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## Advances in Water Resources

journal homepage: www.elsevier.com/locate/advwatres

# Integrating a compressible multicomponent two-phase flow into an existing reactive transport simulator



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#### ARTICLE INFO

Article history: Received 15 March 2016 Revised 23 November 2016 Accepted 25 November 2016 Available online 27 November 2016

Keywords: Compressible two-phase flow Reactive transport Sequential iterative coupling Operator splitting HYTEC Equation of state

#### ABSTRACT

This work aims to incorporate compressible multiphase flow into the conventional reactive transport framework using an operator splitting approach. This new approach would allow us to retain the general paradigm of the flow module independent of the geochemical processes and to model complex multiphase chemical systems, conserving the versatile structure of conventional reactive transport. The phase flow formulation is employed to minimize the number of mass conservation nonlinear equations arising from the flow module. Applying appropriate equations of state facilitated precise descriptions of the compressible multicomponent phases, their thermodynamic properties and relevant fluxes.

The proposed flow coupling method was implemented in the reactive transport software HYTEC. The entire framework preserves its flexibility for further numerical developments. The verification of the coupling was achieved by modeling a problem with a self-similar solution. The simulation of a 2D CO<sub>2</sub>-injection problem demonstrates the pertinent physical results and computational efficiency of this method. The coupling method was employed for modeling injection of acid gas mixture in carbonated reservoir.

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#### 1. Introduction

#### 1.1. Background/motivation

Human activity in the subsurface has been expanding and diversifying (waste disposal, mining excavation and high-frequency storage of energy), and the public and regulatory expectations have been increasing. The assessment of each step of underground operations, including environmental impact evaluation, relies on elaborate simulators and leads to an urgent need to develop multiphysics modeling. Reactive transport, a geochemical research and engineering tool, is used in multicomponent systems and sophisticated chemical processes (activity and fugacity correction according to different models, mineral dissolution and precipitation, cation exchange, oxidation and reduction reactions, isotopic fractionation and filiation), in addition to gas evaporation and dissolution (van der Lee et al., 2003; Mayer et al., 2012; Parkhurst and Appelo, 1999; Steefel, 2009; Yeh et al., 2004). Multiphase flow is based on broad experiences in reservoir engineering research, including the thermodynamic modeling of complex phase behavior. In particular, the equations of state were used to simulate

\* Corresponding author. E-mail address: irina.sin@mines-paristech.fr (I. Sin). and study interfacial tension, gas, steam and alkaline injection in oil reservoirs and enhanced oil recovery (Delshad et al., 2000; Farajzadeh et al., 2012; Nghiem et al., 2004; Wang et al., 1997)..

This work aims to incorporate a compressible multiphase flow module into an existing reactive transport simulator. Our coupling method should therefore meet the following requirements:

- 1. The new approach should handle the different complex multiphase chemical models and retain the general paradigm of a multiphase flow module independent of the geochemical system and conserve the conventional reactive transport structure;
- The number of mass conservation nonlinear equations arising from the flow module should be minimized such that the reduced flow system preserves the matrix structure and minimizes the computational intensity;
- 3. The entire framework should preserve its flexibility for possible non-isothermal, geomechanical and domain decomposition developments in the future.

Reactive transport methods have been extensively investigated over the past two decades (see below). This work focuses on the coupling between multicomponent multiphase flow (MMF<sup>1</sup>) and

http://dx.doi.org/10.1016/j.advwatres.2016.11.014

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 $<sup>^{1}</sup>$  The nomenclature is provided in Table 1. The abbreviations are detailed in Table 2.

Table 1	
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Nomenclature.

