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Hillclimbing saddle point inflation

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ABSTRACT

Recently a new inflationary scenario was proposed in [1] which can be applicable to an inflaton having multiple vacua. In this letter, we consider a more general situation where the inflaton potential has a (UV) saddle point around the Planck scale. This class of models can be regarded as a natural generalization of the hillclimbing Higgs inflation [2].

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The Standard Model (SM) of particle physics is the most successful theory that describes physics below the TeV scale. The observed Higgs mass ~ 125 GeV indicates that the SM can be safely interpolated up to the Planck scale without any divergence or instability. Furthermore, the observed Higgs quartic coupling $\lambda \sim 0.12$ also shows an interesting behavior of the Higgs potential around the Planck scale M_{pl} ; The potential can have another degenerate minimum around that scale. The origin of this behavior comes from the fact that λ and its beta function β_λ can simultaneously vanish around M_{pl} . This is called the Multiple point criticality principle and it is surprising that the Higgs mass was predicted to be around 130 GeV about 20 years ago based on this principle [3].

Various phenomenological and theoretical studies of such a degenerate vacuum have been done so far [4–8]. One of them is the Higgs inflation with a non-minimal coupling $\xi \phi^2 R / M_{pl}^2$ [9]. When this scenario was proposed, it was argued that we need large $\xi \sim 10^5$ in order to obtain the successful inflationary predictions of the cosmic microwave background (CMB). However, the criticality of the Higgs potential makes it possible to realize the inflation even if ξ is relatively small $\sim \mathcal{O}(10)$ by using small but nonzero $\lambda \sim 10^{-6}$ around M_{pl} . See [10] for the detailed analyses.

Although the SM criticality can help the realization of the Higgs inflation, it is difficult to realize the MPP simultaneously because the latter requires $\lambda = 0$ around the Planck scale and we can no longer maintain the monotonicity of the Higgs potential above the scale $\sim M_{pl} / \sqrt{\xi}$. Recently, a new inflationary scenario was proposed in [1] which enables an inflation even if the inflaton potential has multiple degenerate vacua. Then, the authors applied it to

the SM Higgs and showed that it is actually possible to obtain a successful inflation while satisfying the MPP [2]. In those papers, the authors studied a few cases such that the inflaton potential behaves as a quadratic potential around another potential minimum. Although the inflationary predictions of this scenario does not strongly depend on the details of the inflaton potential such as the coefficients of the Taylor expansion, they can depend on the leading exponent of the (Jordan-frame) potential and the choice of the conformal factor. In this letter, we generalize their works to the cases where the inflaton potential has a saddle point around the Planck scale. Our study is meaningful from the point of view of the MPP because this situation can be understood as a natural generalization of this principle. Although some fine-tunings are needed in order to realize a saddle point, some theoretical studies [11–14] suggest that we can naturally archive such fine-tunings by considering physics beyond ordinary field theory.

1. Brief review of hillclimbing inflation

Let us briefly review the hillclimbing inflation. We consider the following action of an inflaton ϕ_J in the Jordan-frame:

$$S = \int d^4x \sqrt{-g_J} \left(\frac{M_{pl}^2}{2} \Omega R_J - \frac{K_J}{2} (\partial \phi_J)^2 - V_J(\phi_J) \right), \quad (1)$$

where $(\partial \phi_J)^2 = g_J^{\mu\nu} \partial_\mu \phi_J \partial_\nu \phi_J$. If we identify ϕ_J as the Higgs, the usual Higgs potential corresponds to $V_J(\phi_J)$ in this framework. Then, by doing the Weyl transformation

$$g_{\mu\nu} = \Omega g_{J\mu\nu}, \quad (2)$$

we have

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$$S = \int d^4x \sqrt{-g} \left[\frac{M_{pl}^2}{2} R - \frac{1}{2} \left(\frac{K_J}{\Omega} + \frac{3}{2} \left(M_{pl} \frac{\partial \ln \Omega}{\partial \phi_J} \right)^2 \right) (\partial \phi_J)^2 - \frac{V_J(\phi_J)}{\Omega^2} \right], \quad (3)$$

where R is the Ricci scalar in the Einstein-frame and we have neglected the total derivative term. Let us now assume that the second term of the kinetic terms dominates. In this case, we can regard $\chi \equiv M_{pl} \sqrt{3/2} \ln \Omega$ or $-M_{pl} \sqrt{3/2} \ln \Omega$ as a fundamental field instead of ϕ_J .¹ For example, in the case of the ordinary Higgs inflation, we have

$$\Omega(\phi_J) = 1 + \xi \frac{\phi_J^2}{M_{pl}^2}, \quad V_J(\phi_J) = \frac{\lambda \phi_J^4}{4}, \quad (4)$$

which leads to the following potential in the Einstein-frame:

$$V_E(\chi) = \frac{\lambda \phi_J^4}{4 \Omega^2} = \frac{\lambda M_{pl}^4}{4 \xi^2} (1 - \Omega^{-1})^2 \simeq \frac{\lambda M_{pl}^4}{4 \xi^2} \left(1 - \exp \left(-\sqrt{\frac{2}{3}} \frac{\chi}{M_{pl}} \right) \right)^2, \quad (5)$$

from which we can see that $V_E(\chi)$ becomes exponentially flat when $\chi \gg M_{pl} \Leftrightarrow \Omega \gg 1$. See also Ref. [10] for more detailed analyses.

