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Optimal trajectory planning for trains under fixed and moving signaling systems using mixed integer linear programming



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ABSTRACT

The optimal trajectory planning problem for multiple trains under fixed block signaling systems and moving block signaling systems is considered. Two approaches are proposed to solve this optimal control problem for multiple trains: the greedy approach and the simultaneous approach. In each solution approach, the trajectory planning problem is transformed into a mixed integer linear programming (MILP) problem. In particular, the objective function considered is the energy consumption of trains and the nonlinear train model is approximated by a piece-wise affine model. The varying line resistance, variable speed restrictions, and maximum traction force, etc. are also included in the problem definition. In addition, the constraints caused by the leading train in a fixed or moving block signaling system are first discretized and then transformed into linear constraints using piecewise affine approximations resulting in an MILP problem. Simulation results comparing the greedy MILP approach with the simultaneous MILP approach show that the simultaneous MILP approach yields a better control performance but requires a higher computation time. Moreover, the performance of the proposed greedy and the proposed simultaneous MILP approach is also compared with that of the greedy and the simultaneous pseudospectral method, where the pseudospectral method is a state-of-the-art method for solving optimal control problems. The results show that the energy consumption and the end time violations of the greedy MILP approach are slightly larger than those of the greedy pseudospectral method, but the computation time is one to two orders of magnitude smaller. The same trend holds for the simultaneous MILP approach and the simultaneous pseudospectral method.

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1. Introduction

Nowadays, the energy efficiency of transportation systems is becoming more and more important because of the rising energy prices and environmental concerns. Rail traffic plays a significant role for the sustainability for transportation systems, since it can provide safe, fast, punctual, and comfortable services (Peng, 2008). The reduction of energy consumption is one of the key objectives of railway systems because energy consumption is one of the major expenses in operational cost, which is about 13–16% of the annual operation and maintenance cost of railway systems in China (Ding, Bai, Liu, & Mao, 2009). Therefore, even a small improvement in energy saving is attractive to the railway operators since it can save a large amount of money. Some driver

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assistance systems have been developed to assist drivers to drive the train optimally, such as FreightMiser (Howlett & Pudney, 1995), Metromiser (Howlett & Pudney, 1995), and driving style manager (Franke, Meyer, & Terwiesch, 2002). With the development of modern railway systems, an automatic train operation system plays a key role in ensuring accurate stopping, operation punctuality, energy saving, and riding comfort (Peng, 2008). The railway control center or automatic train operation systems are responsible for solving the trajectory planning problems based on the information collected by train monitoring systems, such as line resistance, speed limits, maximum traction and braking forces.

In the literature, the research on the optimal control of train operations began in the 1960s and is aimed at solving the trajectory planning problem for a train running from one station to another. Since it has significant effects for energy saving, punctuality, etc., various approaches were proposed for the trajectory planning problem. These approaches can be grouped into two main categories: analytical solutions and numerical optimization. For analytical solutions, the maximum principle is applied and it results in four optimal regimes (i.e., maximum traction, cruising, coasting, and maximum braking) (Howlett,

2000; Howlett, Milroy, & Pudney, 1994; Khmelnitsky, 2000; Liu & Golovicher, 2003). It is difficult to obtain the analytical solution if more realistic conditions are considered as these introduce more complex nonlinear terms into the model equations and the constraints (Ko, Koseki, & Miyatake, 2004). Numerical optimization approaches are applied more and more to the train optimal control problem due to the increasing computing power nowadays. A number of advanced techniques such as fuzzy and genetic algorithms have been proposed to calculate the optimal reference trajectory for trains, see, e.g., Chang and Xu (2000), Chang and Sim (1997), Han et al. (1999), and Ke, Lin, and Lai (2011). But in these approaches, the optimal solution is not always guaranteed to be found. On the other hand, multi-parametric quadratic programming is used in Vařak, Baotić, Perić, and Bago (2009) to calculate the optimal control law for train operations. In that approach, the nonlinear train model with quadratic resistance is approximated by a piecewise affine function. Inspired by Vařak et al. (2009), in Wang, De Schutter, Ning, Groot, and van den Boom (2011) and Wang, De Schutter, van den Boom, and Ning (2013) we proposed to solve the optimal trajectory problem as a mixed integer linear programming (MILP) problem, which can be solved efficiently using existing commercial and free solvers (Atamtürk & Savelsbergh, 2005; Linderoth & Ralphs, 2005) that guarantee finding the global optimum of the MILP problem.

