Accepted Manuscript

The existence of solutions for quasilinear elliptic problems with multiple Hardy terms

Yuanyuan Li



PII: DOI: Reference:	S0893-9659(18)30026-0 https://doi.org/10.1016/j.aml.2018.01.013 AML 5425
To appear in:	Applied Mathematics Letters
Revised date :	27 December 201726 January 201826 January 2018

Please cite this article as: Y. Li, The existence of solutions for quasilinear elliptic problems with multiple Hardy terms, Appl. Math. Lett. (2018), https://doi.org/10.1016/j.aml.2018.01.013

This is a PDF file of an unedited manuscript that has been accepted for publication. As a service to our customers we are providing this early version of the manuscript. The manuscript will undergo copyediting, typesetting, and review of the resulting proof before it is published in its final form. Please note that during the production process errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

The existence of solutions for quasilinear elliptic problems with multiple Hardy terms

Yuanyuan Li^{a,*}

^aSchool of Mathematics and Statistics, North China University of Water Resources and Electric Power, Zhengzhou 450000, China

Abstract

In this paper, we investigate the quasilinear elliptic equations involving multiple Hardy terms with Dirichlet boundary conditions on bounded smooth domains $\Omega \subset \mathbb{R}^N \ (N \geq 3)$, and prove the multiplicity of solutions by employing Ekeland's variational principle. *Keywords:* quasilinear elliptic equation, Hardy potential, nontrivial weak solution, Ekeland's variational principle

2010 MSC: 35D30, 35J20

1. Introduction

In this paper, we consider the following quasilinear elliptic problem:

$$\begin{cases} -\Delta_p u - \sum_{i=1}^n \mu_i \frac{|u|^{p-2}u}{|x-a_i|^p} = |u|^{p^*-2}u + \lambda f(x, u) & x \in \Omega, \\ u = 0 & x \in \partial\Omega, \end{cases}$$
(1.1)

where $\Omega \subset \mathbb{R}^N (N \ge 3)$ is a bounded smooth domain such that the different points $a_i \in \Omega, i = 1, 2, ..., n, -\Delta_p u = -\operatorname{div}(|\nabla u|^{p-2} \nabla u)$ is the *p*-Laplacian of $u. \ 0 \le \mu_i < \overline{\mu} := (\frac{N-p}{p})^p, \ 1 < p < N$ and λ is a positive parameter.

It is well known that the nontrivial weak solutions for the problem (1.1) are equivalent to the nonzero critical points of the energy functional

$$J(u) = \frac{1}{p} \int_{\Omega} \left(|\nabla u|^{p} - \sum_{i=1}^{n} \mu_{i} \frac{|u|^{p}}{|x - a_{i}|^{p}} \right) dx - \frac{1}{p^{*}} \int_{\Omega} |u|^{p^{*}} dx - \int_{\Omega} \lambda F(x, u) dx$$

defined on $W_0^{1,p}(\Omega)$, where $F(x,u) = \int_0^u f(x,s) ds$. But the appearance of multiple Hardy terms makes difficult to investigate the existence of nontrivial solutions for (1.1).

^{*}Corresponding author

Email address: liyuanyuan@ncwu.edu.cn (Yuanyuan Li)

Download English Version:

https://daneshyari.com/en/article/8053754

Download Persian Version:

https://daneshyari.com/article/8053754

Daneshyari.com