



Scale-independent inflation and hierarchy generation



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ABSTRACT

We discuss models involving two scalar fields coupled to classical gravity that satisfy the general criteria: (i) the theory has no mass input parameters, (ii) classical scale symmetry is broken only through $-\frac{1}{12}\zeta\phi^2R$ couplings where ζ departs from the special conformal value of 1; (iii) the Planck mass is dynamically generated by the vacuum expectations values (VEVs) of the scalars (iv) there is a stage of viable inflation associated with slow roll in the two-scalar potential; (v) the final vacuum has a small to vanishing cosmological constant and an hierarchically small ratio of the VEVs and the ratio of the scalar masses to the Planck scale. This assumes the paradigm of classical scale symmetry as a custodial symmetry of large hierarchies.

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The discovery of the weakly interacting Brout–Englert–Higgs (BEH) boson, coupled with the absence of significant evidence for physics beyond the Standard Model, has stimulated a re-evaluation of the possible explanations of the hierarchy problem. In the Standard Model (SM) of the strong and electroweak interactions, which has no fundamental input mass scale other than the BEH mass, an apparent hierarchy problem arises that is due to the additive quadratically divergent radiative corrections to the mass squared of the BEH boson. However, in the pure Standard Model the quadratic divergences are an artifact of the introduction of a mass scale cut-off in momentum space [1]. In the context of field theory, the coefficients of relevant operators have to be renormalized and the theory is defined ultimately by observable renormalized coefficients. In this case neither the quadratically divergent radiative correction to the BEH mass nor the mass counter-term is measurable and only the renormalized mass is physically meaningful. If one maintains scale invariance broken only explicitly by the various trace anomalies and spontaneously to generate the BEH boson mass, then the latter must be viewed as multiplicatively renormalized since no quadratic divergence arises in the trace anomaly. This has further led to the proposal of classically-scale-invariant models that contain the SM, in which the electroweak scale is generated through spontaneous breaking of scale invariance via Coleman–Weinberg mechanism [2,3].

It has been suggested that scale invariance might even apply at the quantum level through “endogenous” renormalization which requires that the regulator mass scale, μ , associated with quantum loops in dimensional regularization, is itself generated by a moduli field.¹ Alternatively, one can always introduce an arbitrary cut-off scale Λ , e.g., by way of momentum space cut-off or Pauli–Villars regularization, but then renormalize the theory at a renormalization scale given by a moduli field to remove the Λ dependence.² However we will not explore this possibility here, concentrating on whether it is possible to build a viable scale invariant theory broken only spontaneously and via the trace anomaly.

Of course a complete theory must include gravity and, if one is to maintain classical scale invariance, it is necessary to do so in a way that generates the Planck scale through spontaneous breaking of the scale invariance such as occurs in the Brans Dicke theory of gravity [9]. The inclusion of gravity means there are additional additive divergent contributions to the BEH mass but these, too, are unphysical and should be absorbed in the renormalized mass which, as before, is multiplicatively renormalized due to the underlying scale invariance and thus avoids the hierarchy problem.

¹ For a recent discussion see [4] and, in the context of the model discussed below see [6].

² It is easy to see that if one subtracts at some mass scale M that is specified externally to the defining field theory action, then the trace anomaly arises as the variation of the renormalized action wrt $\ln(M)$. In replacing the subtraction scale M by an actual field χ that is part of the defining action of the theory, there is no residual trace anomaly; the trace anomaly is simply absorbed into the improved stress tensor itself, which then remains traceless.

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A problem with the scale independent approach occurs if there are massive states coupled to the BEH scalar for then there are large finite calculable corrections to the Higgs mass. In the Standard Model the presence of the Landau pole associated with the $U(1)$ gauge group factor indicates that the SM becomes strongly interacting at the scale associated with the Landau pole. It is common to assume that there will be massive bound states associated with this strong interaction that will couple significantly to the BEH boson and create the “real” hierarchy problem. One possible way to evade this is to embed the SM in a theory with no Abelian gauge group factor that does not have a Landau pole [21]. This must be done close to the electroweak scale to avoid introducing the hierarchy problem via new massive states and leads to a profusion of new states that may be visible at the LHC. However the Landau pole in the SM lies above the Planck scale where gravitational effects cannot be neglected and it is far from clear what the physics above the Landau pole will be and whether it indeed reintroduces the hierarchy problem. For the same reason we did not insist on the absence of a Landau pole in the model considered here.

Similarly it is possible that, when gravity becomes strong, it leads to massive states that generate the real hierarchy problem. Of course there are black holes that can carry SM gauge group charges and couple to the BEH boson. In general such states do not give rise to an hierarchy problem due to their form factor suppression. It is possible that microscopic black holes exist that do not have such form factor suppression but this is not firmly established and, as with the Landau pole problem, we chose to ignore this possibility here.

In this paper we construct a spontaneously broken scale-free model that includes gravity. As such, there is no physical meaning to the vacuum expectation value (vev) of a single scalar field and only dimensionless ratios are measurable. A minimal model capable of generating an hierarchy requires the introduction of two scalar fields, ϕ and χ coupled to gravity in the form:

$$S = - \int d^4x \sqrt{-g} \left[\frac{1}{12} \alpha \phi^2 R + \frac{1}{2} \nabla_\mu \phi \nabla^\mu \phi + \frac{1}{12} \beta \chi^2 R + \frac{1}{2} \nabla_\mu \chi \nabla^\mu \chi + W(\phi, \chi) \right] \quad (1)$$

where: $W(\phi, \chi) = \lambda \phi^4 + \xi \chi^4 + \delta \phi^2 \chi^2$. This theory has no input mass scales, is conformally invariant if $\alpha = \beta = 1$ and is invariant under independent $\phi \rightarrow \pm \phi$, $\chi \rightarrow \pm \chi$.

