



Regular article

On the failure resistance of quasi-periodic lattices

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ABSTRACT

Quasi-periodic materials have been widely studied for their behavior regarding atomic dynamics, photonic, magnetic and electronic properties. They have unique properties inherited from their specific material symmetry. The recent development of additive manufacturing gives the opportunity to produce quasi-periodic structures to benefit from their unique capability. In this paper, quasi-periodic beam lattices are produced and failure experiments are performed. Then, a numerical model is proposed and validated. It is obtained that quasi-periodic Penrose lattices can outperform their periodic counterpart. These results open new ways to design architected materials with enhanced failure energy dissipation capabilities.

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The recent development of additive manufacturing gives the opportunity to produce metamaterials like closed cellular materials efficiently, *i.e.* with a perfect control of the cell shape and distribution. As a particular case, lattice materials are interesting in many fields of application because of their low density. Due to this low density, the question regarding their mechanical properties and their integrity is important. While, their effective elastic properties and energy absorption capabilities under compression have been widely studied [1, 2], their failure behavior remains almost unexplored except a very few papers as [3] concerning crack initiation.

The analysis of lattice materials is usually limited to periodic patterns. But, using additive manufacturing there is no limitation and quasi-periodic arrangements can be obtained. Considering that quasi-periodic structures have demonstrated unique properties regarding various physical phenomena (*e.g.* to store energy in local non-propagative vibration modes or to resist to the propagation of defects), it should be interesting to produce using additive manufacturing quasi-periodic lattices that inherit outstanding properties from their specific arrangement. Quasi-periodic materials have been widely studied for their behavior regarding atomic dynamic, photonic, magnetic and electronic properties [4–6]. They have unique properties inherited from their specific material symmetry. Indeed, quasi-crystals usually have high order large scale symmetry from which they inherit macroscopic isotropy for many physical properties. But contrary to periodic materials that hold the same order of symmetry whatever the observation scale, quasi-crystals appear almost amorphous at smaller scales.

In this paper, quasi-periodic beam lattices are produced at the macroscopic scale (typical beam length of 1 mm) from a photo-sensitive ABS-type polymer powder and failure experiments are performed. Then, a numerical model using elastic Euler-Bernoulli beam elements and an energy based fracture criterion is proposed and validated against the experiments. This allows investigating the failure resistance of some specific arrangements and the impact of characteristic geometrical features on the related energy dissipation. It is obtained that Penrose-type quasi-periodic lattices outperform their periodic counterpart. These results open new ways to design architected materials with enhanced failure energy dissipation capabilities.

The behavior of 2D lattice materials (honeycomb) is investigated. Three types of lattice are selected:

1. quasi-periodic Kite & Dart Penrose tiling [7]
2. periodic approximate of the octagonal lattice [8]
3. periodic hexagonal lattice

They are considered as lattices of elastic beams of rectangular section. Once the absolute size of a specimen is fixed, the remaining parameters to design such materials are: the *unit* cell size or beam length, the beam width and the constitutive material. If the constitutive material is linear and brittle then its properties are supposed to affect the overall behavior (global displacement and force) of the lattice only to a scaling parameter. However, varying the ratio between the *unit* cell size and the specimen size would allow to evidence size effects [9]. Also, the beam width *e* is an important parameter as it strongly affects the ratio between the flexural stiffness (varying as e^3) and tension stiffness (varying as e) of the beams. The stiffness ratio is thus expected to scale with e^2 which allows spanning large investigation domains in terms of

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competition between bending and tension for limited variation of e . This is useful because the variation of e is limited in practice due to the resolution of the manufacturing process (lower bound) and assumptions for beam kinematics (upper bound). The relative density of a lattice scales as e and thus as $1/(l/e)$, l/e being the slenderness of the beams. While the relative density is a meaningful parameter to compare different classes of materials, in the case of beam lattices, slenderness is helping to analyze the trends as it is the parameter governing the competition between flexural modes and tension modes. However, the relation between these two parameters is straightforward and the results can also be interpreted from the insight of the relative density. Note that for a given value of beam slenderness, the relative density for the octogon lattice and the Kite & Dart Penrose tiling are similar while the relative density for the hexagonal lattice is 0.6 times lower.

Experiments have been performed on samples obtained by additive manufacturing. They are made from photo-sensitive ABS-type polymer powder. The bulk material obtained from this process is isotropic. Its elastic behavior is defined by a Young's modulus of 1.4 GPa and a Poisson's ratio of 0.4. The sample design is the same as in [1] with a centered pre-crack oriented at 30° with respect to the direction perpendicular to the loading axis (see Supplementary Material). The lattice structure is embedded by zones completely filled with the material. These zones are caught by the grips of the loading device to apply the remote displacement. The speed of the grips is 0.1 mm/min. This design allows for loading a central square part of 90 mm size with a classical tensile device under macroscopic uniaxial tension. Due to the crack angle of 60° with respect to the loading axis, the crack tips are submitted to a mixed mode loading.

