

Riesz-type inequalities for conjugate differential forms

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Abstract

We prove boundary inequalities for conjugate differential forms in C^1 -domains. They extend the classical Riesz inequalities for conjugate harmonic functions.

Keywords:

Riesz inequalities, harmonic forms, conjugate differential forms, potentials on C^1 -domains

1. Introduction

The following inequality due to M. Riesz [12], involving the real and the imaginary part of holomorphic functions of one complex variable, is very well known:

$$\|g\|_{L^p(S)} \leq C\|f\|_{L^p(S)}, \quad (1.1)$$

($1 < p < \infty$) the function $f + ig$ being holomorphic in the unit disc D , continuous up to the boundary $S = \partial D$, and $g(0) = 0$. Inequality (1.1) plays a key role in harmonic analysis.

Another inequality related to (1.1) concerns normal derivative $\frac{\partial}{\partial \nu}$ and tangential gradient $\text{grad}_{\partial\Omega}$ of a harmonic function defined on a sufficiently smooth bounded domain $\Omega \subset \mathbb{R}^n$. Namely, we have

$$\left\| \frac{\partial \omega}{\partial \nu} \right\|_{L^p(\partial\Omega)} \leq C \|\text{grad}_{\partial\Omega} \omega\|_{L^p(\partial\Omega)}, \quad (1.2)$$

for any harmonic function $\omega \in C^1(\overline{\Omega}) \cap C^2(\Omega)$. Inequality (1.2) was proved by Vishik [18] for $p = 2$ when $\partial\Omega$ is a sphere, conjectured by Mikhlin in [11,

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