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Short communication

# Allocation of resources for the Gaussian multiple access channel with practical partial cooperation

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#### ABSTRACT

A Gaussian multiple access channel, with partial cooperation between sources, is considered. We develop an encoding scheme in which the transmission is carried out over three orthogonal time phases. The first two phases are exploited such that the two sources can practically and partially exchange their messages. In particular, each phase is terminated when each user can generate the other user's codeword. Then, the two users can cooperatively transmit in the third phase. This formulation is used to (i) develop the achievable rate region, and (ii) numerically study the importance of each phase's length and the allocated power to each user in the three characterized transmission phases.

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#### 1. Introduction

Increasing and improving achievable rates, of different users in any multiuser channel, is a major problem in today's wireless communication networks. Two main techniques to attain such goals are cooperation and resource allocation. Optimization of resource allocation like power and bandwidth was extensively studied in many cooperative scenarios like relay channel and multiple access channel (MAC). For instance, the authors in [\[1\]](#page--1-0) investigated the optimum power and time for a relay channel with decode-andforward strategy. In addition, allocating the right power and time for the multiple parallel relay channel was investigated in  $[2]$ . Further, the authors in  $[3,4]$  studied the problem of allocating power to the two users forming the cooperative MAC. For instance, the authors in  $[4]$  divided the available user power between the cooperative phase and the transmission phase such that the sum rate is maximized.

In the simplest cooperative networks, an intermediate node is employed to help the source–destination pair, as in the relay channel [\[5\].](#page--1-0) This method of cooperation was widely investigated in many different scenarios such as the relay broadcast channel  $[6]$ , multiple access relay channel [\[7\]](#page--1-0), and cooperative MAC [\[8,9\].](#page--1-0) For instance, the author in  $[8]$  developed the capacity region of the MAC channel with partial cooperative encoders. In this setting, the encoders are assumed to be connected via links with finite

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capacities. Further, the authors in [\[10\]](#page--1-0) considered the case in which each encoder, sharing the MAC, has the ability to learn the other user's codeword before transmission. In particular, they derived how much of the codewords the encoders should learn and they also obtained the associated capacity region. However, the established capacity regions in  $[8,10]$  are upper bounds since the sources do not spend power and bandwidth to develop common information. In a recent study, the authors in [\[9\]](#page--1-0) considered the MAC channel, with partial cooperative sources, in which each source can divide its signal into private and public parts. In their cooperating encoding scheme, each user can fully decode and then forward the public part of the other user.

In this paper, the MAC channel in which two sources want to communicate with a common destination is considered. This communication scenario may model two phones communicating with their respective receiver i.e., base station or access point. In the considered channel model, at first, the encoders can partially and practically exchange their information, and can then cooperatively transmit to their common destination. In particular, the transmission period is divided into three phases. Specifically, one of the two sources can transmit such that the other user can capture its signal at the end of the first phase. Then, in the second phase, the second source can transmit until the first source can get the second source's signal. We remind that the scenarios in  $[8,10]$  neither spend power nor bandwidth during the cooperative phases. In the last phase, the two sources can cooperate to transmit their messages. In this case, the achievable rate region is initially obtained. Then, resources such as bandwidth and power are optimized such that the achievable rate region is maximized.







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Specifically, the duration of each phase and the associated power are considered. Our numerical results show that as the number of channel uses allocated to phase 3 increases, so does the achievable rate region. Moreover, under certain conditions, as the duration of either the first or the second phase reduces, the other user may allocate more power for cooperation.

The considered channel model is presented in Section 2. Next, the achievable rate is derived in Section 3. Then, in Section [4,](#page--1-0) some numerical examples are studied to show the value of our theoretical results. Finally, the letter is concluded in Section [5](#page--1-0).

#### 2. Multiple access channel with partial decoding

The Gaussian cooperative MAC, as shown in Fig. 1, is considered. In its simplest form, this channel model is composed of two sources,  $S_1$  and  $S_2$ , that want to communicate with a common destination. These two sources are assumed to operate in half-duplex mode since a node cannot simultaneously transmit and receive. Each source,  $S_k, k \in \{1, 2\}$  wants to send a message,  $M_k$ , which is uniformly selected from the set  $M_k = [1, e^{nR_k}]$  to a destination over<br>naises of the channel such that the probability of error vanishes for n uses of the channel such that the probability of error vanishes for sufficiently large *n*. This communication is performed over three orthogonal time phases. Initially, the two transmitters may partially exchange their information and also transmit to their destination in the first two phases. In addition, suppose that each user knows the other user's code-book. Then, each user may partially listen to the other user until it can generate the other user's entire codeword. For instance, in the first phase, which lasts for  $l_1$  uses of the channel, only the source,  $S_1$ , may transmit to both  $S_2$  and the common receiver. Thus, the received signals at the source,  $S_2$ , and the destination are respectively described as

$$
Y_{12} = g_{12}\sqrt{\mu_1}X_1 + Z_2,\tag{1}
$$

$$
Y_{D1} = h_1 \sqrt{\mu_1} X_1 + Z_D.
$$

where  $X_1$  is the transmitted signal by the source  $S_1$ . This signal is subjected to average power  $P_1$  and the factor  $\mu_1$  determines the power allocated to transmit  $X_1$  in the first phase. Indeed,  $g_{12}$  is the channel gain between the two sources,  $h_1$  is the channel gain between  $S_1$  and the common destination. Further,  $Z_2$  and  $Z_D$  are the additive white Gaussian noises (AWGN) at the source  $S_2$  and the destination, respectively. These noises are independent and have identical distributions with zero mean and variances normalized to 1 through this letter.

