set (briefly, IFS) which belongs to (X, τ) is called an intuitionistic fuzzy supra open set (briefly, IFSOS) in X . The complement $\overline{A}$ of an IFSOS A in X is called an intuitionistic fuzzy supra closed set (IFSCS) in X .

We introduce some basic notations and results that are used in the sequel.

Definition 1.1 [2] Let X be a non empty fixed set and I be the closed interval $[0,1]$. In intuitionistic fuzzy set (IFS) A is an object of the following form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle : x \in X \}$$

where the mapping $\mu_A : X \rightarrow I$ and $\nu_A : X \rightarrow I$ denote the degree of membership (namely $\mu_A(x)$) and the degree of non membership (namely $\nu_A(x)$) for each element $x \in X$ to the set A , respectively, and $0 \leq \mu_A(x) + \nu_A(x) \leq 1$ for each $x \in X$.

Obviously, every fuzzy set A on a nonempty set X is an IFS of the following form

$$A = \{ \langle x, \mu_A(x), 1 - \mu_A(x) \rangle : x \in X \}$$

Definition 1.2 [2] Let A and B be IFSs of the form $A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle : x \in X \}$ and $B = \{ \langle x, \mu_B(x), \nu_B(x) \rangle : x \in X \}$. Then

(i) $A \subseteq B$ if and only if $\mu_A(x) \leq \mu_B(x)$ and $\nu_A(x) \geq \nu_B(x)$;

(ii) $\overline{A} = \{ \langle x, \nu_A(x), \mu_A(x) \rangle : x \in X \}$;

(iii) $A \cap B = \{ \langle x, \mu_A(x) \wedge \mu_B(x), \nu_A(x) \vee \nu_B(x) \rangle : x \in X \}$;

(iv) $A \cup B = \{ \langle x, \mu_A(x) \vee \mu_B(x), \nu_A(x) \wedge \nu_B(x) \rangle : x \in X \}$;

(v) $A = B$ iff $A \subseteq B$ and $B \subseteq A$;

(vi) $[A] = \{ \langle x, \mu_A(x), 1 - \mu_A(x) \rangle : x \in X \}$;

(vii) $\langle A \rangle = \{ \langle x, 1 - \nu_A(x), \nu_A(x) \rangle : x \in X \}$;

(viii) $1_- = \{ \langle x, 1, 0 \rangle, x \in X \}$ and $0_- = \{ \langle x, 1, 0 \rangle, x \in X \}$;

We will use the notation $A = \langle x, \mu_A, \mu_A \rangle$ instead of $A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle : x \in X \}$;

Definition 1.3. [6] A family τ of IFS's on X is called an intuitionistic fuzzy supra topology (IFST for short) on X if $0_- \in \tau$, $1_- \in \tau$ and τ is closed under arbitrary suprema. Then we call the pair (X, τ) an intuitionistic fuzzy supra topological space (IFSTS for short). Each member of τ is called an intuitionistic fuzzy supra open set and the complement of an intuitionistic fuzzy supra open set is called an intuitionistic

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