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Jin Zhang, Xiaowei Liu

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### ACCEPTED MANUSCRIPT

## Supercloseness of the continuous interior penalty method for singularly perturbed problems in 1D: vertex-cell interpolation $\stackrel{\Leftrightarrow}{\sim}$

Jin Zhang<sup>a,\*</sup>, Xiaowei Liu<sup>b,1</sup>

<sup>a</sup>School of Mathematics and Statistics, Shandong Normal University, Jinan 250014, China <sup>b</sup>College of Science, Qilu University of Technology, Jinan 250353, China

### Abstract

A continuous interior penalty method with piecewise polynomials of degree  $p \geq 2$  is applied on a Shishkin mesh to solve a singularly perturbed convection– diffusion problem, whose solution has a single boundary layer. This method is analyzed by means of a series of integral identities developed for the convection terms. Then we prove a supercloseness bound of order 5/2 for a vertex-cell interpolation when p = 2. The sharpness of our analysis is supported by some numerical experiments. Moreover, numerical tests show supercloseness clearly for  $p \geq 3$ .

*Keywords:* Singular perturbation, Convection–diffusion equation, Continuous interior penalty method, Shishkin mesh, Supercloseness

#### 1. Introduction

We consider the following two-point boundary value problem

$$-\varepsilon u'' + b(x)u' + c(x)u = f(x) \quad \text{in } \Omega := (0, 1),$$
  
$$u(0) = u(1) = 0,$$
  
(1)

with a positive parameter  $\varepsilon$  and sufficiently smooth functions b, c and f. There exist constants  $\beta$  and  $\mu$  such that

$$b(x) > \beta > 0, \quad c(x) - \frac{1}{2}b'(x) \ge \mu > 0 \quad \text{for } x \in [0, 1],$$
 (2)

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<sup>\*</sup>Corresponding author: jinzhangalex@hotmail.com

<sup>&</sup>lt;sup>1</sup>Email: xwliuvivi@hotmail.com

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