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### Topologically protected dynamics of spin textures

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#### ABSTRACT

We study current-induced dynamics of spin textures in thin magnetic nanowires. We derive effective equations of motion describing the dynamics of the domain-wall soft modes associated with topological defects. Because the magnetic domain walls are topological objects, these equations are universal and depend only on a few parameters. We obtain spin spiral domain-wall structure in ferromagnetic wires with Dzyaloshinskii–Moriya interaction and critical current dependence on this interaction. We also find the most efficient way to move the domain walls by resonant current pulses and propose a procedure to determine their dynamics by measuring the voltage induced by a moving domain wall. Based on translationally non-invariant nanowires, we show how to make prospective magnetic memory nanodevices much more energy efficient.

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#### 1. Introduction

Ferromagnets can be used to store and manipulate spin information, and new developments have created opportunities to use them as active components in spintronic devices [1–4]. Majority of the ideas to employ ferro- and antiferromagnets for memory or logic applications are related to the propagation of domain walls (DWs), skyrmions or other topological spin textures. This resulted in significant experimental [5–11] and theoretical [12–32] progress in this direction. To study theoretically the propagation of the spin textures usually numerical solutions of the Landau–Lifshitz–Gilbert (LLG) equation [13,15] are employed or the dynamics of softest modes for the motion of the topological textures is considered using collective coordinate approach. In this paper we overview the latter approach and consider several important cases of its application to the DW dynamics.

As we will show, for the topologically robust spin textures the equations of motion for their lowest modes are universal and can be described by just a few parameters, which can be whether experimentally measured or analytically calculated for rather simple models. These softest modes are associated with the motion of topological defects comprising the DWs, see Fig. 1. Similar type of equations describe the dynamics of skyrmions [32] or composite skyrmions (vortex–antivortex pair with opposite magnetization polarizations at their core) [33] in ferromagnets. Generally the lowest (zero) mode corresponds to the translation of the spin texture as a whole along the

http://dx.doi.org/10.1016/j.jmmm.2014.12.088 0304-8853/© 2015 Published by Elsevier B.V. nanowire, which is thin enough to have a homogeneous magnetization over its thickness. The other modes correspond to the texture rotations or the internal dynamics of the its topological defects. Below we mostly concentrate on the current driven DW dynamics, although the magnetic field driven case has been extensively studied in the past as well, see e.g. [34,18,19].

#### 2. Model

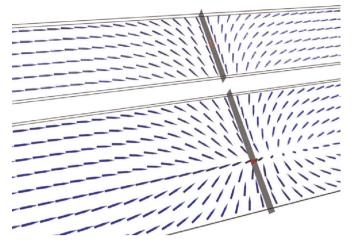
We study the spin texture propagation by employing the LLG equation for the magnetization (**S**) dynamics with adiabatic and nonadiabatic current terms [13,15]:

$$\dot{\mathbf{S}} = \mathbf{S}_0 \times \frac{\delta \mathcal{H}}{\delta \mathbf{S}_0} - j \partial \mathbf{S}_0 + \beta j \mathbf{S}_0 \times \partial \mathbf{S}_0 + \alpha \mathbf{S}_0 \times \dot{\mathbf{S}}_0.$$
(1)

Here  $\mathcal H$  is the magnetic Hamiltonian of the system, j is the electric current in the units of velocity,  $\beta$  is the non-adiabatic spin torque constant,  $\alpha$  is the Gilbert damping constant, and  $\partial=\partial/\partial z$  is a derivative along the wire. We look for a solution of equation (1) in the form  $\mathbf S(z,t)=\mathbf S_0(z,\xi(t))+\mathbf s$ , where the time dependence  $\xi(t)$  is weak, while  $\mathbf s$  is small and orthogonal at each point to the solution  $\mathbf S_0$  of the static LLG equation. In other words, the spin texture dynamics due to an electric current or other perturbations can be parametrized by the time-dependent even-dimensional vector  $\xi(t)$  corresponding to the softest modes of spin texture motion.

The equations for  $\xi(t)$  are called the effective equations of motion. For thin ferromagnetic nanowires, the DWs are rigid

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**Fig. 1.** Types of possible domain walls which can be described by two-component collective coordinate approach. The upper picture shows the simplest type of the domain wall: transverse DW.

topological spin textures. The slow dynamics of the DW can be described in terms of only two collective coordinates corresponding to softest modes of motion. These modes are the DW position  $z_0$  and its conjugate variable – the tilt angle  $\phi$  for the transverse DW. For the vortex DW,  $\phi$  served as the magnetization angle defining the transverse position of the vortex in the wire [18,19]. Up to the leading order in small dissipation ( $\alpha$  and  $\beta$ ) and current, the equations of motion take the form

$$\dot{z}_0 = -\frac{1}{2} \frac{\partial E}{\partial \phi} + j, \tag{2}$$

$$\phi = \frac{1}{2} \frac{\partial E}{\partial z_0} - \frac{\alpha a_{zz}}{2} \frac{\partial E}{\partial \phi} + H + (\alpha - \beta) a_{zz} j.$$
(3)

Here for simplicity we take the magnetic field  $\mathbf{H}$  to be along the wire (in the z direction),  $a_{zz} = \frac{1}{2} \int dz (\partial_z \mathbf{S}_0)^2$ , and  $E(\xi) = \mathcal{H}_\delta[\mathbf{S}_0(z,\xi)]$  is the energy of the domain wall [27] as a function of the soft modes  $\xi$ . These equations are universal and do not depend on details of the microscopic model. The only required input is the energy of a static DW as a function of  $z_0$  and  $\phi$ . The latter function can be either evaluated by means of micromagnetic simulations or an approximate analytical model, as well as experimentally measured for a given nanowire through induced emf due to the DW dynamics [27].

