



Full length article

Three-dimensional elasticity solution for sandwich panels with corrugated cores by using energy method

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ABSTRACT

Sandwich panels having metallic corrugated cores extremely utilized in various engineering fields such as aerospace, automotive, civil, and naval engineering. Although significant efforts have been dedicated in research into corrugated sandwich panels, analytical solutions are still very few. In this paper, analysis of corrugated sandwich panels with trapezoidal shape is carried out analytically.

In the present study, a new analytical approach is developed for bending analysis of corrugated sandwich panels which have not been considered yet. The out-of-plane properties of corrugated core are obtained based on three dimensional theory of elasticity. The state-space method is implemented in conjunction with double Fourier series to solve the coupled partial differential equations. To validate the present approach, numerical results are compared with the results reported in the literature. The sensitivity analysis of the stress and displacement components to the geometrical parameters of corrugated core and its orthotropy is presented by introducing dimensionless ratios.

1. Introduction

Metallic sandwich panels are one group of laminated composites which are used extensively due to their high stiffness and light weight. These panels consist of thin facings sandwiching a core. The high thickness of core provides higher moment of inertia and increase bending stiffness of sandwich panel. Corrugated sandwich panels are a special type of sandwich panels which have corrugated metallic core with alternate ridges and grooves shaped. These types of panels have very encouraging commercial advantages and they are widely used in various areas such as aerospace, automotive, civil, and naval engineering. Because corrugated cores have complex shaped, equivalent material models are required to obtain equivalent properties of them.

Many researchers studied the equivalent properties of corrugated cores. One of the early works is the work of Libove and Hubka [1]. They showed that shear effects is not negligible and should be considered in equivalent orthotropic plates. Chang et al. [2] computed equivalent in-plane properties of corrugated sandwich plates and investigated the bending behavior of corrugated sandwich panels by using Mindlin–Reissner plate theory. By considering classical plate theory (CPT), Xia et al. [3] used equivalent force method to derive equal stiffness terms for any corrugation shapes.

Based on Mindlin–Reissner theory, Bartolozzi et al. [4] studied

acoustic behavior of corrugated core by using energy method to derive equivalent in-plane properties of corrugated core with sinusoidal shape. In other work, they extended the energy method to characterize the equivalent method for arbitrary shape of corrugated cores [5]. Magnucka-Blandzi et al. [6,7] used classical Euler–Bernoulli and broken–line hypothesis to analyze bending and buckling behavior of sandwich beams with sinusoidal corrugated cores. They also studied the effect of transverse shearing deformation for short and long beams.

Based on first-order shear deformation theory (FSDT), Peng et al. [8] investigated free vibration analysis of corrugated-core sandwich plates with orthotropic cores by using mesh-free Galerkin method. The axial crushing responses of multi-layer trapezoidal aluminum corrugated core sandwich structures, were investigated at quasi-static and dynamic strain rates by Cenk et al. [9].

Zheng et al. [10] proposed an equivalent plate model for corrugated cores by using classical shell theory. They presented a complete set of effective in-plate stiffness. Park et al. [11] extended the homogenization model for corrugated composite cores and presented explicit expressions to calculate effective extensional and bending stiffness for them. They showed that effective stiffness and the anisotropy considerably is affected by ply angles. Buannic et al. [12] considered unit cell made of two thin faces with corrugated core and obtained the effective properties of sandwich panels. They determined the deflection

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Nomenclature		$\bar{U}, \bar{V}, \bar{W}$ non-dimensional displacement
A	cross section	V external vertical force
A	length	x, y, z Cartesian reference coordinates, where x is along the corrugation direction
B	width	
C_{ij}	equivalent constants	
c_{ij}	stiffness elastic constants	
E	elastic modulus	<i>Greek symbols</i>
G	shear modulus	γ_{ij} shear strain
h_c	height of core	δ_H horizontal displacement
h_f	facing thickness	δ_V vertical displacement
h_t	total height of panel	E normal strain
I	moment of inertia	H non-dimensional thickness coordinate
L	Length	ν_{zx} Poisson's ration
M_0	external moment	σ_i normal stress
M	bending moment	τ_{ij} shear stress
N	internal normal force	φ angle of tangent line
P	half period of core	<i>Subscripts</i>
Q	external distributed force	0 $z = 0$
T	internal tangential force	n, m half wave numbers in the x and y directions
t_c	thickness of core sheet	xyz reference coordinates
u, v, w	displacement components in the x, y and z	

