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New state estimator for decentralized event-triggered consensus for multi-agent systems for multi-agent systems for multi-agent systems $\frac{t}{t}$ are estimator for decenti \mathbf{N} tate estimator for decembr New state estimator for decentralized New state estimator for decentralized event-triggered consensus event-triggered consensus

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reach consensus in multi-agent systems. It proposes an improved agent state estimator as well as an estimator of the state estimation uncertainty to trigger communications. Convergence to consensus is studied. Simulations show the effectiveness of the proposed estimators in presence of state perturbations. Abstract: This paper extends recent work of Garcia *et al.* on event-triggered communication to consensus is studied. Simulations show the effectiveness of the proposed estimators in presence
of state porturbations

© 2016, IFAC (International Federation of Automatic Control) Hosting by Elsevier Ltd. All rights reserved. σ state perturbations. C 2010, M 110 (MIOLINGROMS: I GENERAL DI TRIGGINGIO CONTROL) HOSGING CJ ERGO EGGI THI TRIGGER FOG \odot 2016. IFAC (Internation

Keywords: Multi-agent systems, event-triggered, consensus, undirected communication graph.

1. INTRODUCTION 1. INTRODUCTION 1. INTRODUCTION 1. INTRODUCTION

Consensus is an important problem in cooperative control, see Olfati-Saber et al. [2007], Wei [2008], Garcia et al. $[2014c,b]$. In this problem, several agents have to be synchronized to the same state. When the control is distributed, consensus usually requires significant exchange of information between neighbouring agents so that each agent can properly evaluate its control law. This communication may be either permanent, as in Olfati-Saber munication may be either permanent, as in Offail-Saber
et al. [2007], Wei [2008], or may take place at discrete time instants, which is much more practical. In the latter case, mstants, which is much more practical. In the latter case,
communications may occur periodically, as in Garcia et al.
[2014b], may be intermittent, as in Wen et al. [2012a,b, $\frac{2014b}{m}$, may be intermittent, as in Wen et al. $\frac{2014b}{m}$, may be intermittent, as in Wen et al. $\frac{2012a}{m}$, 2013 , or may be uncrimeded, as in the calculation, 2013 , or may be event-triggered as in Dimarogonas and Johansson [2009], Jiangping et al. [2011], Dimarogonas et al. [2012], Fan et al. [2013], Garcia et al. [2014c], Zhang et al. [2015]. et al. [2015]. et al. [2012], Fan et al. [2013], Garcia et al. [2014c], Zhang et al. [2012], Fan et al. [2013], Garcia et al. [2014c], Zhang et al. [2015]. et al. [2015]. et al. [2015]. \mathbb{R} event-triggered communication is the most promising approach is the most promising approach \mathbb{R} α is an important problem in cooperative control, α Consensus is an important problem in cooperative control, $\frac{1}{2}$ Consensus is an important problem in cooperative control,

Event-triggered communication is the most promising approach to save communication energy, while allowing a consensus to be reached. To reduce the number of communications in a decentralized case, each agent estimates the state of its neighburs to evaluate its control law. Additionally, each agent also estimates its own state with the information available to its neighbours. The error between this estimate and its actual state is then used to trigger a communication when it reaches some threshold. In Dimarogonas et al. [2012], the agent dynamic is a single integrator and the considered threshold decreases with time while reaching the consensus. This implies an increase with the frequency of communications. In Seyboth et al. [2013], the dynamic is a double integrator and the triggering condition depends on a state-independent and exponentially decreasing threshold. The communication frequency reduces compared to Dimarogonas et al. [2012] but still increases close to consensus. General linear dynamics are considered in Zhu et al. [2014], Garcia et al. [2014c,a]. State-dependent thresholds are then considered to ensure State-dependent thresholds are then considered to ensure State-dependent thresholds are then considered to ensure Event-triggered communication is the most promising ap-Event-triggered communication is the most promising apsome convergence property for the system. These previous approaches were developed for noise-free dynamics and approacnes were developed for noise-free dynamics and
prove sensitive to perturbations. This issue has been partly addressed by Hu et al. [2014] and Cheng et al. [2014] who proposed an event-triggered method to mitigate the impact of perturbations in the case of dynamics described by simple integrators. by simple integrators. by simple integrators. some convergence property for the system. These previous T_{S} parameters the problem of decentralized events of decentralized events of decentralized events of T_{S} some convergence property for the system. The system is \mathcal{L} some convergence property for the system. These previous $\frac{1}{2}$