The samples are loaded until failure. Due to the high amount of elastic energy stored in the specimen, failure is unstable for the tested beam width of 0.2 mm. As an illustration of the results, an image of a Kite & Dart Penrose lattice after failure is presented in Fig. 1 (see Supplementary Material for other configurations). One clearly observes interactions between the crack and the structure of the material. It seems that specific features of the lattice (such as the one marked in blue in Fig. 1) induce a deviation of the crack. They could be named extra-tough features as this effect is obtained systematically. The deviation of the crack path induced by these specific features of the lattice makes the actual crack length longer than if the cracks were straight, resulting in a higher effective (from a macroscopic point of view) failure energy. Conversely, periodic structures have weak planes (lines) inducing directionality effects as illustrated in [9]. Even if zigzag patterns can

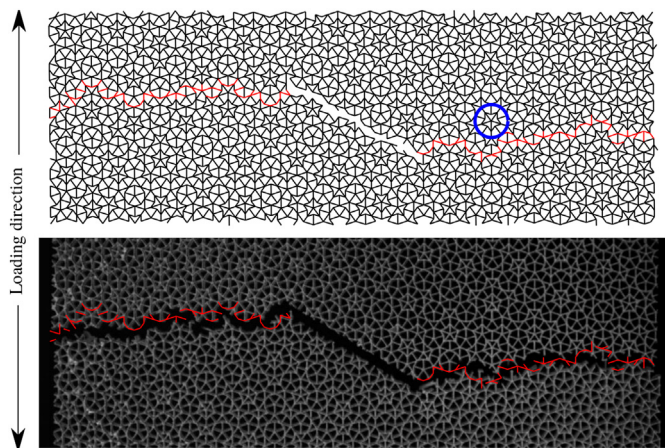


Fig. 1. Comparison of the failure path between experiments and numerical simulations for the Penrose tiling for $e = 0.2$ mm ($l/e \approx 6.7$). The loading direction is vertical and the crack orientation is 30° with respect to the direction perpendicular to the load. The predicted failure path has been overlaid in red onto the experimental picture. The blue circle outlines one of the patterns in the lattice that were to induce a deviation of cracks. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

be obtained in some cases resulting in an increase of the effective failure energy as well, in the tests we performed on periodic lattices, cracks follow straight paths meaning that no dissipation mechanisms induced by the architecture are activated.

For modeling these experiments on the materials described above, a simple numerical model is developed in an in-house MATLAB code. It consists of 2D beam elements under the assumption of Euler and Bernoulli. The constitutive material is assumed to be linear elastic and inertia effects are ignored. The joints between the elements are supposed to be perfect: infinitely rigid with no dissipation. The criterion for beam failure is based on the element-average strain energy density. It allows for weighting the contribution of tension force and bending moment with their actual energy contribution. The averaged strain energy density is denoted for element i as

$$\Phi_i = \frac{1}{2mes(\Omega_i)} \int \sigma : \epsilon d\Omega \quad (1)$$

in the following. In this Equation, Ω_i denotes the volume of element i ($mes(\Omega_i)$ being its size): holds for double contraction of second order tensors and ϵ , respectively σ , is the small strain symmetric tensor, respectively Cauchy stress tensor. The maximum value that can be sustained by a beam before it fails is a material parameter, namely Φ_c . Quasi-static simulations are performed and failure is accounted for using the following steps:

1. Elastic simulation of the lattice under a unit prescribed external load (load factor $\lambda = 1$)
2. detection of the beam i_{max} having the highest averaged strain energy density Φ_{max}
3. the load factor is adjusted so that Φ_{max} equals Φ_c : $\lambda^2 = \Phi_c / \Phi_{max}$
4. the amplitudes of the displacement and external loads computed in step 1 are scaled by λ
5. the results are saved and beam i_{max} is removed from the lattice
6. go to step 1 while the lattice can handle external loading ($\Phi_{max} > 0$)

It is assumed that the behavior of the beams is purely brittle and the global response is adjusted through the load factor in terms of applied displacement and force. In the case when the mechanical response of the specimen is not stable under monotonic loading, snap back (decreasing displacement and force) can be obtained. This is the main difference between the numerical simulations and the experiments in which this instability results in a dynamical response of the specimen (because the displacement can only increase, the specimen “jumps”, with no control on the applied loading, from a stable configuration to the one having the closest but higher prescribed displacement). However, as there is no initial kinetic energy in the system, it is expected that dynamical effects have a very limited influence on the results. The algorithm proposed above to drive the simulation is thus a reliable approximation of the actual loading conditions applied to the specimen. A Griffith like criterion was also tested but its prediction in terms of stability was not correct compared to the experiments. One can argue that such a criterion is based on the existence of a stress singularity at the crack tip. In the analyzed materials herein, this is not the case as the ratio between the crack length and the beam length is low (around 10). Further, in [10], we have demonstrated that a gradient-elasticity model must be used to capture the macroscopic deformation of the lattice and this kind of continuum model is known to cancel out the singularity at the crack tip.

The model involves two material parameters: the Young's modulus E and the critical averaged strain energy density Φ_c . The global response of the specimen scales as E and thus, the only meaningful parameter is the ratio Φ_c/E . However, due to linear nature of the considered model, the crack path is supposed not to depend on this parameter. To simulate the experiments, the two components of the displacement are fixed for all the nodes within a narrow band (its width being the average beam

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