of sandwich panels by using Kirchhoff–Love theory. But they acknowledged that it is necessary to use complicated theories like Mindlin–Reissner models to provide accurate results for stiffer panels. Yan et al. [13] presented analytical formulas based on three-point bending test and compared their results with experimental results. Martinez et al. [14] determined equivalent plate model for composite corrugated-core sandwich panels. Boorle and Mallick [15] extended micromechanical approach used by Martinez et al. [14] to consider effects of various geometric parameters on bending response of composite corrugated sandwich panels. Walczak et al. [16] studied Buckling and vibration of metal sandwich beams with trapezoidal corrugated cores. They used Hamilton's principle in conjunction with Kirchhoff–Love hypothesis to derive the governing equations for three-layered corrugated beams.

Although analytical and numerical treatments of corrugated sandwich panels have been performed by many researches but most of them have been limited to calculate the equivalent in-plane properties of corrugated sandwich panels, despite the fact that corrugated sandwich panels are three-dimensional structures and as a result of those extreme orthotropic natures, equivalent out-of-plane cannot be ignored. The current study extends the work by Bartolozzi et al. [4] for out-of-plane properties of corrugated sandwich panels. Moreover, the three dimensional bending analysis are conducted by considering the obtained equivalent out-of-plane properties. The three dimensional coupled partial differential equations are reduced to the ordinary differential equations by expanding the field variables to double Fourier series along in-plane directions. Then, the state space method is implemented along the thickness direction to solve the problem analytically. The obtained results are compared with classical plate theory (CPT) and the reliability of the CPT is examined.

2. Equivalent orthotropic properties in the z-direction

In this study, trapezoidal sandwich panels are considered with overall thickness h_t , length a and width b as shown in Fig. 1. According to the figure, trapezoidal sandwich panel made up of two upper and lower facing sheets with thickness h_f and a thick core with height of h_c .

The corrugated sandwich panel is considered as a multi-layer composite plate. Using geometrical homogenization approach, the equivalent out-of-plane parameters, i.e. elastic modulus, E_z and Poisson's ration, ν_{zx} are computed. Without loss of generality,

trapezoidal shape is considered for corrugated core in the x -direction. Fig. 2(a) shows schematically a unit-cell of corrugated core contains unit cell of trapezoidal shape. The unit-cell is originated at the lowest clamped end point and the width of the core is assumed to be unit, $b = 1$. As represented in Fig. 2(b), by imposing a vertical force, V , in the z -direction to the upper end of trapezoidal shape, positive vertical displacement, δ_V and negative horizontal displacement in the other direction, δ_H occurs. It is worthy to note that a dummy moment, M_0 , should be applied to the upper end of unit cell to avoid rotation in the xz -plane.

The produced bending moment, normal and tangential forces at a distance x , are

$$M(x) = V \left(\frac{c}{2} - x \right) - M_0 \tag{1-a}$$

$$N(x) = \begin{cases} -V \sin \theta & (AB) \\ 0 & (BC) \end{cases} \tag{1-b}$$

$$T(x) = \begin{cases} V \cos \theta & (AB) \\ V & (BC) \end{cases} \tag{1-c}$$

where θ is angle of tangent. Applying the Castigliano's second theorem, the rotation of the upper end and its vertical and horizontal displacements can be derived as follow:

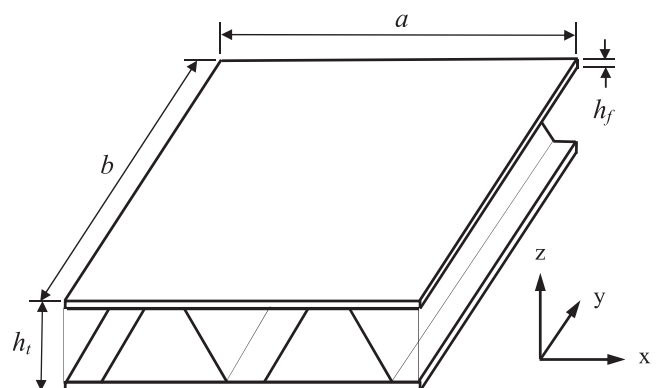


Fig. 1. Schematic representation of sandwich panel with trapezoidal corrugated core.

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