



Fractional statistics description applied to protein adsorption: Effects of excluded surface area on adsorption equilibria



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ARTICLE INFO

Article history:

Received 12 June 2013

In final form 22 August 2013

Available online 30 August 2013

ABSTRACT

Adsorption of large molecules blocking more than one adsorption center on a lattice is described as a fractional statistics problem, based on Haldane's statistics. Excluded surface area is characterized by a statistical exclusion parameter, g , which relates to the molecular size and lattice geometry. The theoretical formalism reproduces the classical Langmuir equation (one excluded state limit), and gives a framework and compact equations to consistently describe the adsorption thermodynamics of structurally diverse proteins ranging from simple species to large ligands.

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1. Introduction

Protein adsorption to solid surfaces is a common but very important event that has stimulated a huge research interest in various areas including medicine, pharmaceutical and analytical sciences, biotechnology, cell biology or biophysics [1–16]. Although the adsorption of proteins is a simple phenomenon at first glance, this behavior needs further elucidation in function of many factors that affect it [17]. The understanding of these factors is imperative to improve our ability to design biocompatible materials and biotechnological devices.

Due to the large size and different shapes of these adsorbing particles, the interactions between the adsorbed proteins on the surface are nontrivial and can be strongly influenced by (i) the entropic contribution to the thermodynamic potential arising from the spatial structure of the molecules in the adsorbed state, and (ii) conformational changes after adsorption [17–23].

Recent contributions on equilibrium and kinetics of proteins adsorbed on solid surfaces have focused on the relevance of accounting for the structure and entropic effects of the adsorbed species [17–19,23]. For example, when blood plasma solutions of albumin, immunoglobulin-G (IgG) and fibrinogen (Fgn) are in contact with a polystyrene surface, the initial adsorption is dominated by the smaller protein (albumin), which is also at larger concentrations in the bulk, to be later replaced by the larger proteins like IgG and Fgn [4,5].

Other studies have suggested the possibility that proteins may adsorb in more than a single conformation, and that the probability of adsorbing in a given conformation may vary with the surface

density of adsorbed protein [17,20,23–27]. In Refs. [24,25], the adsorption of single- and two-domain antifreeze proteins onto an ice crystal was studied. The authors derived equations to describe the two adsorbed states of the protein: state I, with the protein adsorbed perpendicular to the surface on single sites; and state II, with the protein lying parallel to the surface and occupying 2 adjacent sites. The phenomenon has also been observed in experiments. In this line, the adsorption of creatine phosphokinase (CPK) onto hydrophilic (silicon wafers and amino-terminated surfaces) and hydrophobic (Polystyrene, PS, coated wafers) substrates has been investigated [26,27]. This study led to a model, where the adsorption of CPK takes place in four stages: (i) a diffusive one, where all the arriving biomolecules are immediately adsorbed; (ii) the arriving biomolecules might stick on the latter one and afterward diffuse to the free sites on the substrate, followed by conformational changes, (iii) formation of a monolayer and (iv) continuous and irreversible adsorption. A multilayer system might be formed, as well as aggregation processes might play a role at this stage.

The observations described above demonstrate that the solution conditions and the protein–surface interactions have to be considered for the proper understanding and description of the adsorption process. The adsorption of small molecules from the gaseous state onto regular surfaces such as the planar faces of crystals has been extensively studied by physical chemists [28,29]. The understanding of such adsorption phenomena has benefited greatly from the ability to prepare systems of extremely high purity and to measure equilibrium adsorption isotherms precisely over a very broad range of concentrations of the gaseous adsorbing species. Analogous measurements of the surface adsorption of soluble proteins have not yielded (and perhaps cannot yield) similarly extensive and precise data. Partly for this reason, the basis for the

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interpretation of such isotherms remains at a level that is quite crude relative to that applied to the analysis of the simpler inorganic systems.

From a theoretical point of view, two classes of models for the adsorption of proteins to surfaces have been formulated. The first class of models [29–31] utilizes continuum theories of two-dimensional hard particle fluids to calculate the chemical potential of the adsorbed species. The second class of models [32] corresponds to lattice models derived from earlier treatments of gas adsorption [33]. Most of these theoretical developments rely upon the crude assumption of spherically symmetric admolecules (each molecule of adsorbate occupies a single adsorption site and one adsorption state is excluded when one particle is adsorbed). As a consequence of these limitations, there exists a lack of research concerning the probable mechanism of protein adsorption and the configuration of the protein in the adsorbed state.

In this context, the main purpose of the present work is to apply the fractional statistical theory of adsorption (FSTA) [34,35] to study the effects of excluded surface area on the adsorption of proteins of different sizes and shapes. The formalism of FSTA have been recently developed on the basis of a generalization of the Pauli's exclusion principle proposed by Haldane [36] and Wu [37]. The appealing feature of Haldane's statistics is that a system of interacting particles confined in a finite region of the space can be characterized by an 'statistical exclusion parameter' g , accounting for the number of states that are excluded from the states spectrum when a particle is added to the system.

The paper is organized as follows: FSTA is presented in Section 2. In order to test the applicability of the proposed model, Section 3 is devoted to the analysis of the adsorption of proteins of arbitrary size and shape. Finally, the conclusions are given in Section 4.

