

Semiclassical ground states for quasilinear Schrödinger equations with three times growth*

Hui Zhang^{1†}, Fubao Zhang²

1. Department of Mathematics, Jinling Institute of Technology,
Nanjing 211169, China

2. Department of Mathematics, Southeast University, Nanjing 210096, China

Abstract: In this paper, we study the quasilinear Schrödinger equation

$$-\epsilon^2 \Delta u + V(x)u - \epsilon^2 u \Delta(u^2) = Q(x)u^3, \quad u \in H^1(\mathbb{R}^3),$$

where $\epsilon > 0$ is a parameter, V and Q are positive bounded functions. For the equation with three times growth, we establish the existence of ground states for ϵ small using the method of Nehari manifold. We also describe the concentration phenomena of ground states as $\epsilon \rightarrow 0$.

Keywords: Quasilinear Schrödinger equation; Concentration; Nehari manifold; Semiclassical state.

1 Introduction and main results

As models of physical phenomena, quasilinear Schrödinger equations of the form

$$i\epsilon \partial_t z = -\epsilon^2 \Delta z + W(x)z - l(x, |z|^2)z - \kappa \epsilon^2 \Delta h(|z|^2)h'(|z|^2)z, \quad (1.1)$$

have been extensively studied in recent years, where $z : \mathbb{R} \times \mathbb{R}^N \rightarrow \mathbb{C}$, $W : \mathbb{R}^N \rightarrow \mathbb{R}$ is a given potential, ϵ is a positive parameter, $l, h : \mathbb{R}^+ \rightarrow \mathbb{R}$ are suitable functions, and κ is a real constant. For example, $\kappa = 0$, corresponding to semilinear Schrödinger equations, which has been widely investigated, we refer the readers to [2, 20, 24]. The case $h(s) = s$, as a model of the time evolution of the condensate wave function in super-fluid film, has been studied by Kurihara in [16]. While for $h(s) = \sqrt{1+s}$, the equations are the models of the self-channeling of a high-power ultra short laser in matter.

Here we are interested in the case $h(s) = s$ and $\kappa = 1$. Looking for standing wave solutions of (1.1), that is, solutions of the form

$$z(t, x) = e^{-iEt} u(x), \quad E \in \mathbb{R},$$

*The work was supported by the National Natural Science Foundation of China (Nos. 11601204, 11671077, 11571140), the Natural Science Foundation of Jiangsu Province (No. BK20140106), the Natural Science Foundation of Outstanding Young Scholars of Jiangsu Province (No: BK20160063) and the Research Foundation of Jinling Institute of Technology (No. jit-gjfh-201501).

[†]Correspondence: Hui Zhang, Department of Mathematics, Jinling Institute of Technology, Nanjing 211169, China. Email: huihz0517@126.com

Download English Version:

<https://daneshyari.com/en/article/5774550>

Download Persian Version:

<https://daneshyari.com/article/5774550>

[Daneshyari.com](https://daneshyari.com)