



# Mean velocity profiles of fully-developed turbulent flows near smooth walls

## *Distribution de la vitesse moyenne près de la paroi lisse dans un écoulement turbulent*

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### ABSTRACT

The work proposes an indirect turbulence model to represent the mean streamwise velocity profile of fully-developed turbulent channel flows near smooth walls. The proposed turbulence model highlights that the parameters of the velocity distribution are functions of the friction Reynolds number. It is also shown that the proposed expression for the velocity distribution is in line with the principles of dimensional analysis; it allows one to satisfy the imposed boundary conditions; in the regions close to the wall it allows to reproduce (with good agreement) the velocity profiles available in literature obtained through a Direct Numerical Simulation (DNS).

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### R É S U M É

Un modèle de turbulence a été développé pour représenter la distribution de la vitesse moyenne locale dans les écoulements uniformes turbulents. Le modèle proposé permet de décrire la distribution de la vitesse moyenne (en fonction du nombre de Reynolds) près de la paroi lisse d'un canal à section rectangulaire très large. Il est démontré que l'expression proposée est conforme aux principes de l'analyse dimensionnelle; elle permet de satisfaire les conditions aux limites imposées au problème; elle permet de reproduire, dans les zones près de la paroi, les distributions de la vitesse disponibles dans la littérature et obtenues par intégration numérique directe des équations de Navier–Stokes (DNS).

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## 1. Introduction

The impossibility for the logarithmic law and for the power law to represent the mean velocity profiles in every point of a generic cross section of a fully-developed turbulent wall-bounded flow [1,2] has led some authors to propose, in the regions close to the wall, velocity distribution laws based on experimental considerations, on semi-empirical theories or on indirect turbulence models [3–5].

An exhaustive study of the near-wall behaviour of turbulent wall-bounded flows is quoted in Buschmann et al. [6]. In Poggi et al. [7] there is an experimental technique which allows to obtain detailed information on turbulent quantities in the regions close to the wall.

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Using the equation adopted by van Driest [8] – concerning the mixing length – and the study method based on the eddy viscosity, Absi [9] has recently deduced the near smooth wall mean velocity profile from the integration of the momentum equation. With reference to fully-developed turbulent flows in smooth channels having a very wide rectangular cross section, Absi's method allows to determine the mean streamwise velocity profile  $u^+$  in the region close to the wall defined by  $0 \leq y^+ \leq 20$ , having indicated, as usual, with  $u^+$  and  $y^+$  the non-dimensional quantities referred to the distance from the wall  $y$ , to the kinematic viscosity of the fluid  $\nu$  and to the friction velocity  $u_\tau$ , this latter defined by the relation  $u_\tau = \sqrt{\tau_0/\rho}$ , where  $\tau_0$  is the wall-shear stress and  $\rho$  the fluid density.

A different criterion to define the mean streamwise velocity profile in the domain  $0 \leq y^+ \leq 20$  has been proposed by Bucci et al. [10]. The criterion, defined for fully-developed turbulent flows in smooth pipes, is based on the possibility offered by the electrolytic tank to realise an electric field distribution formally superimposable to the required velocity profile. Starting from these results, this note proposes an indirect turbulence model to represent the mean streamwise velocity profile of fully-developed turbulent channel flows near smooth walls. The proposed turbulence model highlights that the parameters of the velocity distribution are functions of the friction Reynolds number. It is also shown that the proposed expression for the velocity distribution is in line with the principles of dimensional analysis; it allows to satisfy the boundary conditions imposed to the problem; it allows to reproduce, in the regions near the wall defined by  $0 \leq y^+ \leq 20$ , the velocity profiles available in literature obtained through a Direct Numerical Simulation of Navier–Stokes equations (DNS).

## 2. Velocity profile near smooth walls

In Bucci et al. [10] it has been shown that it is possible to implement, in an electrolytic tank with a circular shape, an electric field distribution combining two electric field distributions. In detail, the first of them,  $\Delta V_1$ , is obtained with a circular thin lamina with a diameter  $D$  made up of leading material with constant conductivity  $\sigma$ , run through by a uniform current with density  $j$ , for which:

$$\Delta V_1 = \frac{j}{4\sigma} \left( \frac{D^2}{4} - r^2 \right) = C_1 \left( 1 - 4 \frac{r^2}{D^2} \right) \quad (1)$$

where  $r$  measures the distance from the axis; the second distribution of electric field  $\Delta V_2$  is obtained applying the potential difference  $\Delta V_0$  between the condenser armours of a coaxial cylindrical condenser with internal diameter  $d$  and with external diameter  $D$ :

$$\Delta V_2 = \Delta V_0 \frac{\ln \frac{2r}{D}}{\ln \frac{d}{D}} = C_2 \ln \frac{2r}{D} \quad (2)$$

By superimposing  $\Delta V_1$  and  $\Delta V_2$ , the resultant electric field distribution is:

$$\Delta V = \Delta V_1 + \Delta V_2 = C_1 \left( 1 - 4 \frac{r^2}{D^2} \right) + C_2 \ln \frac{2r}{D} \quad (3)$$

The experimental installation used and the method to take over data are described in Bucci et al. [10] that can be consulted for every details.

For the purposes proposed by this note it is sufficient to remember that it is possible to generate an electric field distribution completely superimposable to the mean velocity profiles of fully-developed turbulent pipe flows in the regions near the smooth walls.

The results obtained by Bucci et al. [10] lead to assign to the mean streamwise velocity profile the expression:

$$u^+ = \beta_1 \left( 1 - 4 \frac{r^2}{D^2} \right) + \beta_2 \ln \frac{2r}{D} \quad (4)$$

being:  $u^+ = \frac{\bar{u}}{u_\tau}$  the non-dimensional velocity, defined by the relation between the mean streamwise velocity  $\bar{u}$  and the friction velocity  $u_\tau$ ;  $r$  the distance from the axis of the pipe with diameter  $D$ ;  $\beta_1$  and  $\beta_2$  two functions of friction Reynolds number  $Re_\tau = \frac{u_\tau D}{\nu}$ .

Considering the relation:

$$\frac{2r}{D} = 1 - 2 \frac{y^+}{Re_\tau} \quad (5)$$

Eq. (4) can be expressed as a function of the non-dimensional distance from the wall  $y^+$ :

$$u^+ = \lambda_1 y^+ \left( 1 - \frac{y^+}{Re_\tau} \right) + \lambda_2 \ln \left( 1 - \frac{2y^+}{Re_\tau} \right) \quad (6)$$

where

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