



Technical Note

Measure of bubble non-uniformity within circular region in a direct-contact heat exchanger



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ABSTRACT

The study of bubble swarm distributions in a direct-contact heat exchanger was addressed both theoretically and experimentally. But recently developed approach based on uniform design for measuring bubbles uniformity and mixing efficiency within rectangular or square region cannot be used to characterize the mixture homogeneity and mixing time within circular region. This paper discussed the difference between rectangular or square region and circular region. A quantitative metric of mixing uniformity is used to characterize the bubble patterns within circular region. Simulation studies are also used to illustrate the proposed methodologies while the experimental case considered demonstrate that the proposed approach evaluated the experimental data rather well. The space-time features of the mixing transient have been successfully derived when the bubble swarms or other objects distribute in a circular region. This work brings new insights to evaluate mixing quality of different systems practically, which has a high degree of accuracy (the percentage of enhancing achieved is about 40%).

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1. Introduction

Direct-contact heat exchanger (DCHE) is one of the most efficient kinds of heat exchangers widely used in numerous engineering systems for carrying out heat transfer between two immiscible fluids [1]. It presents an alternative route for efficient utilization of low temperature waste heat resources. The heat transfer between the phases takes place at the interface. Therefore the knowledge of heat transfer enhancement is fundamental for the design and operation of DCHE [2]. And it is necessary to know about the heat transfer characteristics of dispersed phase droplets in a continuous medium. Due to the complexity of the multiphase flow in exchangers, the heat exchange performance has often been expressed in terms of the volumetric heat transfer coefficient [3]. Huang et al. [5] reported that homogeneous regime is one of the basic bubbling regimes in DCHE but less likely to prevail industrially owing to the high gas flow rates employed. This favors the heterogeneous bubbling regime characterized by a wide range of bubble sizes and

considerable frequencies of breakage and coalescence [4]. Furthermore, the bubble uniformity and mixing efficiency are quantities related to the direct-contact heat transfer coefficient in the light of computational homology [5]. It was found that the direct-contact heat transfer performance was not only about the number of bubble swarms which could be characterized by Betti numbers, but it was all about the spatial-time location of bubble swarms because aggregate was considered to be related to the specific surface area [6]. Mixing must satisfy not only the needs of mass and heat transfer but also the required homogeneity in the vessel in the shortest time in order to obtain high-quality products and high efficiency processes [7]. Measuring the homogeneity properly is of great significant from the practical point view and for the validation of theoretical models as well [8]. The purpose of mixing is to obtain a homogeneous mixture. There is an increased desire for measuring and comparing mixing performance. The presence of dispersed phase makes the flow and mixing process of the continuous phase even complicated. Hence, the investigation of characterizing the homogeneous bubbling regime is one of the most useful and instructive topics in DCHE.

Moreover, accurate characterization of fields uniformity is essential for the optimization of velocity field [9–11], electric fields [12,13], magnetic fields [14,15], etc. A large number of mathematical works have been devoted to studying this issue. In

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practice, characterizing the mixing distribution of these flow patterns quantitatively using image processing technology, which has been effectively used for feature extraction in medical, bioengineering [16], pharmaceuticals [17] and chemical industries, has drawn considerable interest in recent years. Aubin et al. (2010) reviewed existing methods for the characterization of mixing and flow in microchannels, micromixers and microreactors [18]. Gameiro et al. (2005) proposed the use of computational algebraic topology to obtain a characterization of the geometry of the patterns, produced by phase separation processes in compound materials [19]. Xu et al. (2011) also applied computational algebraic topology and image analysis to quantify the mixture homogeneity and non-homogeneity in gas agitated reactors stirred by top lance gas injection [20]. The critical point determination of pseudo homogeneous process impact on the accurate estimation of mixing time could be investigated by three-sigma (3σ) method [2]. Fei et al. (2015) and Xu et al. (2016) addressed the key issue that how to measure the space-time uniformity of random bubble swarm in a domain with minimum discrepancy [6,21]. S^2 , a more meaningful parameter, was also represented to study the mixing transient [22]. Of all the above studies, the L_2 -star discrepancy method is one of the most valuable methods to determine mixing time and acquire more information of mixing process, which can successfully quantify mixing time and degree of homogeneity.

The star discrepancy is the most well-known measure for the uniformity of point distributions [23–26]. It is widely used in multivariate integration, pseudorandom number generation, statistics, and computer graphics. Particularly, regarding the measure of distribution uniformity of bubble swarm in direct-contact boiling heat transfer process, it is common practice to quantify the bubble swarm in rectangle region [6,21,22]. However, the patterns were imaged through a circular viewing window from where we could observe the most active stage of the bubbling regime in the bubble evaporation process. In addition, Fang and Wang (1994) found that if $B_2 = \{(x, y) : x^2 + y^2 \leq 1\}$ is a unit disk, and the natural method is using a circumscribed square C^2 of B_2 and to define the set \mathcal{P} for B_2 by those points inside B_2 [27]. It is simple but has one disadvantage that the points that are uniformly scattered on C^2 are usually not very uniform on B_2 [26,28]. It is therefore of fundamental interest to study how well the methodology agree with experimental observations in this paper. Inspired and motivated by Fang and Wang [27] and Fei et al. [6], we have as main objectives to truly investigate and gauge whether the bubble swarms are uniformly scattered within a circular region and to present an analysis of computer experiments and real obtained imaging data of the direct-contact boiling heat transfer process.

