Accepted Manuscript

Existence of solution of a forest fire spread model

Michal Fečkan, Július Pačuta

 PII:
 S0893-9659(18)30116-2

 DOI:
 https://doi.org/10.1016/j.aml.2018.03.035

 Reference:
 AML 5489

To appear in: Applied Mathematics Letters

Received date : 4 February 2018 Revised date : 23 March 2018 Accepted date : 25 March 2018



Please cite this article as: M. Fečkan, J. Pačuta, Existence of solution of a forest fire spread model, Appl. Math. Lett. (2018), https://doi.org/10.1016/j.aml.2018.03.035

This is a PDF file of an unedited manuscript that has been accepted for publication. As a service to our customers we are providing this early version of the manuscript. The manuscript will undergo copyediting, typesetting, and review of the resulting proof before it is published in its final form. Please note that during the production process errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

Existence of solution of a forest fire spread model $\stackrel{\diamond}{\approx}$

Michal Fečkan^{a,*}, Július Pačuta^a

^aDepartment of Mathematical Analysis and Numerical Mathematics, Faculty of Mathematics, Physics and Informatics, Comenius University in Bratislava, Mlynská dolina, 842 48 Bratislava, Slovakia

Abstract

We consider a wildfire spread model represented by the system (1). We use results from the theory of Hamilton-Jacobi equations to prove that there exists a classical solution of (1) for any $(\phi, t) \in$ $\mathbb{R} \times (0, T)$ and some T > 0 and satisfies particular initial conditions. We also use the method of characteristics to obtain the solution of (1) in a certain form.

Keywords: wildfire spread model, Hamilton-Jacobi equations

2010 MSC: 35F21, 35F25, 70H20

1. Introduction

In this paper, we study the system

$$x_t = f_1(x_\phi, y_\phi), \quad y_t = f_2(x_\phi, y_\phi) \quad \text{for } (\phi, t) \in \mathbb{R} \times (0, T), \tag{1}$$

where x_t , y_t , x_{ϕ} and y_{ϕ} denote partial derivatives with respect to t and ϕ , respectively, of functions $x(\phi, t)$ and $y(\phi, t)$, and

$$f_1(x,y) = \frac{a^2 \cos \theta (x \sin \theta + y \cos \theta) - b^2 \sin \theta (x \cos \theta - y \sin \theta)}{\sqrt{a^2 (x \sin \theta + y \cos \theta)^2 + b^2 (x \cos \theta - y \sin \theta)^2}} + c \sin \theta,$$

$$f_2(x,y) = \frac{-a^2 \sin \theta (x \sin \theta + y \cos \theta) - b^2 \cos \theta (x \cos \theta - y \sin \theta)^2}{\sqrt{a^2 (x \sin \theta + y \cos \theta)^2 + b^2 (x \cos \theta - y \sin \theta)^2}} + c \cos \theta.$$

For simplicity, we just write x and y instead of $x(\phi, t)$ and $y(\phi, t)$ in (1). We note that ϕ is a parametrization variable of the curve $(x(\phi, t), y(\phi, t))$, so it does not appear in (1). Here T > 0 and a, b, c, θ are constants. This system was derived in [7] as a model of forest fire spread and its solution (x, y) determines the position of wildfire in time. The ability to predict the direction and speed of fire is very important, since it is essential to make decisions regarding the fire extinguishing, evacuations of communities etc. Of course, such predictions are not easy, since the fire heavily depends on many

^{*}M.F. was supported by the Slovak Research and Development Agency under the contract No. APVV-14-0378 and by the Slovak Grant Agency VEGA No. 2/0153/16. J.P. was supported by the Slovak Research and Development Agency under the contract No. APVV-14-0378 and by the Slovak Grant Agency VEGA No. 1/0347/18. *Corresponding author.

Email addresses: Michal.Feckan@fmph.uniba.sk (Michal Fečkan), julius.pacuta@fmph.uniba.sk (Július Pačuta)

Download English Version:

https://daneshyari.com/en/article/8053639

Download Persian Version:

https://daneshyari.com/article/8053639

Daneshyari.com