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Design of exponential state estimator for neural networks with distributed delays

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Abstract

In this letter, the delay-dependent state estimation problem for recurrent neural networks with both time-varying and distributed time-varying delays is investigated. Through available output measurements, a delay-dependent criterion is established to estimate the neuron states such that the dynamics of the estimation error is globally exponentially stable. The derivative of a time-varying delay can take any value and the activation functions are assumed to be neither monotonic, nor differentiable, which are more general than the recently commonly used Lipschitz conditions. Finally, two illustrative examples are given to demonstrate the usefulness of the obtained condition.

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1. Introduction

In the past decade, neural networks have been studied intensively. They have found a large amount of successful applications in many fields such as signal processing, pattern recognition and static image processing, and these applications depend on the dynamic behaviours heavily. Delayed systems are frequently encountered in various areas realistically, and time delay is often a source of instability and oscillations in the system. Therefore, dynamics in a neural network often have time delays due to many reasons, such as the finite switching speed of amplifiers in electronic neural networks or the finite signal propagation time in biological networks. As a result, either delay-independent or delay-dependent, sufficient conditions have been proposed to verify the asymptotical or exponential stability of delayed neural networks (see, e.g. [1–13]).

On the other hand, since the neuron states are not often fully available in the network outputs in many applications, the neuron state estimation problem is also important for many applications to utilize the estimated neuron state. In recent years, the state estimation problem for neural networks has recently drawn particular research interests, see [14–16] for some recent results. Through available output measurements, the problems addressed in [14–16] are to estimate the neuron states in which the dynamics of the estimation error is globally asymptotically or exponentially stable. For the recurrent neural networks (RNNs) with mixed discrete and distributed delays, [14] first studied the state

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estimation problem and obtained some state estimation conditions. However, the proposed criteria are not applicable for systems with time-varying delays. In [15], though the obtained results can be applicable for systems with time-varying delays, they cannot cope with cases when the derivative of time-varying delay equals or is greater than 1. In [16], the state estimation problem for neural networks with time-varying delay is investigated and the derivative of a time-varying delay can take any value. Yet, the proposed methods cannot deal with the neural networks with both discrete and distributed time delays. So far, to the best of the authors' knowledge, as for the systems with time-varying and distributed delays and the derivative of a time-varying delay can take any value, the state estimation problem has not been fully investigated yet and remains challenging. It is, therefore, our intention in this paper to tackle this problem and provide an LMI-based condition for the desired state estimators, in which the activation functions are assumed to be of more general description.

By introducing the equivalent descriptor form of considered system, the aim of the letter is to estimate the neuron states via available output measurements such that the estimation error converges to zero exponentially. A numerically efficient LMI approach is developed to solve the addressed problem, and the explicit expression of the set of desired estimators is characterized. Two numerical examples are used to illustrate the proposed methods.

Notations. Throughout this letter, for the symmetrical matrices X, Y, X > Y (respectively, $X \ge Y$) means that X - Y > 0 ($X - Y \ge 0$) is a positive-definite (respectively, positive-semidefinite) matrix; $\lambda_{max}(A), \lambda_{min}(A)$ denote the maximum eigenvalue and minimum eigenvalue of the matrix A, respectively. A^{T}, A^{-T} represent for the transposes of matrices A and A^{-1} , respectively. The symmetrical term in a symmetrical matrix is denoted by *, i.e.

$$\begin{bmatrix} X & Y \\ * & Z \end{bmatrix} = \begin{bmatrix} X & Y \\ Y^{\mathrm{T}} & Z \end{bmatrix}.$$

2. Problem formulations

Considering the following neural networks with discrete delays:

$$\dot{z}(t) = -Cz(t) + Ag_1(z(t)) + Bg_2(z(t-\tau(t))) + D\int_{t-\varrho(t)}^t g_3(z(s))ds + I(t),$$
(1)

where $z(\cdot) = [z_1(\cdot), z_2(\cdot), \dots, z_n(\cdot)]^T \in \mathbb{R}^n$ is the neuron state vector; $g_i(z(\cdot)) = [g_{i1}(z_1(\cdot)), \dots, g_{in}(z_n(\cdot))]^T \in \mathbb{R}^n$, i = 1, 2, 3 represents for neuron activation functions; $I(t) = [I_1(t), \dots, I_n(t)]^T \in \mathbb{R}^n$ is a time-varying input vector; $C = \text{diag}\{c_1, c_2, \dots, c_n\}$ is a diagonal matrix with $c_i > 0$; and A, B, D are the connection weight matrix, the delayed weight matrix and the distributively delayed connection weight matrix respectively. Here, $\tau(t), \varrho(t)$ denote the discrete time-varying delay and the distributed time-varying delay satisfying

$$0 \le \tau(t) \le \tau_m, \qquad \dot{\tau}(t) \le \mu, \qquad 0 \le \varrho(t) \le \varrho_m, \tag{2}$$

and τ_m , μ , ϱ_m are constants.

Remark 1. For the state estimation tasks addressed in [14,15], the delays considered are constants. However, the delays in the letter are time varying and its derivative can take any value, which means that our results are more meaningful than the ones in [14,15].

The following assumption is made on the neuron activation functions:

Assumption 1. For $i \in \{1, 2, ..., n\}$, the neuron activation functions in (1) satisfy

$$\sigma_{i}^{-} \leq \frac{g_{1i}(x) - g_{1i}(y)}{x - y} \leq \sigma_{i}^{+},$$

$$\delta_{i}^{-} \leq \frac{g_{2i}(x) - g_{2i}(y)}{x - y} \leq \delta_{i}^{+},$$

$$\rho_{i}^{-} \leq \frac{g_{3i}(x) - g_{3i}(y)}{x - y} \leq \rho_{i}^{+}, \quad \forall x, y \in R, x \neq y, i = 1, 2, ..., n,$$
(3)

where $\sigma_i^+, \sigma_i^-, \delta_i^+, \delta_i^-, \rho_i^+, \rho_i^-$ are constants.

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