This paper addresses the problem of decentralized event-This paper addresses the problem of decentralized event-
triggered communications for consensus of a multi-agent system with both general linear dynamics and state perturbations. This work extends results presented in Garcia et al. $[2014c,a]$ by introducing a new estimator to take et al. [2014c,a] by introducing a new estimator to take
into account the control input of the agents. With this
approach, estimates of the states of all the agents (not approach, estimates of the states of all the agents (not only neighboring ones) are required to evaluate all control laws. More estimates are performed, but this reduces the communication frequency. A convergence analysis is achieved while considering state perturbations composed agent-scale mine conntacting state perturbations composed
of two components: one common to all agents, and one agent-specific. agent-specific. agent-specific. This paper addresses the problem of decentralized event- \mathcal{A}_{S} introducing some notations in Section 2, the problem \mathcal{A}_{S} This paper addresses the problem of decentralized event-This paper addresses the problem of decentralized eventtriggered communications for consensus of a multi-agent

After introducing some notations in Section 2, the problem statement is presented in Section 3. The new estimator $\frac{1}{2}$ is described in Section 4, along with a communication is described in Section 4, along with a communication
protocol. A second estimator to obtain a decentralized
event-triggered strategy is presented in Section 5. Section 6
compares the performance of the proposed approach t event-triggered strategy is presented in Section 5. Section 6 compares the performance of the proposed approach to compares the performance of the proposed approach to state-of-the-art results from Garcia et al. [2014c,a]. state-of-the-art results from Garcia et al. [2014c,a]. state-of-the-art results from Garcia et al. [2014c,a]. After introducing some notations in Section 2, the problem After introducing some notations in Section 2, the problem After introducing some notations in Section 2, the problem

2. NOTATIONS AND HYPOTHESES 2. NOTATIONS AND HYPOTHESES 2. NOTATIONS AND HYPOTHESES 2. NOTATIONS AND HYPOTHESES 2. NOTATIONS AND HYPOTHESES

Classical notations from Cortes and Martinez [2009] are first briefly recalled. Consider a network of N agents which first brieny recalled. Consider a network of N agents which
topology is described by a fixed and undirected graph topology is described by a fixed and undirected graph
 $\mathcal{G} = (\mathcal{N}, \mathcal{E})$. N is the set of agents and \mathcal{E} describes the $\mathcal{G} = (N, \mathcal{E})$. N is the set of agents and E describes the
communication links between pair of agents. The set of neighbours of an Agent i is $\mathcal{N}_i = \{j \in \mathcal{N} | (i,j) \in \mathcal{E}, i \neq j\}.$ N_i is the cardinal number of \mathcal{N}_i . Let $1_N = [1, 1, ..., 1]^T$ neighbours of an Agent i is $\mathcal{N}_i = \{j \in \mathcal{N} | (i,j) \in \mathcal{E}, i \neq j\}.$ C_1 is the cortes and Martinez [2009] $f_{\text{classical notations from Cortes and Martinez}$ [2009] are communication links between pair of agents. The set of
poighbours of an Agent i is $\mathcal{N} = \{i \in \mathcal{N} | (i, i) \in \mathcal{S} | i \neq i \}$. neighbours of an Agent i is $\mathcal{N}_i = \{j \in \mathcal{N} | (i, j) \in \mathcal{E}, i \neq j\}$.
N. is the cardinal number of \mathcal{N}_i . Let $1_N = \begin{bmatrix} 1 & 1 & 1 \end{bmatrix}^T \in \mathcal{N}_i$ communication links between pair of agents. The set of
neighbours of an Agent i is $\mathcal{N}_i = \{j \in \mathcal{N} | (i, j) \in \mathcal{E}, i \neq j\}$.
 N_i is the cardinal number of \mathcal{N}_i . Let $1_N = [1, 1, ..., 1]^T \in$ N_i is the cardinal number of \mathcal{N}_i . Let $1_N = [1, 1, ..., 1]^T \in$

