

# Hidden Oscillations In The Closed-Loop Aircraft-Pilot System And Their Prevention <sup>★</sup>

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**Abstract:** The paper is devoted to studying and prevention of a special kind of oscillations – the Pilot Involved Oscillations (PIOs) which may appear in man-machine closed-loop dynamical systems. The PIO of categories II and III are defined as essentially non-linear unintended steady fluctuations of the piloted aircraft, generated due to pilot efforts to control the aircraft with a high precision. The main non-linear factor leading to the PIO is, generally, rate limitations of the aircraft control surfaces, resulting in a delay in the response of the aircraft to pilot commands. In many cases, these oscillations indicate presence of hidden, rather than self-excited attractors in the aircraft-pilot state space model. Detection of such a kind of attractors is a difficult problem since basin of attraction is not connected with unstable equilibrium. In the paper existence of the hidden attractor in pitch motion of the piloted aircraft is demonstrated and the nonlinear phase shift compensator is designed. The results obtained demonstrate that the proposed method in several times increases the admissible gain of the “airplane-pilot” loop as compared with non-corrected system.

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**Keywords:** hidden attractor, rate limitations, pilot-aircraft model, pilot-involved oscillations, phase shift, nonlinear, compensator

## 1. INTRODUCTION

The oscillation phenomena in dynamical systems play a very significant part in nature, science, technology, medicine, biology, etc. An essential part of the investigations in this field consists in studying so-called *self-excited* and *hidden* oscillations see (Leonov and Kuznetsov, 2013b; Kuznetsov and Leonov, 2014; Leonov et al., 2015b; Kuznetsov, 2016) for surveys and the bibliography. During the initial period of the development of the theory of non-linear oscillations a main attention was paid to studying self-excited oscillating systems, for which the existence of oscillations is “almost obvious” since the oscillation is excited from an unstable equilibrium. Later, the examples of periodic and chaotic oscillations of another type have been found, called *hidden oscillations* and corresponding *hidden attractors*, i.e. attractors, which basin of attraction does not intersect with small neighborhoods of equilibria. Numerical localization, computation, and analytical inves-

tigation of hidden attractors are much more difficult problems than for self-excited ones, since there is no possibility here to use information about equilibria for organization of similar transient processes in the standard computational procedure. For nonautonomous systems, depending on the physical problem statement, the notion of self-excited and hidden attractors can be introduced with respect to the stationary states of the system at the fixed initial time or the corresponding system. For a numerical localization of hidden oscillations, an effective analytical-numerical approach is based on the small parameter method for the harmonic linearization has been developed, justified and demonstrated by the several application examples (Leonov and Kuznetsov, 2013a; Andrievsky et al., 2015b; Leonov et al., 2015a). Application of the harmonic linearization method to performance analysis of harmonically forced nonlinear systems is deeply studied in (Pavlov et al., 2007; Pogromsky et al., 2007; van den Berg et al., 2007; Pogromsky and Van Den Berg, 2014).

Among the other phenomena, when hidden oscillations appear, the co-called *Pilot-Involved Oscillations* (PIO)

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may be mentioned. The PIO is denoted as unintended steady fluctuation of the piloted aircraft generated due to the efforts of the pilot to control the aircraft. While PIOs can be easily determined from the analysis of the post-flight data, the pilots often do not recognize that PIO occurs: from their point of view, the plane seems faulty, having “a breakage” (Ashkenas et al., 1964; Klyde and Mitchell, 2004; Acosta et al., 2014). The PIO is one the topical problems from the very beginning of aviation, and the efforts of many scientists and designers for many years were aimed to their elimination, see (Ashkenas et al., 1964; McRuer, 1995) for mentioning a few.

As is noted in (Ashkenas et al., 1964), the following two types of manual control system behavior should be considered:

- before the PIO occurs, the pilot produces the control by more-or-less random input signals and quasi-stationary set of feedbacks, which are compatible with “good” control with small error, stability, low effort, etc. Only one or two control loops are usually dominant.
- when the PIO happens, the airframe motions are changed from a random-like form to a nearly sinusoidal one.

Therefore one of the widespread tools for studying this phenomenon is the numerical-analytical *harmonic linearization* method (also known as the *describing functions* method) (Garber and Rozenvasser, 1965; Gelb and Vander Velde, 1968; Leonov and Kuznetsov, 2013a). This method is used in the present work for examination of *nonlinear phase predicting filter*, which is intended to be used in the “pilot-airplane” loop for PIO prevention.

The rest of the paper is organized as follows. The aircraft-pilot model in the pitch control loop is presented in Sec. 2. Existence of hidden oscillations in the aircraft-pilot closed-loop contour in absence of correction is demonstrated in Sec. 3. Nonlinear correction for PIO prevention is considered in Sec. 4. Concluding remarks are given in Sec. 5.

