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Hybrid techniques based on solving reduced problem instances for a longest common subsequence problem



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ABSTRACT

Finding the longest common subsequence of a given set of input strings is a relevant problem arising in various practical settings. One of these problems is the so-called longest arc-preserving common subsequence problem. This NP-hard combinatorial optimization problem was introduced for the comparison of arc-annotated ribonucleic acid (RNA) sequences. In this work we present an integer linear programming (ILP) formulation of the problem. As even in the context of rather small problem instances the application of a general purpose ILP solver is not viable due to the size of the model, we study alternative ways based on model reduction in order to take profit from this ILP model. First, we present a heuristic way for reducing the model, with the subsequent application of an ILP solver. Second, we propose the application of an iterative hybrid algorithm that makes use of an ILP solver for generating high quality solutions at each iteration. Experimental results concerning artificial and real problem instances show that the proposed techniques outperform an available technique from the literature.

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1. Introduction

In computer science terms, a *string* (or sequence) *x* of length l_x is a finite sequence of characters from a finite alphabet Σ . In fact, strings are popular data types for representing and storing information. Words and even complete texts, for example, may be stored in a computer in terms of strings. However strings are not only useful in fields such as information and text processing. They arise, in particular, in the field of computational biology. The reason is that most of the genetic instructions involved in the growth. development, functioning and reproduction of living organisms are stored by means of deoxyribonucleic acid (DNA) and ribonucleic acid (RNA) molecules, which are either double-stranded (DNA) or single-stranded (RNA) sequences of nucleotides. In short, each nucleotide is composed of a nitrogenous base, a five-carbon sugar (ribose or deoxyribose), and at least one phosphate group. Concerning RNA, each nucleotide has one of four different nitrogenous bases: guanine (G), uracil (U), adenine (A), and cytosine (C). As a consequence, any RNA molecule can be represented as a string of symbols from $\Sigma = \{G, U, A, C\}$, which is called the *primary struc*ture of a RNA molecule. The primary structure of a RNA molecule is

https://doi.org/10.1016/j.asoc.2017.10.005 1568-4946/© 2017 Elsevier B.V. All rights reserved. a simplified representation, because RNA molecules fold in space and different nucleotides bind together, for example, by means of hydrogene bonds. Generally, guanine (G) can only bind with cytosine (C) and uracil (U) can only bind with adenine (A). These hydrogene bonds are present in the so-called *secondary structure* of an RNA molecule; see Fig. 1a for an example.

For computer science purposes, the hydrogene bonds of the secondary structure of an RNA sequence *x* can be represented by a so-called arc annotation set P_x . In technical terms, P_x is an unordered set of pairs of positions of a string x.¹ Each pair $(i_1, i_2) \in P_x$ represents an arc between positions i_1 and i_2 and is called an arc *annotation*. The only convention is that $i_1 < i_2$ must hold for any arc $(i_1, i_2) \in P_x$. Finally, i_1 is called the *left endpoint* of arc (i_1, i_2) , and i_2 is called the *right endpoint*. A pair (x, P_x) is called an *arc-annotated* sequence [2] (or arc-annotated string). Given this definition, note that the secondary structure of an RNA sequence can conveniently be described by an arc-annotated sequence; see Fig. 1b for an example. In fact, arc-annotated sequences have been widely used for this purpose (see, for example, [3]). In particular, arc-annotated sequences have shown to be useful for the structural comparison of RNA sequences. One of the usual measures when comparing two (or more) sequences is the length of their longest common subsequence

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¹ As a convention, the positions of a string *x* range from 1 to l_x .

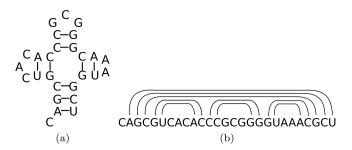


Fig. 1. (a) Example of the secondary structure of an RNA molecule. (b) The corresponding arc-annotated sequence. The example is reproduced from [1].

Table 1

NP-hard cases of the LAPCS problem. The first two table columns indicate the characterizations of the two input strings, without any order.

