Contents lists available at ScienceDirect





Computers and Fluids

journal homepage: www.elsevier.com/locate/compfluid

On the proper setup of the double Mach reflection as a test case for the resolution of gas dynamics codes



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ARTICLE INFO

ABSTRACT

Article history: Received 24 November 2014 Revised 25 February 2016 Accepted 6 April 2016 Available online 8 April 2016

MSC: 76J20 76L05 76M99

Keywords: Double Mach reflection High speed flow High resolution scheme Numerical test case

1. The double Mach reflection

A standard test for the quality of a Riemann solver is the double Mach reflection problem. It was suggested by Woodward and Colella [1], as a benchmark for Euler codes. An analytical treatment is found in [2] and [3] and the references therein, while experimental results are presented in [4] and also in [3, pp. 152 and 168]. Recent examples for its use as test of very high order schemes are, e. g., [5,6]. The problem consists of a shock front that hits a ramp which is inclined by 30 degrees. When the shock runs up the ramp, a self similar shock structure with two triple points evolves. The situation is sketched out in Fig. 1. To simplify the graphical representation, the coordinate system is aligned with the ramp as done for the numerical tests. In the primary triple point, the incident shock *i*, the mach stem *m*, and the reflected shock *r* meet. In the double mach configuration, the reflected shock breaks up forming a secondary triple point with the reflected shock r, a secondary (bowed) mach stem m', and a secondary reflected shock r'. From both triple points, slip lines emanate. The reflected shock r'hits the primary slip line s causing a curled flow structure, the resolution of which may serve as an indicator for the resolution of a numerical scheme. As was already stated by Woodward and

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http://dx.doi.org/10.1016/j.compfluid.2016.04.008 0045-7930/© 2016 Elsevier Ltd. All rights reserved. This short communication discusses the initial and boundary conditions as well as the size of the computational domain for the double Mach reflection problem when set up as a test for the resolution of an Euler scheme for gas dynamics.

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Colella, the main challenge for a high resolution scheme is to resolve the secondary slip line s'. Being a rather weak feature, it is hardly visible in a density plot (e. g., [5,6]) or a plot of any velocity component. According to Woodward and Colella [1], the secondary slip s' line can be best observed in the vertical momentum, which is confirmed by the results depicted in Fig. 3. Thus, throughout this paper we present the results for the vertical momentum ρv .

2. The problem: two issues

For our numerical tests, we use the setting as described in [1]. We start with the shock, a Mach 10 shock in a $\gamma = 1.4$ gas, already on the ramp and rotate the coordinate system, so that the computational grid is aligned with the ramp. The undisturbed gas ahead of the shock has a density of 1.4 and a pressure of 1.

The initial shock hits the bottom of the computational domain at $x_0 = 1/6$. Usually the computational domain is chosen as $[0, 4] \times [0, 1]$ and the results are presented for t = 0.2. At the bottom, we employ solid wall conditions, at the right boundary outflow. At all other boundaries we use Dirichlet–conditions, which are set to the physical values.

Unfortunately, as the results in Fig. 2 show, there are severe disturbances of the flow close to the secondary slip line. Depending on the scheme and the grid resolution, it is difficult to distinguish between slip line and numerical artifact.

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Fig. 1. Sketch of the double Mach reflection problem. The bottom line represents the ramp.

As Fig. 2 shows, this setting results in some numerical artifacts disturbing the secondary reflected shock r' and the region between the secondary reflected shock and the secondary slip line. At lower resolutions (left picture), the artifacts are not distinguishable from the secondary slip line s'. While Woodward and Colella [1], blame this effect to the under-resolved shock in the initial condition, Rider et al., [7] argue that the under-resolved shock in the boundary condition for the upper boundary is responsible for it. Both are partially right and partially wrong.

In Fig. 3, we show results for the double Mach reflection computed on $[0, 4] \times [0, 2]$ instead of $[0, 4] \times [0, 1]$. It can be seen that what in Fig. 2 seemed to be one (kinked) phenomenon in fact are two artifacts: one arising from the shock position at the upper boundary-it shows up as a slight disturbance above the shock close to the right boundary and as a slight disturbance a little bit left of the secondary slip line-and one that follows the shock at a certain distance (and slightly to the right of the secondary slip line), indicating that it results from the initial condition. This means that there indeed is an artifact arising from the initial condition (hypothesis by Woodward and Colella) and an artifact arising from the boundary condition (hypothesis by Rider et al.).

In the following, we will investigate both hypotheses by means of numerical tests with different settings. This will give us some hints on the proper use of the double Mach reflection as a test case for Euler codes.

3. The numerical environment for the tests

To set up tests in order to investigate the hypotheses by Rider et al., and by Woodward and Colella, one has to make sure that the grid resolution is the only variable parameter in the numerical scheme. Besides this, the size of the computational domain and the initial and the boundary conditions may vary. But the basic features of the method have to be fixed, including Riemann solver, grid structure, basic approach (finite differences, finite volumes, discontinuous Galerkin,...), reconstruction techniques, limiters, time scheme etc. In this study, we resort to finite volumes on a uniform equidistant Cartesian grid with $\Delta x = \Delta y$. The basic scheme uses wave propagation according to LeVeque [8], with algebraic limiting and Roe with Harten-Hyman entropy fix [9]. Thus, it is a second order TVD-scheme. The second order corrections are applied also for the corner fluxes. As limiter, we employ the mixed use of CFL-Superbee and Superpower as described in [10], modified for nonlinear waves according to Jeng and Payne [11] as described in [12]. The code used for the examples is clawpack [13]. No special starting procedure, reduced time steps etc., is employed. As for Fig. 2, we do not show the entire computational domain. We restrict the *x*-direction to [0, 3] or, in Fig. 4, show a close-up of the region of interest: the region containing the triple points. As already mentioned, the quantity shown is always the vertical



Fig. 2. Numerical artifact near the secondary slip line in the standard setting with $\Delta x = \Delta y = 1/120$ (left) and $\Delta x = \Delta y = 1/480$ (right) and computational domain [0, 4] × [0, 1]. Note the interference of the slip line and the numerical artifact.



Fig. 3. Double Mach reflection computed on [0, 4] × [0, 2]. Left vertical momentum, right density. Note that in the density plot, the secondary slip line is invisible.

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