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 $\mathbb{R}^{N\times 1}$ be the all-one vector and $\mathbf{I}_N\in\mathbb{R}^{N\times N}$ be the identity matrix of size N . Since G is undirected, its Laplacian matrix L is symmetric. L also satisfies $L1_N = 0$ and has only one null eigenvalue $\lambda_1(L)$ and all its non-zeros eigenvalues $\lambda_2(L) \leq \lambda_3(L) \leq \ldots \leq \lambda_N(L)$ are strictly positive.

The Kronecker product is denoted by ⊗. For a matrix $M, \lambda_{\min}(M), \lambda_{\min>0}(M),$ and $\lambda_{\max}(M)$ are respectively the smallest, the smallest strictly positive, and the largest eigenvalue of M . For a given vector x and a symmetric matrix M , $||x||_M = x^T M x$.

3. PROBLEM STATEMENT

Assume that the dynamic equations of Agent i are

$$
\dot{x}_{i}(t) = \mathbf{A}x_{i}(t) + \mathbf{B}u_{i}(t) + d_{i}(t)
$$
 (1)

$$
u_{i}(t) = c_{1} \mathbf{F} \sum_{j \in \mathcal{N}_{i}} \left(y_{i}^{i}(t) - y_{j}^{i}(t) \right), \qquad (2)
$$

where $x_i \in \mathbb{R}^n$ is the state of Agent i, $u_i \in \mathbb{R}^m$ is its control input evaluated using $y_j^i \in \mathbb{R}^n$, the estimate of x_j performed by Agent i as described in Section 4, and $d_i(t)$ is some state perturbation. $c_1 = c + c_2$ with $c = 1/\lambda_2(L)$ and $c_2 \geq 0$ is a design parameter. $\mathbf{F} = -\mathbf{B}^T \mathbf{P}$ where P is a symmetric positive semi-definite matrix, solution of the Riccati equation

$$
\mathbf{PA} + \mathbf{A}^T \mathbf{P} - 2 \mathbf{P} \mathbf{B} \mathbf{B}^T \mathbf{P} + 2\alpha \mathbf{P} < 0,\tag{3}
$$

with $\alpha > 0$.

The additive perturbation is assumed to be such that

$$
d_{i}(t) = m(t) + s_{i}(t), \qquad (4)
$$

where $m(t) \in \mathbb{R}^n$ is a bounded time-varying perturbation with $\|m(t)\| \leq M_{\text{max}}$, identical for all agents and $s_i(t) \in$ \mathbb{R}^n is a bounded agent-specific perturbation, with for all $i = 1, \ldots, N \, \|s_i(t)\| \leq S_{\text{max}} \, \forall t.$ The vector of all state perturbations is denoted by

$$
d(t) = 1_N \otimes m(t) + [s_1(t)^T ... s_N(t)^T]^T
$$
. (5)

The problem considered consists in designing a control scheme to reach a bounded consensus, while limiting the communications between agents. For that purpose, communication time instants are chosen locally by Agent i using an event-triggered approach involving the state estimation error $e_i^i = y_i^j - x_i$, as detailed in Section 5.

In this paper, we suppose as in Garcia et al. [2014c] that there is no communication delay, and agents know perfectly their own state.

4. AGENT STATE ESTIMATION AND COMMUNICATION PROTOCOL

4.1 Agent state estimation

Define $t^i_{j,k}$ as the time at which the k-th message sent by Agent j has been received by Agent i . The time instant at which the k -th message has been sent by Agent j is denoted $t_{j,k}$. The time of reception by Agent i of the ℓ -th message is t_{ℓ}^{i} , whatever the sending agent.