First characterization	Second characterization	Complexity
UNLIMITED	UNLIMITED	NP-hard [2,9]
UNLIMITED	CROSSING	NP-hard [2,9]
UNLIMITED	NESTED	NP-hard [2,9]
UNLIMITED	CHAIN	NP-hard [2,9]
UNLIMITED	PLAIN	NP-hard [13]
CROSSING	CROSSING	NP-hard [2,9]
CROSSING	NESTED	NP-hard [2,9]
CROSSING	CHAIN	NP-hard [2,9]
CROSSING	PLAIN	NP-hard [13]
NESTED	NESTED	NP-hard [13]
STEM	STEM	NP-hard [14]

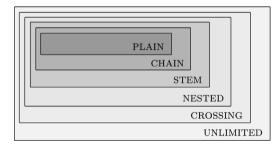


Fig. 2. Hierarchy of different classifications of arc-annotated sequences.

(LCS); see, for example, [4,5]. In this context, given a sequence x over a finite alphabet Σ , sequence t is called a *subsequence* of x, if t can be produced from x by deleting characters. Given a set of input strings $\{s_1, \ldots, s_n\}$, the problem of finding the longest commons subsequence of all input strings is, in general, NP-hard [6]. The best techniques available nowadays for solving this problem are based on beam search [7] (see [8], for example).

1.1. The LAPCS problem

The longest common subsequence problem in the context of arc-annotated sequences—the *longest arc-preserving common subsequence* (LAPCS) problem—has first been introduced in [9,2]. Given two input sequences *x* and *y*, the set of possible *assignments A* is defined as the set of all a_{ij} —where $i \in \{1, ..., l_x\}$ and $j \in \{1, ..., l_y\}$ —such that x[i] = y[j]. In other words, *A* consists of all a_{ij} such that at position *i* of *x* and at position *j* of *y* there is the same letter. A valid common subsequence of the two input sequences *x* and *y* can then be represented by a subset $S \subseteq A$ that fulfills the following conditions:

Table 2

Polynomially solvable cases of the LAPCS problem. The first two table columns indicate the characterizations of the two input strings, without any order.

First characterization	Second characterization	Complexity
NESTED	CHAIN	<i>O</i> (<i>nm</i> ³) [15,1]
NESTED	PLAIN	$O(nm^3)$ [15,1]
CHAIN	CHAIN	$O(nm^3)$ [15,1]
CHAIN	PLAIN	<i>O</i> (<i>nm</i>) [2,9]
PLAIN	PLAIN	<i>O</i> (<i>nm</i>) [11]

• **Common subsequence condition:** For any two assignments $a_{i,j}$, $a_{k,l} \in S$ (where $a_{i,j} \neq a_{k,l}$) it must hold that either i < k and j < l, or i > k and j > l.

In order to translate such a solution into the corresponding common subsequence, the assignments in *S* have to be ordered from small to large indices, either according to the first or the second index. Then, the letters corresponding to the assignments must be joined in this order.

A solution *S* that fulfills the common subsequence condition is called *arc-preserving* if the arcs induced by the solution are preserved:

 Arc preservation condition: for any two assignments a_{i,j}, a_{k,l} ∈ S (where a_{i,j} ≠ a_{k,l} and i < k) it must hold that (i, k) ∈ P_x ⇔ (j, l) ∈ P_y.

Given two arc-annotated input strings (x, P_x) and (y, P_y) , the LAPCS problem consists in finding a solution $S \subseteq A$ that fulfills both the common subsequence and the arc preservation condition and is of maximal cardinality. Note that such a mapping corresponds to the longest arc-preserving common subsequence of x and y.

In practice, the nature of the arc annotation in the context of RNA sequences generally satisfies some conditions. Given an arcannotated string (x, P_x), the relative positioning of two arcs (i_1 , i_2)

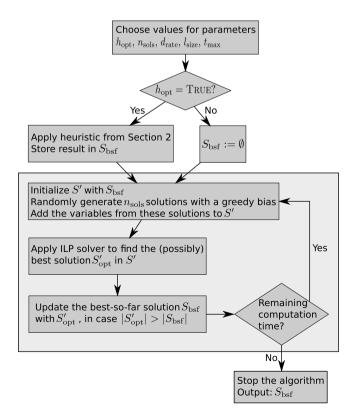


Fig. 3. Flow diagram of HyB-ALG (see also Algorithm 1).

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