Latin symbols		
$a_k$	activity of potential catalyzing or inhibiting species	
$A_s$	specific surface area, $[m^2/m^3 \text{ solution}]$ or $[m^2/kg \text{ mineral}]$	
C <sub>l, k</sub>	total liquid mobile concentration of basis species k, [mol/kgw]	
C <sub>s, k</sub>	immobile concentration of basis species $k$ , $[mol/kgw]$	
Cg, m	gas concentration of basis species $m$ , $[mol/m^3]$	
C <sub>i</sub>	concentration of primary species <i>i</i> in chemical module	
d dt	dissolution parameter of transport model	
נו ח	time step molecular diffusion coefficient of phase $\alpha$ [ $m^2/s$ ]	
$D^{e}_{\alpha}$	effective diffusion coefficient of phase $\alpha$ , $[m^2/s]$	
$D_{\alpha}^{\alpha}$	diffusion-dispersion tensor of fluid phase $\alpha$	
е	evaporation parameter of transport model	
$f_i^{\alpha}$	fugacity of species $i$ in phase $\alpha$	
F	residual function	
g	gravitational acceleration vector, [ <i>m</i> /s <sup>2</sup> ]	
<b>J</b> <i>v</i>	Jacopian	
K kum	kinetic rate constant in $[mol/m^2/s]$	
$k_{m}^{fl}$	maximum number of iterations in flow coupling	
$k_{\rm max}^{\rm rt}$	maximum number of iterations in reactive transport coupling	
$k_{r\alpha}$	relative permeability of phase $\alpha$	
Κ	intrinsic permeability, [m <sup>2</sup> ]	
K	intrinsic permeability tensor, [m <sup>2</sup> ]	
K <sub>i</sub>	K-value/equilibrium ratio	
K <sub>j</sub>	equilibrium constant of reaction <i>j</i>	
Ks Kh	Henry's law constant	
M M	molar mass of species [kg/mol]	
n <sub>a</sub>	quantity of matter in phase $\alpha$	
n	normal vector	
N <sub>c</sub>	number of primary species in chemistry module	
$N_f$	number of fluid phases $\alpha$	
Ng	number of gas species	
N <sub>kin</sub>	number of kinetic reactions	
N <sub>Nit</sub>	number of Picard iterations	
Nn	number of phases	
N <sub>r</sub>	number of independent chemical reactions	
Ns	number of species in chemistry module	
$p_{\alpha}$	liquid/gas pressure, [Pa]	
P	pressure, [Pa]	
$\mathbf{P}_{c}$	set of the children pressures mass source term of phase $\alpha$ [kg/s]	
α α <sub>α k</sub>	mass source term of species k in phase $\alpha$ . [kg/s]	
$q_{g,m}$	source term of basis species m in the gas phase, $[mol/m^3]$	
$q_{l, k}$	source term of basis species k in the liquid phase, [mol/kgw]	
Qs	ion activity product	
$r_{\alpha\beta}$	reaction term of phases $\alpha$ and $\beta$ in $\alpha$ transport operator	
R	gas constant, []/K/mol]	
$R_{\alpha}$	reaction term of species k in phase $\alpha$ [kg/s]	
$R_{\alpha, \kappa}$	reaction term of basis species m in the gas phase. $[mol/m^3]$	
$R_{l, k}$	reaction term of basis species $k$ in the liquid phase, $[mol/kgw]$	
R	geochemical reaction operator	
Sj	concentration of species <i>j</i> in chemical module	
Sα	saturation of phase $\alpha$	
t t	calculation time of entire system per time step	
t <sub>fl</sub>	calculation time of flow coupling per iteration	
t <sub>ot</sub>	calculation time of gas transport operator per iteration	
t <sub>rtc</sub>	calculation time of reactive transport coupling per iteration	
Т	temperature, °C and K	
$T_i$	total concentration in chemistry module	
$T_c$	set of the critical temperatures	
$I_{\alpha}$	transport operator of phase $\alpha$	
$u_{\alpha}$	Darcy's velocity of phase $\alpha$	
v V~	volume of porous space occupied by phase $\alpha$ [ $m^3$ ]	
V <sub>tot</sub>	total volume, [m <sup>3</sup> ]	
x <sub>i</sub>	mole fraction of basis species <i>i</i> in the liquid phase	
$X_{\alpha, k}$	mass fraction of basis species $k$ in phase $\alpha$	
x	vector of primary variables of the flow system	
$y_i$	mole fraction of basis species $i$ in the gas phase	