#### 3. Results and discussion

#### 3.1. Translationally noninvariant nanowires

Eqs. (2) and (3) allow the description of the DW dynamics in translationally noninvariant nanowires [30]. Thus one can treat the effects of DW pinning in a wire and consider nanostrips of varying width. As one of the examples of the usage of Eqs. (2) and (3) we consider a magnetic memory device based on a flat hourglass-shaped nanostrip sketched in Fig. 2 (a). We propose a non-volatile device, which employs the magnetization direction within the DW as the information storage. Without applied current, a transverse DW stays at the narrowest place in the nanostrip. When a certain current pulse is applied, the DW magnetization angle  $\phi$  flips from 0 to  $\pi$ . At the intermediate step of this switching process, the DW also deviates from the narrowest part of the nanostrip but at the end it comes back with the opposite magnetization direction in the center of the DW. At a later time, the same current

pulse can move it back to the original configuration.

The time that it takes to switch the magnetization depends on the current pulse shape. During this process the main energy loss in a realistic wire is the Ohmic loss. How much energy is needed for a single switching also depends on the parameters of the current pulse. Using Eqs. (2) and (3) we find the optimal current pulse shape for a given switching time and the minimal required energy per flip as a function of the switching time, Fig. 2(b) [30].

## 3.2. Ferromagnetic nanowires with Dzyaloshinskii–Moriya interaction

One can also use Eqs. (2) and (3) to describe the ferromagnetic nanowires with Dzyaloshinskii–Moriya interaction (DMI) [23]. Recently the spiral structure of magnetization due to DMI has been experimentally observed [35–37]. To describe the spin spiral DWs in ferromagnetic nanowires one should use the Hamiltonian:

$$\mathcal{H} = \int dz \left[ \frac{J}{2} (\partial_z \mathbf{S})^2 + D\mathbf{S} \cdot \left( \mathbf{e}_z \times \partial_z \mathbf{S} \right) - \lambda S_z^2 \right]. \tag{4}$$

Here **S** is the normalized magnetization vector, J > 0 is the exchange interaction constant, D is the DMI constant assuming that the wire is cut or grown along the DMI vector. We consider a thin uniform ferromagnetic wire which can be modeled as a one-dimensional classical spin chain, where the wire is along the z-axis. The last term in Eq. (4) is due to uniaxial anisotropy (with the anisotropy constant  $\lambda$ ) which shows that the system favors the magnetization along the wire. A transverse anisotropy is also added later as a perturbation. By minimizing the Hamiltonian (4) with the appropriate boundary conditions one can get a spin spiral DW. Using the equations of motion (2) and (3) with the Hamiltonian (4), one obtains [23]

$$\dot{z}_0 = \frac{\beta}{\alpha} \dot{j} + \frac{(\alpha - \beta)(1 + \alpha \Gamma \Delta)}{\alpha (1 + \alpha^2)} \left[ \dot{j} - \dot{j}_c \sin(2\phi) \right],\tag{5}$$

$$\phi = \frac{(\alpha - \beta)\Delta}{(1 + \alpha^2)\Delta_0^2} \left[ j - j_c \sin(2\phi) \right],\tag{6}$$

where  $j_c$  is the critical current above which the spin spiral starts rotating around the axis of the nanowire,  $\Delta$  is the DW width ( $\Delta_0$  is the DW width in the absence of DMI), and  $\Gamma = D/J$  is the pitch of the spin spiral. A snapshot of a moving spin-spiral DW in a nanowire with DMI is shown in Fig. 3. Based on these equations one can study the influence of DMI on the critical current and drift velocity of domain wall [23].

#### 3.3. Time-dependent currents and Ohmic losses

For the highest performance of DW memory or logic devices, it is important to minimize the Ohmic losses in the wire, which are due to the resistance of the wire itself and the entire circuit. They are proportional to the time-averaged current square,  $\langle j^2 \rangle$ . Their minimization has a twofold advantage. First, one can increase the maximum current which still does not destroy the wire by excessive heating and therefore move the DWs with a higher velocity, since the DW velocity increases with the applied current. Second, it creates the most energy efficient memory devices and increases their reliability.

These goals can be achieved by utilizing "resonant" time-dependent current pulses, which allow us to gain a significant reduction of Ohmic losses. Based on the DW equations of motion, we show in the next section that all thin wires can be characterized by three parameters obtained from dc-driven DW motion experiments: critical current  $j_c$ , drift velocity  $V_c$  at the critical current,

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