

# The jump-like crack growth model, the estimation of fracture energy and $J_R$ curve

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Received 24 August 2006; received in revised form 2 March 2007; accepted 8 March 2007

Available online 14 March 2007

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## Abstract

In this paper the jump-like crack growth model for monotonic loading is applied to re-examine both the onset of crack growth and process of stable crack growth. In the former case the fracture energy associated with a new surface creation is estimated and the in-plane constraint influence on this quantity is examined using the  $J-A_2$  approach. In the later case the formula to compute the  $J$ -resistance curve is re-examined and compared with the one known from the standards. In the analysis the plane strain model of a structural element made of elastic–plastic material is assumed.

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*Keywords:* Fracture energy; In-plane constraint;  $J_R$ -curve; Jump-like crack growth

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## 1. Introduction

In the most analyses of stable crack growth under monotonic loading it is assumed that the crack extension is a continuous process. It is a natural consequence of the fundamental assumptions of mechanics of continuum. However, the microscopic observations of the fracture surfaces reveal that in the most real cases the crack growth process is not a continuous one. It concerns both cleavage and ductile fracture mechanisms which are a result of microcrack or void nucleation-growth-coalescence processes taking place at a small distance from the front of a macro-crack. There are many observations and theories (often controversial) concerning these processes that are summarized e.g. in the recent book [1] or paper [2]. The complexity of the crack growth process can be observed in the three-dimensions (3D) during the in situ observations using a high resolution synchrotron X-ray tomography. Qian et al. [3] are among the first who presented such results for ductile materials. This paper [3], is the best example that the real fracture process, in the most cases, is not a continuous propagation of the straight crack front.

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**Nomenclature**

$a, a_i$	crack length, crack length after $i$ th jump
$b$	unbroken ligament of the specimen
$n$	Ramberg–Osgood power exponent
$u$	load–point displacement
$u_e, u_p$	elastic, plastic part of the load–point displacement
$u_i$	displacement vector
$x$	coordinate, measuring distance from the crack tip along the crack faces
$A_1, A_2$	coefficients in the YCS formulae
$\Delta A$	finite crack surface increment
$A'$	new crack surface
$A_c, A_u, A_F$	surfaces of crack, displacement and external loading application areas (Fig. 2)
$B$	specimen thickness
$C_i$	specimen compliance after $i$ th crack jump
$E'$	$E' = E$ , $E$ -Young modulus, for plane stress, $E' = E/(1 - \nu^2)$ for plane strain
$F_i$	external force
$G$	energy release rate
$J$	$J$ -integral
$J_c, J_{IC}$	critical value of the $J$ -integral and critical plane strain standard value of $J$ -integral respectively
$K$	stress intensity factor
$L$	characteristic length in the YCS formulae
$N$	$N = 1/n$
$P_i$	external force
$R$	work of external forces
$S$	surface of the specimen
$T_i$	stress vector along the plane of the crack location
$U$	strain energy
$U_e, U_p$	elastic and plastic strain energy
$V$	volume of the specimen
$W$	specimen width
$\alpha$	constant in the Ramberg–Osgood relation
$\varepsilon_{ij}$	strain tensor
$\varepsilon_0$	$\sigma_0/E$
$\eta$	coefficient relating $J$ -integral to the deformation energy
$\nu$	Poisson ratio
$\sigma_{ij}$	stress tensor
$\tilde{\sigma}_{ij}^k$	$k = 1, 2, \dots$ functions in the YCS formula
$\Gamma$	fracture energy per unit surface
HRR	Hutchinson–Rice–Rosengren
OC	O'Dowd–Shih
SIF	SIF
ssy	small scale yielding
YCS	Yang–Chao–Sutton

Discontinuous crack growth is even more pronounced during fatigue, stress corrosion, hydrogen assisted cracking or fracture at high temperatures. Many jump-like crack growth models were presented in the literature (e.g. [4–10]) in order to explain a complex nature of these processes.

In this paper the analysis is limited to fracture process under monotonically increasing external loading or load–point displacement only. Both the onset of crack growth and stable crack growth will be discussed.

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