2. Fractional statistical theory of adsorption of polyatomics

In this section, we summarize the basis of the FSTA description [34,35], which allows to describe the configurational entropy through a single function (parameter), namely the statistical exclusion, g , accounting for the configuration of the molecules in the adsorbed state. In this approximation, the interaction of one isolated molecule with a solid surface confined in a fixed volume is represented by an adsorption field having a total number G of local minima in the space of coordinates necessary to define the adsorption configuration. Thus, G is the number of equilibrium states of a single molecule at infinitely low density. In general, more than one state out of G are prevented from occupation upon adsorption of a molecule. Furthermore, because of possible concurrent exclusion of states by two or more molecules, the number of states excluded per molecule, $g(N)$, being a measure of the 'statistical' interactions, depends in general on the number of molecules N within the volume. From the definition of the number of states available for a N th molecule after $(N-1)$ ones are already in the volume V , $d_N = G - \sum_{N'=1}^{N-1} g(N') = G - G_0(N)$, which is a generalization of the one recently established by Haldane [36], the generalized configurational factor, $W(N) = (d_N + N - 1)! / [N!(d_N - 1)!]$, can be calculated. Consequently, the Helmholtz free energy function can be expressed as $\beta F(N, T, V) = -\ln W(N) + N \ln q_i + \beta N \epsilon_o$, q_i being the partition function from the internal degrees of freedom of a single molecule in the adsorbed state. The general form for the chemical potential of noninteracting adsorbed polyatomics is obtained from $\beta \mu = (\frac{\partial F}{\partial N})_{T,V}$, as:

$$\beta \mu = \ln \left[\frac{n \left[1 - \tilde{G}_0(n) + n \right]^{\tilde{G}_0(n)-1}}{\left[1 - \tilde{G}_0(n) \right]^{\tilde{G}_0(n)}} \right] - \ln K, \quad (1)$$

where $n = N/G$ is the density (n finite as $N, G \rightarrow \infty$), $\tilde{G}_0(n) \equiv \lim_{N,G \rightarrow \infty} G_0(N)/G$, $\tilde{G}'_0 \equiv d\tilde{G}_0/dn$ and $K = q_i \exp(-\beta \epsilon_o)$.

It is worth noticing that the Eq. (1) has well known approximate isotherms as limiting cases. Namely, for constant adsorption energy per particle $\epsilon_o = const.$, and spherically symmetric adsorbates (or single-site occupation in the lattice fashion of the adsorption field) which exclude only one state (one minimum), $\tilde{G}_0(n) = n$, $\tilde{G}'_0(n) = 1$, then Eq. (1) reduces to the Langmuir isotherm

$$Kp = \frac{\theta}{(1-\theta)}, \quad (2)$$

where $p \propto \exp(\beta \mu)$, $\theta = n = N/M$ is the surface coverage (fraction of occupied sites) and we have identified the total number of states G with the total number of adsorption sites M .

On the other hand, if the exclusion parameter is constant, $g(n) = g$, $\tilde{G}_0(n) = gn$ and $\tilde{G}'_0(n) = g$, a particular isotherm function arises from Eq. (1)

$$Kp = \frac{n[1 - n(g-1)]^{g-1}}{[1 - ng]^g}. \quad (3)$$

The parameter g in the last equation have a precise physical meaning, can be obtained from adsorption experiments and is related directly to the spatial configuration of a polyatomic molecule in the adsorbed state. Alternatively, Eq. (3) can be used by assuming some approach to calculate g as a function of the model's parameters. Thus, given shape and size of adsorbate, the adsorption isotherm it is straightforwardly obtained.

For molecules made out of k identical units (each of which can occupy an adsorption site in a lattice), a simple approximation for g can be obtained, assuming independence of adsorption sites. Under this consideration, $g = mk$, where $m(\equiv m(c, k))$ is the number of distinguishable configurations of the molecule per lattice site (at zero density) and depends on the lattice/molecule geometry. In addition, $G = mM$ and $n = N/G = N/(mM) = kN/(gM) = \theta/g$. For instance, straight k -mers adsorbed 'in registry' on sites of a square lattice would correspond to $m = 2$, $g = 2k$ and $n = \theta/(2k)$. On the other hand, if $g = k$ ($m = 1$) and $n = \theta/k$, Eq. (3) reduces to the exact adsorption isotherm of noninteracting chains (k -mers) adsorbed flat on a one-dimensional lattice [38]. This is already a simple example of the underlying relationship between the statistical exclusion parameter g and the spatial configuration of the admolecule.

The proposed formalism allows us to deal very simply with a whole variety of configuration of the adsorbed molecule that can occur. In the next section, analysis of lattice-gas simulations has been carried out in order to bear the significance of the parameter g in terms of the adsorbate/surface geometry.

3. Applications: adsorption of proteins of arbitrary size and shape

Before starting the study, and in order to analyze adsorption from liquid solutions, it is convenient to write the theoretical isotherms given in Section 2 in a more appropriate form. In this framework, Eq. (3) adopts the form

$$\ln(Kc) = \ln \theta + (g-1) \ln[g - \theta(g-1)] - g \ln(g - \theta g), \quad (4)$$

where $n = \theta/g$ and the pressure p has been replaced by the concentration of the solute in the liquid c .

Figure 1 shows the adsorption isotherms calculated using Eq. (4) with values of g for various differently shaped particles (see Figure 2): $(a \times a)$ -squares, $k = 4$, $m = 1$ and $g = 4$; $(a \times \sqrt{2}a)$ -triangles, $k = 3$, $m = 4$ and $g = 12$; and $(a \times 10a)$ -rectangles, $k = 22$, $m = 2$ and $g = 44$. The curves from top to bottom correspond to increasing values of g . This effect can be explained as follows. Rectangles

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