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## Approximations for finite-time ruin probability in a dependent discrete-time risk model with CMC simulations

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#### Abstract

Consider a discrete-time risk model in which the insurer is allowed to invest its wealth into a risk-free or a risky portfolio under a certain regulation. Then the insurer is said to be exposed to a stochastic economic environment that contains two kinds of risks, the insurance risk and financial risk. Within period i, the net insurance loss is denoted by  $X_i$  and the stochastic discount factor from time i to zero is denoted by  $\theta_i$ . For any integer n, assume that  $X_1, \ldots, X_n$  form a sequence of pairwise asymptotically independent but not necessarily identically distributed real-valued random variables with distributions  $F_1, \ldots, F_n$ , respectively;  $\theta_1, \theta_2, \ldots, \theta_n$  are another sequence of arbitrarily dependent nonnegative random variables; and the two sequences are mutually independent. Under the assumption that the average distribution  $n^{-1} \sum_{i=1}^n F_i$  is dominatedly varying tailed and some moment conditions on  $\theta_i$ ,  $i = 1, \ldots, n$ , we derive a weakly equivalent formula for the finite-time ruin probability. We demonstrate our obtained results through a Crude Monte-Carlo simulation with asymptotics.

**Keywords:** Discrete-time risk model with insurance and financial risks; Pairwise asymptotical independence; Dominated variation; Ruin probability; Crude Monte-Carlo simulation

AMS Subject Classification: 62P05; 62E10; 91B30

## 1 Introduction

Consider a discrete-time risk model, in which within period  $i \ge 1$ , an insurer's net loss (the aggregate claim amount minus the total premium income) is denoted by a real-valued random variable (r.v.)  $X_i$  with distribution  $F_i$ ; the stochastic discount factor (the reciprocal of the stochastic return rate) from time *i* to zero is denoted by a nonnegative r.v.  $\theta_i$ ; and assume that  $\{X_i, i \ge 1\}$ obey some certain dependence structure,  $\{\theta_i, i \ge 1\}$  are arbitrarily dependent, but  $\{X_i, i \ge 1\}$ and  $\{\theta_i, i \ge 1\}$  are mutually independent. In particular, the stochastic discount factors can be specialized to a product of some independent and identically distributed (i.i.d.) nonnegative r.v.s,

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