

# A time domain approach for identifying nonlinear vibrating structures by subspace methods

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Received 2 August 2006; received in revised form 21 March 2007; accepted 20 April 2007

Available online 3 May 2007

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## Abstract

Starting from the perspective of nonlinearities as internal feedback forces, a method in the time domain for the identification of nonlinear vibrating structures is described. Although its formulation is very simple, particular care has to be taken to reduce the ill-conditioning of the problem, in order to find numerically stable solutions. To this purpose the robustness and the high numerical performances of the subspace algorithms are successfully exploited, as demonstrated by the implementation of the method on simulated data from single and multi-degree of freedom systems with typical nonlinear characteristics. The method allows to estimate the coefficients of the nonlinearities away from the location of the applied excitations and also to identify the linear dynamic compliance matrix when the number of excitations is smaller than the number of response locations. The results comparison reported in this paper highlights the key advantage of the proposed method: the capability of treating multi-degree of freedom nonlinear systems holding different types of nonlinearities and the capability of selecting non-negligible nonlinear terms, with a light computational effort and with a limited number of time samples.

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**Keywords:** Nonlinear identification; Subspace methods; Time domain; MDOF

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## 1. Introduction

Identification of nonlinear dynamical systems has been thoroughly investigated in recent years and the number of papers published is the proof of growing interest within the research community and also of its effectiveness within the industrial framework. An exhaustive list of the techniques developed to identify the behaviour of nonlinear dynamical systems is hard to write; a few of these techniques, for instance, had a brief success, being sometimes too complicated or not applicable over a wide range of real Multi-Degree Of Freedom (MDOF) systems. A recent up-to-date article draws a complete picture describing the past and recent developments in system identification of nonlinear dynamical structures [1].

The number of methods developed is large and, generally, no method exists to be adopted whenever, for any type of nonlinearity, system complexity or exciting force. A comprehensive list should include the coherence

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## Nomenclature

$A$	dynamical system matrix of the state-space model
$A_c$	dynamical system matrix of the continuous time state-space model
$B$	input matrix of the state-space model
$B_c$	input matrix of the continuous time state-space model
$c$	viscous damping coefficient
$C$	output matrix of the state-space model
$C_v$	viscous damping matrix
$d$	deadspace
$D$	direct feedthrough matrix of the state-space model
$f$	external force vector
$f_{nl}$	nonlinear internal force vector
$F_E$	“input” vector of the NIFO formulation
$g_j(t)$	$j$ th scalar nonlinear function
$h$	number of degrees of freedom
$H$	Frequency Response Function matrix of the underlying linear system
$H_E$	“extended” Frequency Response Function matrix of the nonlinear system
$I$	identity matrix
$i$	number of block rows in block Hankel matrices
$k$	stiffness coefficient
$K$	stiffness matrix
$l$	number of columns in block Hankel matrices
$L_{nj}$	location vector of the $j$ th nonlinearity
$m$	mass coefficient
$M$	mass matrix
$n$	dimension of the state vector
$N_{\text{avg}}$	number of spectral averages
$N_i$	number of input degrees of freedom (external forces)
$N_o$	number of output degrees of freedom
$\mathcal{O}_i$	oblique projection matrix
$p$	number of nonlinear functions
$q$	dimension of the output vector $y$
$r$	time instant
$s$	number of available measurements
$t$	time
$\Delta t$	sampling period
$T$	non-singular $n \times n$ similarity transformation matrix
$u$	input vector
$u_r$	input at time instant $r$
$U_{0 2i-1}$	input block Hankel matrix
$v_r$	measurement noise at time instant $r$
$w_r$	process noise at time instant $r$
$W_p$	past inputs and outputs matrix
$x$	state vector
$x_r$	state at time instant $r$
$y$	output vector
$y_r$	output at time instant $r$
$Y_{0 2i-1}$	output block Hankel matrix
$z$	generalised displacement
$\Gamma_i$	extended observability matrix

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