# **Accepted Manuscript**

On local quadratic convergence of inexact simplified Jacobi-Davidson method for interior eigenpairs of Hermitian eigenproblems

Zhong-Zhi Bai, Cun-Qiang Miao

PII: S0893-9659(17)30101-5

DOI: http://dx.doi.org/10.1016/j.aml.2017.03.021

Reference: AML 5219

To appear in: Applied Mathematics Letters

Received date: 17 February 2017 Revised date: 30 March 2017 Accepted date: 30 March 2017



Please cite this article as: Z. Bai, C. Miao, On local quadratic convergence of inexact simplified Jacobi-Davidson method for interior eigenpairs of Hermitian eigenproblems, Appl. Math. Lett. (2017), http://dx.doi.org/10.1016/j.aml.2017.03.021

This is a PDF file of an unedited manuscript that has been accepted for publication. As a service to our customers we are providing this early version of the manuscript. The manuscript will undergo copyediting, typesetting, and review of the resulting proof before it is published in its final form. Please note that during the production process errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

### **ACCEPTED MANUSCRIPT**

# On Local Quadratic Convergence of Inexact Simplified Jacobi-Davidson Method for Interior Eigenpairs of Hermitian Eigenproblems \*

Zhong-Zhi Bai<sup>‡ §</sup> and Cun-Qiang Miao<sup>‡ §</sup>

<sup>‡</sup>State Key Laboratory of Scientific/Engineering Computing Institute of Computational Mathematics and Scientific/Engineering Computing Academy of Mathematics and Systems Science Chinese Academy of Sciences, P.O. Box 2719, Beijing 100190, P.R. China Emails: bzz@lsec.cc.ac.cn, miaocungiang@lsec.cc.ac.cn

> §School of Mathematical Sciences University of Chinese Academy of Sciences Beijing 100049, P.R. China

#### Abstract

For the Hermitian eigenproblems, under proper assumption on an initial approximation to the desired eigenvector, we prove local quadratic convergence of the inexact simplified Jacobi-Davidson method when the involved relaxed correction equation is solved by a standard Krylov subspace iteration, which particularly leads to local cubic convergence when the relaxed correction equation is solved to a prescribed precision proportional to the norm of the current residual. These results are valid for the interior as well as the extreme eigenpairs of the Hermitian eigenproblem and, hence, generalize the results by Bai and Miao in 2017 (Linear Algebra Appl. 520(2017), 215-241) from the extreme eigenpairs to the interior ones.

**Keywords:** Hermitian eigenproblem, Jacobi-Davidson method, inexact iteration, standard Krylov subspace iteration, local convergence.

AMS(MOS) Subject Classifications: 65F10, 65F15, 15A18; CR: G1.3.

## 1 Introduction

Consider the standard matrix eigenvalue problem

$$Ax = \lambda x, \quad \text{with} \quad ||x|| = 1, \tag{1.1}$$

where  $A \in \mathbb{C}^{n \times n}$  is a large sparse Hermitian matrix,  $\lambda \in \mathbb{C}$  is an eigenvalue of the matrix A, and  $x \in \mathbb{C}^n$  is the associated (right) eigenvector. Here we denote by  $\|\cdot\|$  the Euclidean norm

<sup>\*</sup>Supported by The National Natural Science Foundation (No. 11671393) and The National Natural Science Foundation for Creative Research Groups (No. 11321061), P.R. China.

### Download English Version:

# https://daneshyari.com/en/article/5471683

Download Persian Version:

https://daneshyari.com/article/5471683

<u>Daneshyari.com</u>