In Garcia et al. [2014c], the estimate $y_j^i(t)$ of x_j performed by Agent i is

$$
y_j^i(t_{j,k}^i) = x_j(t_{j,k}^i),
$$
\n(6)

$$
\dot{y}_{j}^{i}(t) = \mathbf{A} y_{j}^{i}(t), \quad t_{j,k}^{i} \le t < t_{j,k+1}^{i}.
$$
 (7)

Let $y^i = \begin{bmatrix} y_1^{iT} & y_2^{iT} & \cdots & y_N^{iT} \end{bmatrix}^T \in \mathbb{R}^{Nn}$ be the vector gathering the estimates of the state of all agents performed by Agent i. The vector gathering the estimates of their own state by each agent is $y = \left[y_1^{1T} y_2^{2T} \dots y_N^{NT}\right]^T \in \mathbb{R}^{Nn}$.

The first state estimator proposed here takes into account the control input of the agents and the way it is evaluated

$$
\dot{y}_{j}^{i}(t) = \mathbf{A} y_{j}^{i}(t) + \mathbf{B} \tilde{u}_{j}^{i}(t), \quad t_{j,k}^{i} \le t < t_{j,k+1}^{i}(8)
$$

$$
\tilde{u}_j^i(t) = c_1 \mathbf{F} \sum_{p \in \mathcal{N}_j} \left(y_j^i(t) - y_p^i(t) \right)
$$
\n(9)

$$
y_j^i(t_{j,k}^i) = x_j(t_{j,k}^i).
$$
 (10)

Considering all agents, (8)-(10) can be rewritten as

$$
\dot{y}^{i}(t) = \mathbf{A}_{c} y^{i}(t), \quad t^{i}_{j,k} \le t < t^{i}_{j,k+1} \quad (11)
$$

$$
y_j^i(t_{j,k}^i) = x_j(t_{j,k}^i),
$$
\n(12)

where $\mathbf{A}_c = \overline{\mathbf{A}} + \overline{\mathbf{B}}_1$, $\overline{\mathbf{A}} = \mathbf{I}_N \otimes \mathbf{A}$, and $\overline{\mathbf{B}}_1 = c_1 L \otimes (\mathbf{B} \mathbf{F})$. Each agent has then to estimate the states of all agents of the network to determine the control inputs applied by all other agents.

4.2 Communication protocol

As in Garcia et al. [2014c], the message broadcast by Agent *i* at $t_{i,k}$ contains its state x_i ($t_{i,k}$) and $t_{i,k}$. Agent *j*, $j \in \mathcal{N}_i$, uses $x_i(t_{i,k})$ to update its estimate y_i^j (6). Nevertheless, this is not possible when $j \notin \mathcal{N}_i$. The following protocol is proposed to address this issue and implement $(8)-(10)$.

Let $\mathcal{T}^i = [t^i_{1,k_1} \dots t^i_{N,k_N}]^T$ be the vector of reception times of $y_1^1 \ldots y_N^N$ by Agent *i*. When an agent broadcasts a message, it updates its own estimate y_i^i with x_i , *i.e.*, $y_i^i(t_{i,k}) = x_i(t_{i,k})$ and transmits y^i and \mathcal{T}^i to its neighbours. Then, each neigbhour compares the time instants in \mathcal{T}^i with those of its own \mathcal{T}^j . Only the components of y^j such that $t_{i,k} > t_{j,k}$, *i.e.*, corresponding to a more recent time instant, are replaced by those of y^i .

With this communication protocol, Agent j is thus able to update its estimate y_i^j of x_i even if $j \notin \mathcal{N}_i$.

4.3 Estimation v^i of y^i by Agent j

With the previously introduced communication protocol, y_j^i is only known by Agent i and cannot be used by Agent j in its communication triggering condition. To address this issue, each Agent i considers estimates v^j = $\left[v_1^{jT} \dots v_N^{jT}\right]^T \in \mathbb{R}^{Nn}$ of y^j for all $j \in \mathcal{N}_i \cup \{i\}$, with the constraint that estimate v^i performed by Agent i and Agent j when $j \in \mathcal{N}_i$ have to be identical. As a consequence, it is less frequently updated than y^i and thus it is less accurate.

The dynamics of v^i is expressed as

$$
\dot{v}^i(t) = \mathbf{A}_c v^i(t) \tag{13}
$$

$$
v^{i}(t_{i,k}) = y^{i}(t_{i,k})
$$
\n(14)

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