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General approach to constructing optimal multipoint families of iterative methods using Hermite's rational interpolation¹

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Abstract

We discuss accelerating convergence of multipoint iterative methods for solving scalar equations, using particular type rational interpolant. Both derivative-free and Newton-type methods are investigated simultaneously. As a conclusion a Theorem of König's type for multipoint iterations is stated. A new optimal multipoint family of methods based on rational interpolation is constructed. The iteration uses n function evaluations per cycle and $\mathcal{O}(j)$ operations in j-th step of a single iteration to obtain 2^{n-1} order of convergence. Several equivalent forms of the obtained iterates and development techniques are presented.

 $\mathrm{MSC}{:}\ 65\mathrm{H05}$

Keywords: Iterative methods, Nonlinear equations, Hermite Rational Interpolation, Divided difference.

1. Introduction

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Multipoint methods are among the most efficient tools in approximating a single root of a nonlinear equation by iterative means. The search for reliable methods to construct these powerful root-finders is very intensive and has increased over the years. For details and relevant references, the reader is re-

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