On the other hand, a new possibility has been proposed in Ref. [1], where it is shown that we can also consider the $\Omega \ll 1$ region instead of $\Omega \gg 1$. In this case, because V_E is given by $V_E = V_J/\Omega^2$, V_J needs to behave as

$$V_J = V_0 \Omega^2 (1 + \dots) \quad (6)$$

around $\Omega = 0$ in order to realize the inflationary era, i.e. $H = \dot{a}/a = \text{const.}$ Because the conformal factor Ω should approach one after inflation, the inflaton *climbs up* the Jordan-frame potential. This is the reason why the authors of Ref. [1] call this scenario “Hillclimbing (Higgs) inflation”. Let us briefly summarize the inflationary predictions of this scenario. By expanding the Jordan-frame potential V_J as a function of Ω

$$V_J = V_0 \Omega^2 (1 + \sum_{m \geq n} \eta_m \Omega^m), \quad (7)$$

we obtain

$$\epsilon = \frac{M_{pl}^2}{2} \left(\frac{V'}{V} \right)^2 \simeq \frac{1}{3} \left(\sum_m \eta_m m \Omega^m \right)^2, \quad (8)$$

$$\eta = M_{pl}^2 \frac{V''}{V} \simeq -\frac{2}{3} \sum_m \eta_m m^2 \Omega^m, \quad (9)$$

where the prime represents the derivative with respect to χ and we have used the relation $\chi = \sqrt{3/2} \ln \Omega$. Furthermore, we can relate the initial value of Ω to the e -folding number N :

$$N = \int dt H = \frac{1}{M_{pl}^2} \int d\chi \frac{V}{\partial V / \partial \chi} \simeq \frac{3}{2 \eta n n^2} \frac{1}{\Omega_{ini}^n}. \quad (10)$$

From those equations, we obtain the following inflationary predictions:

¹ The choice of the sign depends on the region we consider; When we consider $\Omega \geq 1$ (≤ 1), we take $\chi = (-)M_{pl} \sqrt{3/2} \ln \Omega$.

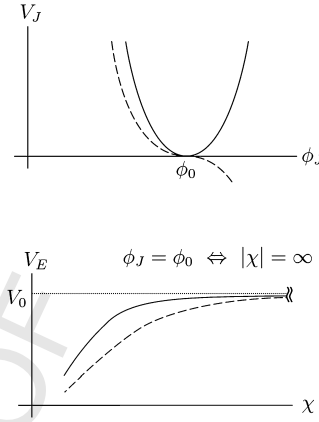


Fig. 1. Upper (Lower): A schematic behavior of the Jordan (Einstein)-frame potential around the saddle point ϕ_0 ($\chi = \infty$). Here, the solid (dashed) contour corresponds to $k = \text{odd}$ (even).

$$n_s = 1 - 6\epsilon + 2\eta \simeq 1 - \frac{2}{N}, \quad r = 16\epsilon = \frac{12}{n^2 N^2}. \quad (11)$$

Note that both of them do not depend on the details of the inflaton potential such as its coefficients η_n 's. This is the similar behavior of the ξ or α attractor [15–17]. However, the leading exponent n depends on a specific model we consider and the choice of the conformal factor. In the following, we consider the hillclimbing inflation around a (UV) saddle point of an inflaton potential.

2. Hillclimbing saddle point inflation

Let us now consider a general situation where the Jordan-frame potential has a saddle point ϕ_0 around the Planck scale:

$$V_J(\phi_0) = 0, \quad V_J^{(1)}(\phi_0) = 0, \quad V_J^{(2)}(\phi_0) = 0, \quad \dots, \quad V_J^{(k)}(\phi_0) = 0 \quad (12)$$

with $V_J^{(i)}$ denoting the i -th derivative of V_J . In the following, we assume

$$\begin{cases} V_J^{(k+1)}(\phi_0) > 0 & \text{for odd } k, \\ V_J^{(k+1)}(\phi_0) < 0 & \text{for even } k, \\ V_J^{(k+2)}(\phi_0) \neq 0 \end{cases} \quad (13)$$

in order to realize a positive vacuum energy in $\phi_J \leq \phi_0$.² This is schematically shown in the upper panel of Fig. 1. In this case, we can expand V_J around ϕ_0 as

$$\begin{aligned} V_J(\phi_J) &= \frac{V_J^{(k+1)}}{(k+1)!} (\phi_J - \phi_0)^{k+1} + \frac{V_J^{(k+2)}}{(k+2)!} (\phi_J - \phi_0)^{k+2} \\ &= \frac{|V_J^{(k+1)}| \phi_0^{k+1}}{(k+1)!} \left(1 - \frac{\phi_J}{\phi_0} \right)^{k+1} \\ &\quad \times \left(1 + v_1^{(k+2)} \left(\frac{\phi_J}{\phi_0} - 1 \right) + v_2^{(k+3)} \left(\frac{\phi_J}{\phi_0} - 1 \right)^2 \right), \end{aligned} \quad (14)$$

where

$$v_1^{(k+2)} = \frac{\phi_0 V_J^{(k+2)}}{(k+2) V_J^{(k+1)}}, \quad v_2^{(k+3)} = \frac{\phi_0 V_J^{(k+3)}}{(k+2)(k+3) V_J^{(k+1)}}. \quad (15)$$

² The third assumption is not necessary for our present set up. We can also consider a more general situation such that $V_J^{(k+1)}(\phi_0) \neq 0$, $V_J^{(k+2)}(\phi_0) = 0$, \dots , $V_J^{(k+m)}(\phi_0) = 0$, $V_J^{(k+m+1)}(\phi_0) \neq 0$.

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