

Accepted Manuscript

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PII: S0893-9659(17)30288-4
DOI: <https://doi.org/10.1016/j.aml.2017.09.009>
Reference: AML 5337

To appear in: *Applied Mathematics Letters*

Received date: 9 July 2017
Revised date: 18 September 2017
Accepted date: 18 September 2017

Please cite this article as: S. Gao, Z. Chen, W. Shi, New oscillation criteria for third-order neutral differential equations with continuously distributed delay, *Appl. Math. Lett.* (2017), <https://doi.org/10.1016/j.aml.2017.09.009>

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New oscillation criteria for third-order neutral differential equations with continuously distributed delay

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Abstract

In this paper, we establish some new criteria for oscillation and asymptotic behavior of solutions of a certain class of third-order neutral differential equations with continuously distributed delay. We study the case of noncanonical equations subject to various conditions. An example is given to illustrate the main results.

Keywords: Oscillatory solution, Third-order neutral differential equation, Continuously distributed delay, noncanonical

2010 MSC: 34K11

1. Introduction

In this paper, we consider the oscillation behavior of the solution of third order neutral differential equation with continuously distributed delay(see[2])

$$\left[r(t) \left[x(t) + \int_a^b p(t, \mu) x[\tau(t, \mu)] d\mu \right]'' \right]' + \int_c^d q(t, \xi) f(x[\sigma(t, \xi)]) d\xi = 0, \quad t \geq t_0. \quad (1.1)$$

Throughout this paper, the following conditions are assumed to hold:

$$(H_1) \quad r(t) \in C^1([t_0, \infty), (0, \infty)), \quad r'(t) \geq 0, \quad \int_a^\infty \frac{1}{r(t)} dt < \infty;$$

$$(H_2) \quad p(t, \mu) \in C([t_0, \infty) \times [a, b], R), \quad 0 \leq p(t) \equiv \int_a^b p(t, \mu) d\mu \leq P < 1;$$

(H₃) $\tau(t, \mu) \in C([t_0, \infty) \times [a, b], R)$ is not decreasing function for μ , and such that

$$\tau(t, \mu) \leq t, \quad \lim_{t \rightarrow \infty} \min_{\mu \in [a, b]} \tau(t, \mu) = \infty;$$

$$(H_4) \quad q(t, \xi) \in C([t_0, \infty) \times [c, d], (0, \infty));$$

(H₅) $\sigma(t, \xi) \in C([t_0, \infty) \times [c, d], R)$ is not decreasing function for ξ , and such that

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