However, the approaches mentioned above ignore the impact caused by the signaling systems, e.g., a fixed block signaling (FBS) system or a moving block signaling (MBS) system. An FBS system is a block system using fixed block sections, which are protected by trackside traffic signals. A train cannot enter a block section until a signal indicates the train may proceed. In an MBS system, the blocks are defined as safe zones around each train in real time. Regular communication between trains and zone controllers is needed for knowing the exact locations and speeds of all trains in that zone at any given time. An MBS system allows trains to run closer together compared with an FBS system, thus increasing the line capacity. Lu and Feng (2011) consider the operation of two trains on a same line and optimize the trajectory of the following train with constraints caused by the leading train in an FBS system. More specifically, a parallel genetic algorithm is used to optimize the trajectories for the leading train and the following train, resulting in a lower energy consumption (Lu & Feng, 2011). Gu, Lu, and Tang (2011) apply nonlinear programming to optimize the trajectory for the following train. Two situations of the leading train, i.e. running and stopped, are studied and the corresponding strategies are proposed for the following train. In addition, Ding et al. (2009) take the constraints caused by the MBS system into account and develop an energy-efficient multi-train control algorithm to calculate the optimal trajectories. Three optimal control regimes, i.e. maximum traction, coasting, and maximum braking, are adopted in the algorithm and the sequences of these three regimes are determined by a predefined logic.

In this paper, the constraints caused by the leading train in an FBS system and an MBS system are formulated. These constraints are discretized and then recast as linear constraints by piecewise affine approximations. Thus, they can be easily included into the MILP problem, which can be solved efficiently compared to the existing approaches. Furthermore, the greedy approach and the simultaneous approach are proposed to solve the trajectory planning problem for multiple trains. We also compare the MILP approach with the state-of-art optimization approach: pseudospectral methods. Over the last decade, pseudospectral methods have risen to prominence in the numerical optimal control area (Elnagar, Kazemi, & Razzaghi, 1995), which were applied to solving optimal control problems (Gong et al., 2007), such as orbit transfers, lunar guidance, magnetic control. Therefore, we have selected the pseudospectral method for the comparison of the case study.

The remainder of this paper is structured as follows. In Section 2, the train model and the MILP approach for a single train are summarized based on Wang et al. (2013). Section 3 introduces the principle of railway signaling systems, i.e. the FBS system and the MBS system. Section 4 formulates the constraints for the following train caused by the leading train under an FBS system and shows how to include these constraints into the MILP formulation. The constraints caused by the MBS system are considered and included in the MILP problem in Section 5. Section 6 illustrates the calculation of the optimal trajectories using the data from Beijing Yizhuang subway line. We conclude with a short discussion of some topics for future work in Section 7.

2. Train model and the MILP approach

In this section, the formulation of the optimal control problem and the MILP approach we proposed in Wang et al. (2013) are summarized.

2.1. Optimal control problem

A continuous-space mass-point model is often used in the literature on train optimal control (Franke, Terwiesch, & Meyer, 2003), which can be described as follows (Liu & Golovicher, 2003):

$$\begin{aligned} m\rho \frac{d\tilde{E}}{ds} &= u(s) - R_b(v) - R_l(s, v), \\ \frac{d\tilde{t}}{ds} &= \frac{1}{\sqrt{2\tilde{E}}}, \end{aligned} \quad (1)$$

where m is the mass of the train, ρ is a factor to consider the rotating mass (Hansen & Pacht, 2008), \tilde{E} is the kinetic energy per mass unit, which is equal to $0.5v^2$, v is the velocity of the train, s is the position of the train, u is the control variable, i.e. the traction or braking force, which is bounded by the maximum traction force u_{\max} and the maximum braking force u_{\min} , so $u_{\min} \leq u(s) \leq u_{\max}$, $R_b(v)$ is the basic resistance including roll resistance and air resistance, and $R_l(s, v)$ is the line resistance caused by track grade, curves, and tunnels. See Wang et al. (2013) for more details.

The kinetic energy per mass unit $\tilde{E} = 0.5v^2$ and time t are chosen as the states and the position s is taken as the independent variable for the train model as in Franke et al. (2003). The trajectory planning problem for trains can then be formulated as (Wang et al., 2011)

$$\begin{aligned} J &= \int_{s_{\text{start}}}^{s_{\text{end}}} \max(0, u(s)) ds \\ \text{s.t.} \\ u_{\min} &\leq u(s) \leq u_{\max}, \\ 0 &< \tilde{E}(s) \leq \tilde{E}_{\max}(s), \\ \tilde{E}(s_{\text{start}}) &= \tilde{E}_{\text{start}}, \quad \tilde{E}(s_{\text{end}}) = \tilde{E}_{\text{end}}, \\ t(s_{\text{start}}) &= 0, \quad t(s_{\text{end}}) = T, \end{aligned} \quad (2)$$

and the train model (1), where the objective function J is the energy consumption without regenerative braking; $\tilde{E}_{\max}(s)$ is equal to $0.5V_{\max}^2(s)$ where $V_{\max}(s)$ is the maximum allowable velocity, which depends on the train characteristics and line conditions, and as such it is usually a piecewise constant function of the coordinate s (Khmelnitsky, 2000; Liu & Golovicher, 2003); s_{start} , $\tilde{E}(s_{\text{start}})$, and $t(s_{\text{start}})$ are the position, the kinetic energy per mass, and the departure time at the beginning of the route; s_{end} , $\tilde{E}(s_{\text{end}})$, and $t(s_{\text{end}})$ are the position, the kinetic energy per mass, and the arrival time at the end of the route, respectively, where the scheduled running time T is given by the timetable or the

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