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## Regularization of an inverse nonlinear parabolic problem with time-dependent coefficient and locally Lipschitz source term

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## Abstract

We consider a backward problem of finding a function u satisfying a nonlinear parabolic equation in the form  $u_t + a(t)Au(t) = f(t, u(t))$  subject to the final condition  $u(T) = \varphi$ . Here A is a positive self-adjoint unbounded operator in a Hilbert space H and f satisfies a locally Lipschitz condition. This problem is ill-posed. Using quasi-reversibility method, we shall construct a regularized solution  $u_{\varepsilon}$  from the measured data  $a_{\varepsilon}$  and  $\varphi_{\varepsilon}$ . We show that the regularized problems are well-posed and that their solutions converge to the exact solutions. Error estimates of logarithmic type are given and a simple numerical example is presented to illustrate the method as well as verify the error estimates given in the theoretical parts.

**Keywords and phrases:** Nonlinear parabolic problem, Backward problem, Quasi-reversibility, Ill-posed problem, Contraction principle.

Mathematics subject Classification 2000: 35K05, 35K99, 47J06, 47H10.

## 1. Introduction

Let  $(H, \|\cdot\|)$  be a Hilbert space with the inner product  $\langle \cdot, \cdot \rangle$ . Let *A* be a positive self-adjoint operator defined on a dense subspace  $D(A) \subset H$  such that -A generates a compact contraction semi-group S(t) on *H*. Let  $f : [0, T] \times H \to H$  satisfy the locally Lipschitz condition: for each M > 0, there exists k(M) > 0 such that

$$\|f(t,u) - f(t,v)\| \le k(M) \|u - v\| \text{ if } \max\{\|u\|, \|v\|\} \le M.$$
(1)

We shall consider a backward problem of finding a function  $u : [0, T] \rightarrow H$  such that

$$u_t + a(t)Au(t) = f(t, u(t)), \quad 0 < t < T,$$
  
$$u(T) = \varphi, \tag{2}$$

where  $a \in C([0, T])$  is a given real-valued function and  $\varphi \in H$  is a prescribed final value.

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