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Advanced Forecasting Methods Based on Spectral Analysis

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Abstract

This article presents a time series estimation and prediction methods with the use of classic and advanced forecasting tools. In addition, rarely applied in practice approach using spectral analysis to an identification of variation patterns and prediction will be presented. The effect of spectral analysis will be an estimation of prediction model parameters. The main assumption is the model consist of trigonometric functions combination with a certain frequency. The model includes only those frequencies which have greatest influence on process variation. The effectiveness of the method will be examined by a numerical example. The area of the proposed methodology is broad and goes beyond economics.

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Keywords: spectral analysis; forecasting time series;

1. Introduction

Time series analysis allows the detection of the nature described by the line of observation of the phenomenon and the ability to predict future values. Dynamically changing the values of time series are the result of exposure to many factors. which often cannot be identified. To avoid the necessity of determining their quantity. type and quantity of the effect. you can use the strong dependencies that arise between them. registered in the following time units. These variables are often characterized by cyclical variations. and random fluctuations. which can also be changed in accordance with the given pattern. In the time series there is the need to transform the observed values of the variable y_t in a form suitable to determine the dependencies that occur between values. This purpose will be used for spectral

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analysis as a tool for transforming time series into a series in the frequency domain. In the analysis of the mass spectra of the time series $\{y_t: t = 1. 2. \ldots. T\}$ is considered as an infinite sum of time series of different frequencies ω. which correspond to the oscillation periods $\tau = 2\pi/\omega$. For the description of the model will be used the trigonometric functions sine and cosine. i.e. a linear combination of elementary periodic signals. In turn. the transformation will be carried out using a discrete Fourier transformation for product demand data within two months. For the analysis of cyclic fluctuations. a time window of Bartlett will be used. It is an example of a filter which will be used to smooth the spectrum. obtained in the process of time series transformation. This approach allows you to identify those frequency components that contribute significantly to the explanation of changes in the researched time series. On this basis. a forecast for future time periods will be constructed.

2. Review of spectral analysis uses

The time series describing the given phenomena in time. in many cases. may take a chaotic process. Except of the number of components. such as a trend or a constant level of variable. there is also the cyclical and random component. The imposition of many cyclic components of different frequencies in combination with random fluctuations leads to the fact that widely used methods of forecasting are not accurate enough (Clements and Hendry. 2001). The considered phenomenon described using cyclical time series changes. is often called spectral analysis and can be applied to predict future sales in a company. It is a popular method. often used in Geophysics to study the physical processes occurring in the Earth (Burkhard. 2000). in astronomy to study the stars (Chattopadhyay and Chattopadhyay. 2014) and meteorology to predict the weather (Ehrendorfer. 2012). It can also be used for a prediction in the field of transportation as real-time traffic flow (Tchrakian et al.. 2012) or short-term traffic flow forecasting as an element of a hybrid method (Zhang et al.. 2014) using spectral analysis. In the literature of the subject. spectral analysis is not widely used. despite the fact that many economic and logistics phenomena include cyclic changes that are repeated at a certain period of time. In the field of management and optimization of goods and cash flows within companies organized in the logistics network it can be found only a slight mention in a scientific publication about the possibility of using spectral models in forecasting. There are no scientific papers that accurately reflect the technique under consideration approach. supported by the analysis of the efficiency by a representative set of real data. In connection with all the foregoing issues. there is a strong prerequisite for this work to increase benefits from the use of the presented approach in the field of demand forecast of the goods flow. in logistics enterprises.

3. Model formulation

The main objective of spectral analysis is to draw attention to the cyclical processes. It involves the wave structure of considered variables of stochastic processes. allowing us to analyze time series in the frequency domain. This is possible through the use of trigonometric functions as functions sine and cosine. often called harmonics (Anderson. 2011). Each function defined in the interval from 0 to π. The quantity of harmonics for n observations is n/2 (Hearn and Metcalfe. 1995). First harmonic has a period equal to n. the second n/2. one n/3. etc. For the application of this approach the stationarity requirement of the time series should be met [Warner. 1998]. Otherwise. you must delete the trend or to reduce it to stationarity by means of the differentiation operation. (Bisgaard and Kulahci. 2011). Thus. the process can be represented as follows:

$$y_t = f(t) + \sum_{i=1}^{n/2}\left[a_i \sin\left(\frac{2\pi}{n} it\right) + b_i \cos\left(\frac{2\pi}{n} it\right)\right] \quad (1)$$

where: i - number of harmonics. a_1. b_1. a_2. b_2.… - constant values. $f(t)$ - the function describing the observed trend in the series.

The values of the parameters a_1. b_1. a_2. b_2 are obtained by the method of least squares. using the following structures:

$$a_i = \frac{2}{n}\sum_{i=1}^{n}\left[y_t \sin\left(\frac{2\pi}{n} it\right)\right] \quad dla\ \ i = 1 \ldots \frac{n}{2} - 1 \quad (2)$$

$$b_i = \frac{2}{n}\sum_{i=1}^{n}\left[y_t \cos\left(\frac{2\pi}{n} it\right)\right] \quad dla\ \ i = 1 \ldots \frac{n}{2} - 1 \quad (3)$$