2. Experiment and method

2.1. Experimental study and image analysis

This investigation is focused on the bubble evaporation; the present system is based on the non-isothermal DCHE. It has many advantages such as relative simplicity of design, fewer scaling problems, higher heat transfer coefficient (about 20–100 times that of single-phase flow [29]), having no metallic heat transfer surfaces that are prone to corrosion and fouling, and the capacity to operate at relatively small temperature driving forces [3]. Direct-contact heat transfer process the exchange of heat between the continuous phase, heat transfer fluid (HTF), and the dispersed phase, R-245fa (1,1,1,3,3 pentafluoropropane), by bring them into contact directly at different temperature. The apparatus for DCHE is illustrated in Fig. 1a, and the mixing uniformity measurements were obtained from the DCHE. Intuitively, the DCHE (1) consists of level gauge (2), viewing windows (3), pressure gauge (4), ther-

mometer (5), K-type thermocouple (6) and nozzle (7). The continuous phase was injected into the exchanger at the beginning of our experiment. HTF was heated to the desired temperature that is high enough to make the dispersed phase evaporate completely. After that, the dispersed phase liquid was supplied to DCHE through a tube from a supply tank. Then, the continuous and dispersed phases undergo heat exchange inside the DCHE. The heat transfer process progressively reduces the temperature of R-245fa. The evaporation was allowed to take place until the heat transfer temperature difference had not been enough to cause the phase change of R-245fa. To carried out the experiment, four different parameters, including the height of HTF, the initial heat transfer temperature difference, and the low rate of refrigerant and HTF, were selected. The bubble patterns were imaged using a high-speed shutter video camera (the brand of the video camera was PRAKTICA from Germany and the resolution of the images was 4 million pixels with no light-emitting diode light). For this current analysis, we focused on the properties of mixing transient. The original images are converted to binary images, with black bubbles surrounded by the other nonblack spacing (see Fig. 1b).

2.2. Measures of uniformity within a circular region

There are a number of existing methods in the literature to define uniformity of point distribution [26]. Discrepancy is a well-known statistical measure of point set uniformity. Although various definitions of the discrepancy measures exist in the literature, discrepancy generally provides a single number that define the overall quality of a set of sample points. A large discrepancy indicates deviations from uniformity such as clustering or heterogeneity, while small discrepancy indicates that the pattern is more regular. Generally speaking, if a set of n points is uniformly scattered on a unit disk $B_2 = \{(x, y) : x^2 + y^2 \leq 1\}$, the polar coordinates could be used previously:

$$\begin{cases} x = r \cos(2\pi\theta), \\ y = r \sin(2\pi\theta), \end{cases} \quad (1)$$

where $(r, \theta) \in C^2 = [0, 1]$. In the following discussions, point-set $\mathcal{P} = \{n_i\}_i^N$ denotes the N sample points in an arbitrary bounded two-dimensional Euclidean region of interest Ω . For one rectangular local region $[0, \theta] \times [0, r]$, the number of points encapsulated can be counted. The true area of a local region is given by product θr and the local discrepancy function $d_p^*(\theta, r)$ in this region is given by:

$$d_p^*(\theta, r) = \left| \frac{\mathcal{P} \cap ([0, \theta] \times [0, r])}{N} - \theta r \right| \quad (2)$$

As shown for example in the bottom of Fig. 2, it is obvious that these points are not scattered uniformly on B_2 and that most of these points are concentrated around the center of the B_2 . It is also seen from the top of Fig. 2 that the points are scattered quite uniformly. However, a faulty judgment was obtained by the previous method reported in the literature [6] obviously. Studying carefully its reason, it is immediately clear from Eq. (2) that the star discrepancy is only applicable to rectangular region Ω . This limitation will inhibit its use in new application areas where the region may not be rectangular [27]. If the fan-shaped region is used to replace the rectangle in the definition of F -discrepancy, the Eq. (3) gives a statistical measure for uniformity of \mathcal{P}_F on B_2 .

$$d_p^*(r, \theta) = \left| \frac{N(G, \mathcal{P}_F)}{N} - \frac{\nu(G)}{u(B_2)} \right| = \left| \frac{N(G, \mathcal{P}_F)}{N} - \frac{\pi r \theta}{\pi} \right| = \left| \frac{N((r, \theta), \mathcal{P})}{N} - r \theta \right| \quad (3)$$

where $N((r, \theta), \mathcal{P})$ is used to denote the number points in \mathcal{P} falling inside the rectangle $[0, r] \times [0, \theta]$ which is equal to the number of the points \mathcal{P}_F belonging to the fan-shaped region as follows,

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