Similarly, during the second phase, which lasts for  $(l_2 - l_1)$  uses of the channel, only source  $S_2$  can transmit such that the received signals by the source  $S_1$  and the destination are respectively modelled as

$$
Y_{21} = g_{21} \sqrt{\zeta_2} X_2 + Z_1, Y_{D2} = h_2 \sqrt{\zeta_2} X_2 + Z_D.
$$
 (2)



Fig. 1. MAC channel with a three-phase transmission scheme. The duration of first-, second- and third-phases are  $l_1$ ,  $(l_2 - l_1)$ , and  $(n - l_2)$  uses of the channel, respectively.

where  $X_2$  is the signal generated by  $S_2$ . The average transmit power by this source is constrained by  $P_2$ , and the factor  $\zeta_2$  determines the allocated power to transmit  $X_2$  in the second phase. Further,  $g_{21}$  and  $h_2$  are the channel gains from  $S_2$  to the source  $S_1$  and the destination, respectively. Moreover,  $Z_1$  is an AWGN with zero mean and unit variance.

Finally, in the last phase,  $(n - l_2)$  uses of the channel are used such that the two sources can cooperate to send their signals. This can be obtained by employing superposition encoding [\[11\]](#page--1-0) at each source. Therefore, the sources  $S_1$  and  $S_2$  can generate the following two signals, respectively,

$$
X_{13} = \sqrt{\mu_3 \alpha} X_1 + \sqrt{\frac{\mu_3 \overline{\alpha} P_1}{P_2}} X_2,
$$
  

$$
X_{23} = \sqrt{\zeta_3 \overline{\beta} X_2} + \sqrt{\frac{\zeta_3 \overline{\beta} P_2}{P_1}} X_1,
$$

$$
(3)
$$

where  $\alpha$  and  $\beta$  are the power allocation factors used by  $S_1$  and  $S_2$ , respectively, in phase 3 to transmit their signals. In addition,  $\bar{\alpha} = (1 - \alpha)$ , and  $\bar{\beta} = (1 - \beta)$  are also used by  $S_1$  and  $S_2$ , respectively, to forward the other user's signal. Eurther  $\mu$ , and  $\zeta$ , determine the to forward the other user's signal. Further,  $\mu_3$  and  $\zeta_3$  determine the total allocated power to  $S_1$  and  $S_2$  during the third phase, respectively. In this case, the received signal at the destination is expressed as

$$
Y_{D3} = h_1 X_{13} + h_2 X_{23} + Z_D. \tag{4}
$$

*Remark-1:* Note that the sources,  $S_1$ , and  $S_2$ , do not transmit in the second and the first phases, respectively. Thus, each source should properly allocate its power between the two phases. For instance, the source  $S_1$  may allocate  $\mu_1P_1$  in the first phase with transmission period  $l_1$ , and  $\mu_3P_1$  in the third phase which lasts for  $(n - l_2)$  uses. Thus, the average power is given as

$$
\left(\frac{l_1}{n}\right)\mu_1 P_1 + \left(\frac{n-l_2}{n}\right)\mu_3 P_1 = P_1. \tag{5}
$$

A similar analysis may be used to understand the power allocation at  $S_2$ . In this case, the average power is given by

$$
\left(\frac{l_2 - l_1}{n}\right)\zeta_2 P_2 + \left(\frac{n - l_2}{n}\right)\zeta_3 P_2 = P_2. \tag{6}
$$

#### 3. Achievable rate region of MAC with partial cooperation

In this section, we develop a three-phase transmission scheme such that the two users can exchange their signals and also transmit to their destination. In particular, the first two phases enable the users to partially exchange their messages. For example, each user may listen to the other source until it can completely generate its signal. Then, in the last phase, the two users can cooperatively transmit to their receiver. Here, we outline the signalling and the associated achievable rates in the three phases.

Phase 1: In this phase, the source  $S_1$  is only allowed to transmit. This transmission can be captured by both  $S_2$  and the common destination. The source  $S_2$  is required to partially listen to  $S_1$  until it can generate the entire codeword of  $S<sub>1</sub>$ . Further, the common destination may decode the signal  $X_1$  at the end of phase 3. In this case, the received signals are previously given in  $(1)$ . At the end of this phase, and depend on the first  $l_1$  symbols, the source  $S_2$ may decode the signal  $X_1$  if

$$
R_{S_1S_2} \leq \left(\frac{l_1}{n}\right) C\left(|g_{12}|^2 \mu_1 P_1\right) = I_1
$$
\n(7)

where  $C(x) = \frac{1}{2} \log(1+x)$ . This decoding may be achieved at the source  $S_2$  with probability of error upper bounded by  $P_{e,S_2} \leq e^{-l_1E(G,I_1)}$  in which the Gallager's random coding exponent,  $E(G, l_1)$ , is expressed by [\[12\]](#page--1-0)

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