



Original research article

Time series prediction using dynamic Bayesian network



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ABSTRACT

Time series prediction is a challenging research topic, especially for multi-step-ahead prediction. In this paper, a novel multi-step-ahead time series prediction model is proposed based on combination of the Kalman filtering model (KFM) and the echo neural networks (ESN). Recently, the studies demonstrate the ESN model is a promising strategy for multi-step-ahead time series prediction, at the same time, the KFM is a recursion-based sequence information processing approach, which has been used effectively for prediction, filtering and smooth of time series data. In this paper, we consider to use the recursion-based KFM to enhance performance of the ESN-based direct prediction model. A novel graph model named the E-KFM that generated from combination of the ESN and the KFM is developed to predict multi-step-ahead time series data. The simulation and comparison results show that the proposed model is more effectiveness and robustness.

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1. Introduction

Recently, time series forecasting is concerned by many researches, most of time prediction models focus on one-step-ahead prediction, the multi-step-ahead prediction is still a challenge topic. We can divide the multi-step-ahead time series forecasting into two kinds of ways [1–3]: direct-based and iterate-based approaches. The direct-based approaches always build prediction models to estimate multi-step-ahead values directly. The iterate-based approaches often first constructs one-step-ahead forecasting framework, and the predictions are usually used as known information to estimate the next ones. In iterate-based approaches, the prediction accuracy is great influenced by cumulative errors, on the other hand, for direct-based methods, time cost of methods always is an important element to be considered.

In split of aforementioned two main trend approaches, other time series forecasting approaches are also concerned, for example, such as, multi-input several multi-outputs (MISMO) forecasting framework [6,7], the multi-input multi-output (MIMO) approach [5], and DirRec method [4], and so on. The MIMO and the MISMO strategy usually concern to get higher prediction accuracy, however, it is often with the higher time cost. The MISMO approaches divide original forecasting problem into subtasks, using optimal solution or cross-validation, to estimate system outputs [8], on the one hand, the forecasting performance is usually not bad, however, the time cost of computation still need to be improved.

In this article, a new graph-based approach is proposed for improving performance of time series forecasting, and the algorithm is based on combination of the echo state network (ESN) [9,10] and Kalman filtering frame. The prediction system is described by the dynamic Bayesian network (DBN), the DBN can present random sequence signals entirely. Our motives can be described as follow.

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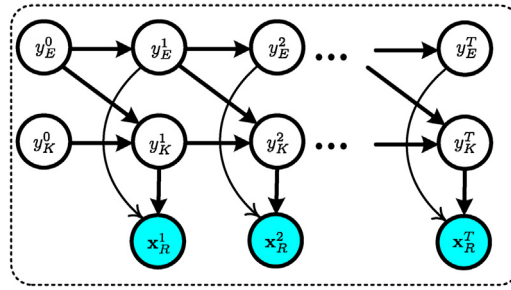


Fig. 1. DBN presentation for E-KFM.

Firstly, in last years, many scholars have proved that the ESN is promising time series prediction system. In many fields, the ESN has been used to predict sequence information [9,10], hence, in this paper, the ESN model is selected as one part of our forecasting frameworks.

Secondly, in split of the ESN method has good prediction performance, only short-time sequence information is used to estimate the coming information. Such as, for the ESN real-time forecasting [9], only previous part of short-time data is utilized as input signals to predict data, if all previous sequence data is used to estimate the coming data, the forecasting performance would be further improved.

In short, in this paper, the short-time forecasting model would be combined with the long-time sequence estimation approach together. The sequence information processing methods usually can use sequence signals entirely and effectively. For example, the Kalman filtering model [11,12] is an effective algorithm to handle sequence signals data, such as, sequence data smoothing, filtering and prediction [13–15]. Further, for random signals representation and processing, the dynamic Bayesian network (DBN) is a good selection. According to [13], the DBN-based sequence processing system is with more flexible representation, on the other hand, the model can work with other models easily. Such, in our paper, a combination frame is proposed, the frame put the ESN-based forecasting model and the KFM together, and the combination system is described using DBN graph model too, it is called the E-KFM time series prediction model.

The rest parts are organized as follows. Section 2 describes the detail steps of the E-KFM for multi-step-ahead prediction. Simulation results are analyzed in Section 3, and conclusions are drawn in Section 4.

