## Accepted Manuscript

Outer Inverses and Jacobi Type Identities

Ravindra B. Bapat, Manjunatha Prasad Karantha, Nupur Nandini, Divya P. Shenoy


| PII: | S0024-3795(17)30559-1 |
| :--- | :--- |
| DOI: | https://doi.org/10.1016/j.laa.2017.09.025 |
| Reference: | LAA 14331 |

To appear in: Linear Algebra and its Applications

Received date: 24 April 2017
Accepted date: 20 September 2017

Please cite this article in press as: R.B. Bapat et al., Outer Inverses and Jacobi Type Identities, Linear Algebra Appl. (2017), https://doi.org/10.1016/j.laa.2017.09.025

This is a PDF file of an unedited manuscript that has been accepted for publication. As a service to our customers we are providing this early version of the manuscript. The manuscript will undergo copyediting, typesetting, and review of the resulting proof before it is published in its final form. Please note that during the production process errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

# Outer Inverses and Jacobi Type Identities 

Ravindra B. Bapat ${ }^{\text {a }}$, Manjunatha Prasad Karantha ${ }^{\text {b,1,* }}$, Nupur Nandini ${ }^{\text {b,2 }}$, Divya P. Shenoy ${ }^{\text {b,c }}$<br>${ }^{a}$ Theoretical Statistics and Mathematics Unit, Indian Statistical Institute Delhi Center, 7, SJS Sansanwal Marg, New Delhi 100 016. India<br>${ }^{b}$ Department of Statistics, Manipal University, Manipal, 576 104. India<br>${ }^{c}$ Department of Mathematics, Manipal Institute of Technology, Manipal University, Manipal, 576 104. India


#### Abstract

We consider matrices over a commutative ring and characterize the class of outer inverses for which Jacobi type identities can be extended. We obtain a necessary and sufficient condition for the existence of Rao-regular Drazin inverse in terms of sum of principal minors of $A^{k}$ for some $k$. Also, we obtain determinantal formula for the Rao-regular Drazin inverse. Conjectures are formulated which give expressions for outer inverse and the conjectures are proved in some special cases.


Keywords: matrices over commutative ring, outer inverse, generalized inverse, Rao-regular matrix, Jacobi identity, determinantal formula 2010 MSC: 15A09, 06A06, 16D25

## 1. Preliminaries

Jacobi identity relates any minor of $A^{-1}$, the inverse of matrix $A$, with determinant $|A|$ and the complementary minor in transpose of $A$. Several extensions have been attempted by several authors, when the matrix $A$ is singular and

[^0]
# https://daneshyari.com/en/article/5773040 

Download Persian Version:
https://daneshyari.com/article/5773040

## Daneshyari.com


[^0]:    *Corresponding author
    Email addresses: rbb@isid.ac.in (Ravindra B. Bapat), kmprasad63@gmail.com; km.prasad@manipal.edu (Manjunatha Prasad Karantha), n.nandini048@gmail.com (Nupur Nandini ), divyaanooppai@gmail.com (Divya P. Shenoy)
    ${ }^{1}$ Author acknowledge the support by "Science and Engineering Research Board (DST, Govt. of India)" under Extra Mural Research Funding Scheme (SR/S4/MS:870/14).
    ${ }^{2}$ Author acknowledge the support of Manipal University through Dr. TMA Pai Ph.D. Scholarship Fellowship.

