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### **ACCEPTED MANUSCRIPT**

## On boundedness of four-dimensional Hausdorff matrices on the double Taylor sequence spaces

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#### Abstract

In this paper, we introduce the double Taylor sequence space  $\mathcal{T}_p^{r,s}$  consisting of all sequences whose doubly Taylor transforms of orders r, s are in the space  $\mathcal{L}_p$  of non-absolute type which is a Banach space including the space  $\mathcal{L}_p$ . Further, some inclusion relations concerning the space  $\mathcal{T}_p^{r,s}$  are given. Then, we focus on the evaluation of the exact values of the operator norm and lower bound of four-dimensional Hausdorff matrices as operators mapping the double sequence space  $\mathcal{L}_p$  into the double Taylor sequence spaces  $\mathcal{T}_p^{r,s}$ . Some estimates are obtained. In particular, we apply our results to some special cases of four-dimensional Hausdorff matrices, such as Cesáro, Euler, Hölder and Gamma matrices.

Keywords: Double sequences, Matrix domain, Four-dimensional Hausdorff matrices, Operator norm and lower bound.

2000 MSC: 46A45, 26D15.

## 1. Introduction

By  $\Omega$ , we denote the space of all real or complex valued double sequences which is the vector space with coordinatewise addition and scalar multiplication. Any vector subspace of  $\Omega$  are called as the double sequence space. The space of bounded double sequences is denoted by  $\mathcal{L}_{\infty}$ , which is a Banach space with the norm  $\|x\|_{\mathcal{L}_{\infty}} = \sup_{n,m} |x_{n,m}|$ . Also the space  $\mathcal{L}_p$  of double sequences [7] is defined by

$$\mathcal{L}_p = \left\{ (x_{n,m}) \in \Omega : \sum_{n=0}^{\infty} \sum_{m=0}^{\infty} |x_{n,m}|^p < \infty \right\}, \ (0 < p < \infty).$$

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