2. Prediction model

To build a multi-input and one-output nonlinear system model: $f : \mathbb{R}^D \rightarrow \mathbb{R}$, which is used for h -step-ahead prediction, and it is written as: $\hat{y}(n+h) = f(\mathbf{x}_R(n))$. The $\mathbf{x}_R(n) = [x(n), \dots, x(n-(D-1)\tau)]^T$, where the τ is time delay coefficient, the precondition of time series data reconstruction is $D \geq 2d_1 + 1$, where the d_1 is correlation dimension. Based on the DBN graph model theory and phase space reconstruction theory [16], the DBN graph model of time series prediction is built in Fig. 1, which is a combination of the ESN-based prediction and the KFM model, it is called the E-KFM model.

The ESN is a recurrent-based calculation neural network, it is made up of input layer of signals, a recurrent-based reservoir and signals output layer. Let \mathbf{x}_R^t and y_E^t be the input and output signals in time t , respectively. The echo state e^t inside the reservoir and output y_E^t are generated as follows [10]: $e^t = f(\mathbf{W}_{in}\mathbf{x}_R^t + \mathbf{W}_z e^{t-1})$, and $y^t = e^t \mathbf{W}_{out}$, where $f(\cdot)$ denotes the reservoir activation function, and $\mathbf{W}_{in}, \mathbf{W}_z$ and \mathbf{W}_{out} are weight value matrixes are corresponding to input layer, echo layer and output layer, respectively. In the E-KFM, if let the $x_R(n)$ be input of the ESN, and $y_E(n+h)$ be the h -step-ahead prediction data of the ESN, we have: $\hat{y}_E(n+h) = f_{ESN}(\mathbf{x}_R(n))$, where the $f_{ESN}(\cdot)$ is a function denoted the operation of ESN-based prediction.

Similar to ESN-based prediction, let $x_R(n)$ be the measurements of the KFM, h -step-ahead prediction data $y_K(n+h)$ be the true states of the KFM, we have: $\hat{y}_K(n+h) = f_{KFM}(\mathbf{x}_R(n))$. For simple, let \mathbf{x}_R^t, y_K^t and y_E^t be the value of $x_R(n), y_K(n+h)$ and $y_E(n+h)$ at time t , respectively. Given the observation sequence $\mathbf{x}_R^{1:t}$, the hidden sequence $y_K^{1:t}$ is obtained using the DBN probability inference, the obtained $y_K^{1:t}$ would be the higher accuracy prediction. The detail is discussed as follows.

Based on the DBN graph in Fig. 1, considering the E-KFM model as a physical system, we have:

$$\begin{cases} y_K^{t+1} = \mathbf{F}_t \mathbf{Y}_{K+E}^t + \mathbf{w}_t \\ \mathbf{x}_R^t = \mathbf{H}_t \mathbf{Y}_{K+E}^t + \mathbf{v}_t \end{cases} \quad (1)$$

where $\mathbf{Y}_{K+E}^t = (y_K^t, y_E^t)^T$ and $y_E^t = f_{ESN}(\mathbf{x}_R^t)$, and the $\mathbf{F}_t, \mathbf{H}_t, \mathbf{w}_t$ and \mathbf{v}_t are state transition matrix, observation matrix, system noise and measurement noise, respectively. Both of the \mathbf{w}_t and \mathbf{v}_t are Gaussian distributions: $\mathbf{w}_t = \mathcal{N}(\mathbf{0}, \mathbf{Q}_t), \mathbf{v}_t = \mathcal{N}(\mathbf{0}, \mathbf{R}_t)$, where the \mathbf{Q} and \mathbf{R} are system noise matrix and measurement noise matrix, respectively. Suppose all continue variables in the E-KFM are Gaussian distributions, let prior state of distribution of E-KFM be: $p(y_K^t) = \mathcal{N}(\mu_K, \Sigma_K)(y_K^t)$, and $p(y_E^t) = \mathcal{N}(\mu_E, \Sigma_E)(y_E^t)$. Let the state condition distribution of the E-KFM be $p(y_K^{t+1} | \mathbf{Y}_{K+E}^t) = \mathcal{N}(\mathbf{F}_t \mathbf{Y}_{K+E}^t, \mathbf{Q}_t)(\mathbf{Y}_{K+E}^t)$, and the measurement distribution of the E-KFM be $p(\mathbf{x}_R^t | \mathbf{Y}_{K+E}^t) = \mathcal{N}(\mathbf{H}_t \mathbf{Y}_{K+E}^t, \mathbf{R}_t)(\mathbf{x}_R^t)$. The DBN parameters are calculated using the Maximum Likelihood [11] (ML) algorithm.

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