The theory has remarkable properties that we illustrate for one representative choice of parameters ($\alpha, \beta, \lambda, \xi, \delta$) in Fig. 1. At early times it has a period of inflation during which, as we will show later on, observationally viable spectra of scalar and tensor perturbations can be generated. Furthermore, it has an infra-red (IR) fixed point set by ratios of the coupling constants and which is radiatively stable to quantum corrections and during which the universe can undergo accelerated expansion.

In the context of unimodular gravity³ references [5,6] provide seminal studies of the model. These studies concentrate on the $\xi = O(1)$ case in which the field χ may be interpreted as the Higgs, in turn requiring $\beta = O(10^5)$ to produce “Higgs inflation”.

In this paper we extend the analysis to cover other values of the parameters. By way of motivation we note that in the context of the hierarchy problem it is important that there should be no heavy states significantly coupled to the Higgs. In this case it has been argued [8] that the solution to the strong CP problem

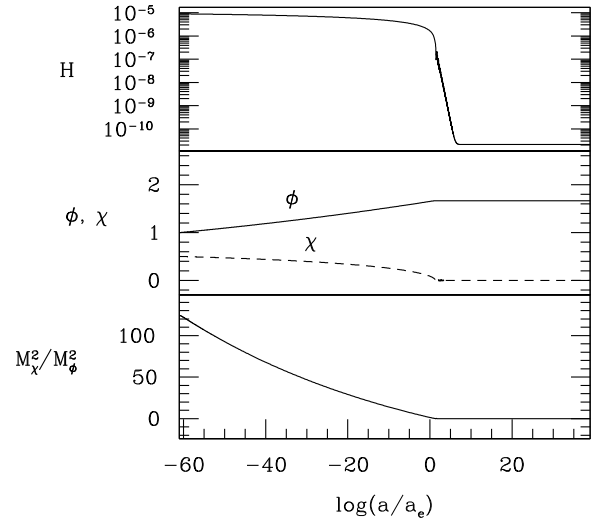


Fig. 1. Plot of the Hubble parameter, H , ϕ , χ and the ratio of the two components of the effective Planck mass, M_ϕ^2 and M_χ^2 , as a function of a ; we have normalized the x-axis to the scale factor at the end of inflation, a_e .

requires the introduction of the axion and, in the context of this model, the most economical solution is to identify the axion with a component of the χ field. However then the coupling ξ must be small to avoid the introduction of a low-lying Landau pole. A second difference is that we determine the inflationary solution in the “Jordan” frame of eq. (1) whereas the analysis of references [5,6] was performed in the Einstein frame. Our analysis has the advantage that it has a simple analytic solution in the slow-roll region, clarifying the origin of the structure of the model. Finally, the IR fixed point structure of the model studied here differs from that in [5,6] where the unimodular constraint introduces an explicit cosmological constant.

In the Jordan frame the field equations immediately follow from eq. (1):

$$M^2 G_{\alpha\beta} = T_{\alpha\beta}^\phi + T_{\alpha\beta}^\chi - g_{\alpha\beta} W(\phi, \chi) \quad (2)$$

where

$$\begin{aligned} T_{\alpha\beta}^\phi &= \left(1 - \frac{\alpha}{3}\right) \nabla_\alpha \phi \nabla_\beta \phi + \left(\frac{\alpha}{3} - \frac{1}{2}\right) g_{\alpha\beta} \nabla_\mu \phi \nabla^\mu \phi \\ &\quad - \frac{\alpha}{3} \phi \nabla_\alpha \nabla_\beta \phi + \frac{\alpha}{3} g_{\alpha\beta} \phi \square \phi \\ T_{\alpha\beta}^\chi &= \left(1 - \frac{\beta}{3}\right) \nabla_\alpha \chi \nabla_\beta \chi + \left(\frac{\beta}{3} - \frac{1}{2}\right) g_{\alpha\beta} \nabla_\mu \chi \nabla^\mu \chi \\ &\quad - \frac{\beta}{3} \chi \nabla_\alpha \nabla_\beta \chi + \frac{\beta}{3} g_{\alpha\beta} \chi \square \chi \end{aligned} \quad (3)$$

and:

$$\square \phi - \frac{\alpha}{6} \phi R - \frac{\partial W}{\partial \phi} = 0, \quad \square \chi - \frac{\beta}{6} \chi R - \frac{\partial W}{\partial \chi} = 0. \quad (4)$$

The effective Planck mass, $M^2 = M_\phi^2 + M_\chi^2$ (where $M_\phi^2 = -\alpha \phi^2/6$ and $M_\chi^2 = -\beta \chi^2/6$) is time varying during the inflationary period (when $M_\phi^2 \ll M_\chi^2$) but constant during the late time accelerated expansion phase (when $M_\phi^2 \gg M_\chi^2$), obeying current constraints on gravitational physics. To obtain the normal form of the Einstein equations at late times, M^2 must be positive and therefore at least one of the coefficients α or β must be negative, inconsistent with the conformally invariant choice. However the resultant theory is still scale-independent [7].

³ The unimodular constraint does not play a role during the inflationary stage.

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