## 2. AIRCRAFT-PILOT MODEL

### 2.1 Aircraft-pilot model

*Aircraft model.* The following transfer function of the X-15 research aircraft longitudinal dynamics from the elevator deflection to pitch angle  $\theta$  is taken (Mehra and Prasad, 1998; Alcalá et al., 2004)

$$W_{\delta}^{\theta}(s) = \left\{ \frac{\theta}{\delta_e} \right\} = \frac{86.9(s + 0.883)}{(s + 25)(s + 0.3516)(s + 0.02845)} \times \frac{s + 0.0292}{s^2 + 1.68s + 5.29}, \quad (1)$$

where  $\delta_e(t)$  denotes the elevator deflection with respect to the trimmed value,  $\theta(t)$  stands for the pitch angle (all variables are given in the SI units),  $s \in \mathbb{C}$  is the Laplace transform variable.

*Rate-limited actuator model.* The actuator is modeled as a first-order low-pass filter with rate limitation:

$$\dot{\delta}_e(t) = \text{sat}_{\bar{\omega}}(T^{-1}(u(t) - \delta_e(t))), \quad (2)$$

where  $\text{sat}_{\bar{\omega}}(\cdot)$  denotes the following *saturation* function  $\text{sat}_{\bar{\omega}}(z) = \begin{cases} z, & \text{if } |z| \leq \bar{\omega}, \\ \bar{\omega} \text{sign } z, & \text{otherwise} \end{cases}$ ,  $\text{sign}(\cdot)$  is a *signum* function. (To simplify the exposition we assume that the servo has a unit static gain).

*Pilot models.* The pilot is often modeled as a serial element in the closed-loop system, which, having enough flight skills, develops a stable relationship between his control action and a specific set of flight sensors signals (McRuer and Jex, 1967).

Below, two kinds of the pilot model are considered.

**1. Pilot model in the form of a static gain.** Following (Rundqwist and Stahl-Gunnarsson, 1996; Mehra and Prasad, 1998; Alcalá et al., 2004; Andrievsky et al., 2015a), a pilot may be modeled in the form of a static gain  $K_p$ , applied to the pitch tracking error, so that

$$u(t) = K_p(\theta^*(t) - \theta(t)). \quad (3)$$

**2. Pilot model in the form of a lead-lag-delay unit.** Based on (McRuer and Jex, 1967; Barbu et al., 1999; Lone and Cooke, 2014; Efremov et al., 2015) the pilot behavior may be modeled by the following describing function, which corresponds to the open-loop crossover model:

$$W_p(s) = \left\{ \frac{u}{\Delta\theta} \right\} = K_p \frac{T_L s + 1}{T_I s + 1} e^{-\tau_e s}, \quad (4)$$

where  $\Delta\theta$  is the displayed error between desired  $\theta^*(t)$  and actual  $\theta(t)$  pitch angles;  $u(t)$  denotes the pilot's control action, applied to the elevator servo;  $K_p$  is the pilot static gain;  $T_L$  is the lead time constant (relative rate-to-displacement sensitivity);  $T_I$  stands for the lag time constant;  $\tau_e$  denotes the effective time delay, including transport delays and high frequency neuromuscular lags. As stated in the (McRuer and Krendel, 1959; McRuer et al., 1965; McRuer and Jex, 1967), the pilot attempts to adjust the lead or lag value, that the sensitivity of the low frequency response of the closed-loop system to variations in  $T_L$  or  $T_I$  is small and leaving an effective time delay as his primary means to control the stability of the closed-loop and the dominant modes.

## 3. HIDDEN OSCILLATIONS IN THE AIRCRAFT-PILOT CLOSED-LOOP CONTOUR

Let us study behavior of the closed-loop system (1), (2), (3), (4) numerically, assuming that the pilot's control action  $u(t)$  is obtained by a feedback between desired  $\theta^*(t)$  and actual  $\theta(t)$  pitch angles, i.e. that the pilot input is displayed signal  $\Delta\theta(t) = \theta^*(t) - \theta(t)$ . Following (Mehra and Prasad, 1998; Alcalá et al., 2004) let  $\bar{\omega} = 15/57.3$  deg/s be given. Actuator (2) time constant be taken as  $T = 0.02$  s. The following parameters of pilot (4) describing function (4) are taken (McRuer and Jex, 1967; Barbu et al., 1999; Andrievsky et al., 2015a):  $\tau_e = 0.4$  s,  $T_L = 0.625$  s,  $T_I = 0.250$  s, gain  $K_p$  is a varying parameter.

### 3.1 Pilot model in the form of a static gain (3)

Consider the aircraft-pilot system model (1), (2), (3).

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