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Lindsay T. Keegan, Jonathan Dushoff



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# Estimating Finite-Population Reproductive Numbers in Heterogeneous Populations

Lindsay T. Keegan<sup>a,1</sup>, Jonathan Dushoff<sup>b</sup>

<sup>a</sup>615 North Wolfe St  
The Johns Hopkins University  
Bloomberg School of Public Health  
Baltimore, Maryland, USA

<sup>b</sup>1280 Main Street West  
McMaster University  
Hamilton, Ontario, Canada

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## Abstract

The basic reproductive number,  $\mathcal{R}_0$ , is one of the most important epidemiological quantities.  $\mathcal{R}_0$  provides a threshold for elimination and determines when a disease can spread or when a disease will die out. Classically,  $\mathcal{R}_0$  is calculated assuming an infinite population of identical hosts. Previous work has shown that heterogeneity in the host mixing rate increases  $\mathcal{R}_0$  in an infinite population. However, it has been suggested that in a finite population, heterogeneity in the mixing rate may actually *decrease* the finite-population reproductive numbers. Here, we outline a framework for discussing different types of heterogeneity in disease parameters, and how these affect disease spread and control. We calculate “finite-population reproductive numbers” with different types of heterogeneity, and show that in a finite population, heterogeneity has complicated effects on the reproductive number. We find that simple heterogeneity *decreases* the finite-population reproductive number, whereas heterogeneity in the intrinsic mixing rate (which affects both infectiousness and susceptibility) *increases* the finite-population reproductive number when  $\mathcal{R}_0$  is small relative to the size of the population and *decreases* the finite-population reproductive number when  $\mathcal{R}_0$  is large relative to the size of the population. Although heterogeneity has complicated effects on the finite-population reproductive numbers, its implications for control are straightforward: when  $\mathcal{R}_0$  is large relative to the size of the population, heterogeneity decreases the finite-population reproductive numbers, making disease control or elimination easier than predicted by  $\mathcal{R}_0$ .

*Keywords:* Basic Reproductive Number, Heterogeneity, Super-spreaders

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## 1. Introduction

The effect of heterogeneity on disease dynamics is a foundational question in infectious disease modeling. Recently, renewed attention has been given to the impact of heterogeneity on the basic reproductive number,  $\mathcal{R}_0$  (31; 45; 36).  $\mathcal{R}_0$  is the average number of secondary infections from a single infectious individual in an otherwise totally susceptible

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*Email address:* keeganlt@mcmaster.ca (Lindsay T. Keegan )

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