Table 1 (continued)

Latin symbols	
$Z_{c}$	compressibility factor set of the critical compressibility factors
Greek symbols	
$\alpha = \{l, g\}$ $\alpha_{ij}$ $\gamma_j$ $\Delta$ $\varepsilon_g$ $\varepsilon_{Nf}$ $\varepsilon_{qss}$ $\varepsilon_{rt}$ $\mu_{\alpha}$ $\rho_{\alpha}^{\alpha}$ $\rho_{\alpha}^{\alpha}$ $\tau_{\alpha}$ $\phi$ $\psi_{\alpha}$ $\Omega$ $\Sigma_{\alpha}$	liquid/gas phase stoichiometric coefficient activity coefficient matrix of binary interaction coefficients of PR EOS gas quantity tolerance in reactive transport coupling residual function tolerance in flow coupling quasi-stationary state tolerance in flow coupling tolerance in reactive transport coupling viscosity of phase $\alpha$ , $[Pa \cdot s]$ mass density of phase $\alpha$ , $[kg/m^3]$ density of phase $\alpha$ in the gravity term, $[kg/m^3]$ tortuosity of phase $\alpha$ porosity fugacity coefficient of species <i>i</i> in phase $\alpha$ volumetric rate of phase $\alpha$ , $[m^3/s]$ acentric factor set mathematical transport operator of phase $\alpha$
$\ \cdot\ _{\infty}$ $\mathbb{1}_{\mathbb{R}_{>0}}(\cdot)$	infinity norm indicator function of the set of strictly positive real numbers

Table 2

Abbreviations.

AIM	adaptive implicit method
CFL	Courant-Friedrichs-Lewy number
DAE	differential algebraic equations based method
DSA	direct substitution approach
EOS	equation of state
FIM	fully implicit method
FVM	finite volume method
GIA	global implicit approach
IMPEC	implicit pressure/explicit concentration
MMF	multiphase multicomponent flow
MMRF	multiphase multicomponent reactive flow
ODE	ordinary differential equations based method
PDE	partial differential equation
OSA	operator splitting approach
RT	reactive transport
SI	saturation index
SIA	sequential iterative approach
SNIA	sequential non-iterative approach
TPFA	two-point flux approximation

reactive transport (RT) modules and starts by surveying the existing approaches

1.2. A review of multiphase multicomponent flow and reactive transport codes

#### 1.2.1. Operator splitting algorithms between MMF and RT

The strength of the operator-splitting approach (OSA) (sequential iterative (SIA) or sequential non-iterative (SNIA)) arises from the framework flexibility, which allows each model to be developed and verified independently. These are important reasons for selecting the OSA for the coupling between MMF and RT, particularly when extending a hydrogeochemical code from singleto two-phase flow. The following codes apply the OSA: Code-Bright (Olivella et al., 1996) (coupling with the reactive transport code RETRASO (Saaltink et al., 2004)), DuMu<sup>X</sup> (based on DUNE) (Ahusborde et al., 2015; Vostrikov, 2014), DUNE (Hron et al., 2015), HYDROGEOCHEM (unsaturated) (Yeh et al., 2004, 2012), iCP (Nardi et al., 2014), IPARS (Peszynska and Sun, 2002; Wheeler et al., 2012), MIN3P (the bubble model) (Mayer et al., 2012; Molins and Mayer, 2007), MORES (Farajzadeh et al., 2012; Wei, 2012), NUFT (Hao et al., 2012), PFLOTRAN (Lichtner et al., 2015; Lu and Lichtner, 2007), Download English Version:

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